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Using eddy covariance to measure the dependence of air–sea CO₂ exchange rate on friction velocity

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Abstract. Parameterisation of the air–sea gas transfer velocity of CO₂ and other trace gases under open-ocean conditions has been a focus of air–sea interaction research and is required for accurately determining ocean carbon uptake. Ships are the most widely used platform for air–sea flux measurements but the quality of the data can be compromised by airflow distortion and sensor cross-sensitivity effects. Recent improvements in the understanding of these effects have led to enhanced corrections to the shipboard eddy covariance (EC) measurements.

Here, we present a revised analysis of eddy covariance measurements of air–sea CO₂ and momentum fluxes from the Southern Ocean Surface Ocean Aerosol Production (SOAP) study. We show that it is possible to significantly reduce the scatter in the EC data and achieve consistency between measurements taken on station and with the ship underway. The gas transfer velocities from the EC measurements correlate better with the EC friction velocity ($u_*$) than with mean wind speeds derived from shipboard measurements corrected with an airflow distortion model. For the observed range of wind speeds ($u_{10N} = 3–23$ m s$^{-1}$), the transfer velocities can be parameterised with a linear fit to $u_*$. The SOAP data are compared to previous gas transfer parameterisations using $u_{10N}$ computed from the EC friction velocity with the drag coefficient from the Coupled Ocean–Atmosphere Response Experiment (COARE) model version 3.5. The SOAP results are consistent with previous gas transfer studies, but at high wind speeds they do not support the sharp increase in gas transfer associated with bubble-mediated transfer predicted by physically based models.

1 Introduction

Mass exchange across the air–sea interface is an important component of the Earth’s climate system. Uptake by the world oceans has removed approximately 25 % of the anthropogenic carbon dioxide (CO₂) emissions from the atmosphere (Le Quéré et al., 2015). Understanding the processes that control the ocean–atmosphere exchange of CO₂ is important in order to estimate global carbon fluxes and to assess the evolution and future impact of ocean uptake on Earth’s climate.

The flux of CO₂ across the air–sea interface can be written as

$$F_{CO₂} = \Delta p_{CO₂} a_{CO₂} k_{CO₂},$$

where $\Delta p_{CO₂}$, $a_{CO₂}$, and $k_{CO₂}$ are the partial pressure difference, the solubility, and the transfer velocity. The gas transfer velocity is often parameterised as a polynomial function of the mean wind speed at a height of 10 m a.s.l. ($u_{10N}$). Several different experimental approaches have been used to quantify air–sea gas exchange: (i) tracer studies utilising ambient gases ($^{14}$CO₂) (e.g. Wanninkhof, 1992; Sweeney et al., 2007) which integrate the flux over timescales of years, (ii) deliberately introduced tracers ($^3$He / SF₆) (e.g. Nightingale et al., 2000; Ho et al., 2006) which integrate the flux over
timescales of days, and (iii) direct eddy covariance (EC) flux measurements on hourly timescales (e.g. McGillis et al., 2001, 2004; Kondo and Osamu, 2007; Miller et al., 2009, 2010; Prytherch et al., 2010; Edson et al., 2011; Blomquist et al., 2014). Some EC measurements tend to support a cubic wind-speed dependence for $k_{\text{CO}_2}$, (e.g. McGillis et al., 2001; Prytherch et al., 2010; Edson et al., 2011), whereas results from tracer studies (e.g. Nightingale et al., 2000; Ho et al., 2011) and more recent EC studies (Miller et al., 2010; Butterworth and Miller, 2016a) are better fitted by a quadratic model. Gas exchange measurements at high wind speeds are rare and the extrapolation of the $k_{\text{CO}_2}$ vs. $u_{10N}$ relation leads to large uncertainties in global CO$_2$ uptake; e.g. Takahashi et al. (2002) found a 70% enhancement in annual CO$_2$ uptake when comparing cubic to quadratic wind-speed parameterisations.

EC is a method for the direct measurement of surface fluxes of momentum, heat, or trace gases at a height of a few metres above the surface (Kaimal and Finnigan, 1994). The CO$_2$ flux is defined as the covariance of the CO$_2$ mixing ratio ($x'_{\text{CO}_2}$) with the vertical wind speed ($w'$) multiplied by the dry air density ($\rho_{\text{air}}$):

$$F_{\text{CO}_2} = \rho_{\text{air}} \langle w' x'_{\text{CO}_2} \rangle.$$  

(2)

There are several challenges associated with the shipboard use of EC to measure air–sea fluxes. One is the need to correct measured wind speeds for anemometer accelerations and changes in orientation due to ship motion. Another is the disturbance of the wind field by the ship, here termed airflow distortion (AFD). The presence of the ship superstructure can lead to deflection of the wind vector and acceleration or deceleration of the mean wind speed. Uplift of air as it passes over the ship also leads to a discrepancy between the measurement height and the height from which the sampled air originated. This can lead to biased results when Monin–Obukhov similarity theory (MOST) profiles are used to extrapolate shipboard measurements to a specific reference height (typically 10 m). The resulting errors in the wind-speed measurements are sensitive to the sensor location and the orientation of the ship with respect to the wind field.

Typical approaches to deal with this problem are by careful anemometer placement, by restricting the use of data to a narrow sector of relative wind direction, or by using numerical airflow models to quantify airflow disturbance (Yelland et al., 1998, 2002; Popinet et al., 2004; O’Sullivan et al., 2013, 2015).

Direct comparisons between shipboard momentum-flux measurements and those from low-profile buoys or floating platforms (FLIPs) have shown significant differences (Pedreros et al., 2003; Edson et al., 1998). Landwehr et al. (2015) showed that these discrepancies could be explained by inappropriate application of the platform motion correction and rotation of the wind vector, which can lead to over-estimations of the deflection of the apparent wind vector and provided an adapted correction.

Another concern is airflow generated by the moving platform that is not accounted by tracking the motion of the measurement volume. Ship motion is essentially wave driven and this signal can therefore manifest itself as a residual motion peak in the flux spectra. Flügge et al. (2016) showed that residual motion-correlated signals in the momentum-flux spectra measured from a discus buoy were related to the platform motion as they were not observed in the spectra measured at a nearby tower. Prytherch et al. (2015) provided evidence that the residual motion signal in momentum-flux spectra obtained aboard the RRS James Clark Ross was caused by motion-induced flow distortion rather than by wave-induced momentum flux. They also provided a simple correction for the induced bias via linear regression of the motion-corrected wind-speed signal with the vertical acceleration and velocity signals. Similar methods were previously employed successfully by Yang et al. (2013).

The non-dispersive infrared CO$_2$ gas analysers used in most EC studies have cross sensitivities to water vapour, which lead to large uncertainties in the measurements and unrealistic transfer velocity estimates (Kondo and Osamu, 2007; Prytherch et al., 2010; Edson et al., 2011; Blomquist et al., 2014). The cross-sensitivity effect can be mitigated by the use of closed-path systems in combination with a dryer to remove water vapour fluctuations in the measurement volume (Miller et al., 2010). CO$_2$ gas analysers also exhibit motion sensitivity (Miller et al., 2010), yielding signals that may covary with motion-induced apparent winds. If not fully corrected, such signals would lead to spurious fluxes.

Here, we discuss the analysis of EC measurements of momentum and CO$_2$ fluxes taken aboard the R/V Tangaroa during the Southern Ocean Surface Ocean Aerosol Production (SOAP) study, which was conducted from February to March 2012 on the R/V Tangaroa (Law et al., 2017). The SOAP study was conducted in biologically productive waters on the Chatham Rise east of New Zealand. The CO$_2$ flux measurements were previously published in Landwehr et al. (2014). Here, the data are reanalysed using the corrections proposed by Landwehr et al. (2015) and Prytherch et al. (2015). We describe the correction methods and discuss the resulting improvements in the quality of the EC fluxes and mean wind speeds. Air–sea gas transfer velocities are calculated using continuous underway measurements of seawater and atmospheric CO$_2$, and compared with results from previous gas exchange studies.

2 Methods

2.1 Sea water, atmospheric, and flux measurements

The EC system consisted of two CSAT3 sonic anemometers mounted on the bow mast at a nominal height of 12.6 m a.s.l.. The two anemometers (port and starboard) were mounted 0.38 m away from the ship’s main axis so that the distance between the two sensing volumes was 0.76 m. An inertial
motion sensor (IMU – Systron Donner MotionPak II) measured linear accelerations and angular rates along three orthogonal axes. The motion sensor was located between and slightly aft of the sonic anemometers. Together with a GPS compass and the ship’s gyrocompass, these data were used to completely describe the ship’s motion following Miller et al. (2008). Two LI-COR non-dispersive infrared gas analysers (IRGAs) of the model LI-7500 were installed in a laboratory van on the forecastle and supplied with sample air via heated stainless steel tubing (ID = 1 cm, L = 20 m). A bypass flow system was used to provide a high flow rate of 100 standard litres per minute (slpm) through the long tubing of which a fraction (18 slpm) was passed through the gas analysers. The sample air was dried prior to analysis using a Nafion membrane dryer. The bypass flow system allowed for a high flow rate through the long sample tubing to minimise delay and loss of turbulent fluctuations. There was a pressure drop of 260 mbar between the inlet and the gas analyser. Further details on the EC system can be found in Landwehr et al. (2014).

Surface water $pCO_2$ was measured using a showerhead-equilibrator-based system followed by a drier and infrared gas analyser (LI-COR 6251). Seawater was supplied from a 5 m depth intake through the ship’s scientific seawater supply. The gas analyser was calibrated using four gas standards ranging in concentration from 0.0 to 406.8 ppmv. The pre-equilibrator-based system followed by a drier and infrared gas analyser (LI-COR 6251). Seawater was supplied from a 5 m depth intake through the ship’s scientific seawater supply. The gas analyser was calibrated using four gas standards ranging in concentration from 0.0 to 406.8 ppmv. The precision of the system is estimated to be about ±1% (Currie et al., 2011).

Wind-speed measurements from the automated weather station (AWS) positioned above the crow’s nest of the R/V Tangaroa (25.6 m a.s.l.) are also used in this study.

2.2 Simulation-based airflow distortion correction

The Gerris computational fluid dynamics (CFD) model was used to simulate flow over the R/V Tangaroa for a range of azimuth angles at 15° intervals. Gerris achieves a high degree of numerical efficiency by using an adaptive grid, increasing the grid resolution in regions of high turbulence (Popinet, 2003). The adaptive grid was limited to the 0.5 m resolution of the numerical CAD model of the ship, which did not include details such as the foremast or handrails, nor the two vans placed on the forecastle during SOAP. The large-eddy simulations (LESs) did not explicitly include viscous terms but included “numerical viscosity” associated with the discretisation provided for subgrid-scale dissipation (Popinet et al., 2004). The inflow velocity was uniform with height, rather than a more realistic logarithmic profile. The Gerris model is started with initial conditions; the flow speed and uplift predictions were obtained from a time average of the modelled time-evolving three-dimensional turbulence, after the conditions have reached steady state. The simulations were used to estimate corrections for acceleration and uplift of apparent wind at the AWS anemometer at the crow’s nest (25.6 m a.s.l.) and the two anemometers at the bow mast (12.6 m a.s.l.). The wind speeds were subsequently corrected for platform motion and converted to $u_{10N}$.

2.3 Correction for platform motion and flow distortion

In Landwehr et al. (2014), the measured wind speed was fully motion corrected before the mean tilt was estimated. This leads to an overestimation of the vertical tilt $\theta$ that scales with the ratio of the apparent and true wind speed. Here, we estimate the vertical tilt angle by rotating the apparent wind vector for each 12 min interval and subsequently applying the radial planar fit (rPF) following Landwehr et al. (2015). The vertical tilt of the wind vector varied from about 5° for beam-on-wind directions to a maximum of 12.4° for bow-on-wind directions.

The tilt in the wind vector indicates an uplift of the air passing over the ship. For the bow mast anemometers, an uplift ranging from 0.5 to 4 m was estimated from the observed momentum-flux cospectra and from LES simulations, as described in Appendix A. The estimated undisturbed height of the sampled air ($z$) was used to normalise the wind-speed measurements to a nominal height of 10 m a.s.l. On average, this resulted in $u_{10N}$ estimates about 2% higher than those based on the sampling height. The uplift estimate can also be used to improve the measurement height adjustment of other bulk measurements like temperature and humidity.

2.4 Regression of the vertical wind-speed signal with platform motion signals

Figure 1 shows average cospectra of the turbulent component of the vertical velocity with the longitudinal (along-wind) component of horizontal velocity ($nCo_{uw}$) during a 220 min period when the ship was pointed into the wind. The cospectra are shown with different levels of vertical tilt and sensor motion corrections applied.

In this example, the platform motion leads to a large negative peak in the cospectrum. This was mostly removed when the measured speed was corrected for platform motion following Miller et al. (2008). However, some residual structures remain in the frequency band of the ship’s motion ($0.07 Hz \leq n \leq 0.3 Hz$). For this data set, the structure typically consisted of two peaks in opposite directions; i.e. one added energy to the observed momentum flux and the other removed energy.

Prytherch et al. (2015) showed that the structures in the cospectrum are a measurement error related to the wave-induced platform motion and suggested a regression of the wind speeds with the platform’s acceleration and velocity signals to remove the erroneous signal. This motion-scale correction (MSC) was used with a small modification. The acceleration and velocity signals, used in the MSC, were separated into high- and low-frequency components using a complementary filter at $f_c = 0.1 Hz$. This procedure provided a much higher effectiveness of the MSC. Our inter-
Adjusting the coordinate system for this brings $nC_{ouw}(n)$ closer to the semi-empirical shape ($nC_{ouw}$, Kaimal et al., 1972). This is true, however, only for $n \leq 1$ Hz. For $n \approx 1$ Hz, the shape of $nC_{ouw}(n)$ is rather independent of $\theta$, and for $n \geq 2$ Hz the adjustment of the natural coordinate system causes $nC_{ouw}(n)$ to diverge from $nC_{ouw}^{K33}$. At those higher frequencies, $nC_{ouw}(n)$ was well matched for $\theta = 0^\circ$. In this example, $U \approx 13.5 \text{ m s}^{-1}$; hence, $n = 1$ Hz corresponds to a length scale of $\lambda = U (n)^{-1} = 1.1$ m.

In order to quantify the potential bias in the momentum flux, the integration of $nC_{ouw}$ was separated into the part below and above $n = 1$ Hz, where for the frequencies above $n = 1$ Hz, the observed cospectrum $nC_{ouw}(n \geq 1)$ was replaced with $nC_{ouw}^{K33}(\xi, U, L)$ as predicted by Eq. (A1). The bias can then be formulated as

$$\Delta u_\alpha^2 = \langle uu \rangle^{-1} \int_{1 \text{ Hz}}^{5 \text{ Hz}} \left[ nC_{ouw} - nC_{ouw}^{K33}(\xi, U, L) \right] \text{dn},$$

where $\langle uu \rangle$ is computed from the integration of $nC_{ouw}$ over the full frequency range.

The results are plotted in Fig. B3 in the Appendix. The overestimation of $u_\alpha$, as estimated from Eq. (3) is $2\%$ on average but ranges from $0$ to $6\%$ and appears to be a function of $\xi$ and $\xi^2$, which define the fraction of spectral energy at $n \geq 1$ Hz. Relative wind direction is also important in determining the overestimation of $u_\alpha$. This measurement bias could be reduced by placing the anemometer further away from the ship’s hull in order to reduce the vertical tilt of the wind vector.

In order to compare the EC-based measurements of the air-side friction velocity ($u_{10}$) with other wind-speed measurements, they are converted to $u_{10N}$ using the wind-speed-dependent drag coefficient from the Coupled Ocean–Atmosphere Response Experiment (COARE) model version 3.5 (Edson et al., 2013). This done by iterating three times through the following equations:

$$C_{D10N} = \left( \frac{\kappa}{\log_{10}(10z_0^{-1})} \right)^2,$$

$$u_{10N} = \frac{u_\alpha}{\sqrt{C_{D10N}}},$$

where ($z_0 = \nu u_{10}^{-1} + \alpha u_{10}^2 g^{-1}$) is the roughness length depending on gravity ($g$), kinematic viscosity ($\nu$), roughness Reynolds number for smooth flow ($\nu \approx 0.11$), and the wind-speed-dependent Charnock parameter:

$$\alpha = \begin{cases} 0.0017 u_{10N} - 0.005, & (u_{10N} \leq 19.4 \text{ m s}^{-1}) \\ 0.028, & (u_{10N} > 19.4 \text{ m s}^{-1}) \end{cases}$$

which is recomputed for each iteration (Edson et al., 2013).

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**Figure 1.** Average along-wind momentum-flux cospectra (220 min period, relative wind direction $\alpha = 15.5^\circ$, $u_a = 0.62 \text{ m s}^{-2}$). Shown are spectra for different tilt-motion corrections: (i) the measured wind speed corrected only for instantaneous platform orientation and wind direction ($u_{me}$) (black line); (ii) corrected for the vertical tilt of the streamline ($\theta = 10^\circ$) (dashed magenta line); (iii) the tilt-motion-corrected wind speed (Landwehr et al., 2015) (dashed grey line); (iv) additional application of the motion-scale correction (MSC), which was adapted from Prytherch et al. (2015) and regression with speed and heading (NAV) (thin blue line); (v) also shown is the semi-empirical shape of the cospectrum (Kaimal et al., 1972) (green dashed line). The shaded area marks the part of the momentum-flux signal that was removed by the MSC and NAV corrections. In this case, the reductions were $5$ and $3\%$ of the $u_a$ estimate, respectively.

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**2.5 Observation of elevated energy in the momentum-flux cospectra at high frequencies**

It is conventional in EC data analysis to “rotate” the anemometer signals to correct for sensor or airflow tilt, to satisfy the condition that $(\tau = 0)$ and $(\vec{w} = 0)$. Figure 1 illustrates the effect of this rotation on measured winds from the SOAP cruise. For this interval, the tilt of vertical was estimated to be $(\theta = 10^\circ)$ upward from horizontal $(|w_{me}| \geq 0)$. 

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2.6 Regression corrections applied to the CO2 signal

LI-7500-measured CO2 densities were converted to mixing ratios using the simultaneously measured pressure, temperature, and water vapour density in the measurement volume. The LI-7500 deployed in this experiment has sensitivity to motion (Miller et al., 2010). Following Miller et al. (2010), the residual motion signal was quantified for each 12 min interval by a linear regression of the $x_{\text{CO2}}$ signal against the three acceleration signals and subtracted from the $x_{\text{CO2}}$ signal. The LI-7500 sensors also have cross sensitivity to H2O (Kohsiek, 2000). The Nafion dryer removed humidity fluctuations effectively, reducing the ambient H2O content by 93 % (Miller et al., 2010; Landwehr et al., 2014). A similar reduction was observed for the temperature fluctuation in the tubing walls. Small (< 10 %) differences in the CO2 fluxes measured by the two LI-7500 units correlated with the residual humidity and temperature “fluctuations” measured by the dry closed-path IRGA units. The bias signal was quantified by linear regressions of $x_{\text{CO2}}$ with $x_{\text{H2O}}$ and the cell temperature $T_{\text{cell}}$, and subtracted from the $x_{\text{CO2}}$ signal. This reduced the disagreement between the CO2 fluxes measured by the two units and the scatter in the CO2 flux time series significantly. Since the variations of $T_{\text{cell}}$ and $x_{\text{H2O}}$ in the CP-IRGA are fully decoupled from the atmospheric variations by the long sample tubing and the diffusion dryer, there is no danger of removing real CO2 flux signal with this regression. The regression resulted in a small reduction of the observed CO2 fluxes ( < 2 % on average) and a 20 % reduction in variability of the flux signal. The mean, median, and standard deviation of the CO2 flux were −5.14, −4.85, and 2.60, respectively, with the regression being applied, and −5.23, −4.84, and 3.07 mol m$^{-2}$ yr$^{-1}$ without regression.

2.7 Correction of the CO2 fluxes for attenuation of high-frequency fluctuations

In order to assess the reduction of the CO2 flux signal measured with the closed-path analysers due to high-frequency attenuation, resulting from the long inlet tubing, the normalised $\langle w_{\text{CO2}} \rangle$ cospectra were compared with the cospectra of the sonic speed of sound $\langle w_{\theta_s} \rangle$. The flux loss was estimated as the ratio of the cumulative sums counting from low to high frequencies (ogives) at $n = 0.3$ Hz (Marandino et al., 2007; Blomquist et al., 2010). High-frequency fluctuations of CO2 are attenuated by the measurement system due to passage of air through the intake tubing, drier, and closed-path detector. According to similarity theory, the fraction of CO2 flux lost due to high-frequency attenuation depends on wind speed and atmospheric stability: for high wind speeds, the cospectra are shifted to higher frequencies, thus increasing the relative loss in the CO2 flux. At low wind speeds, stratification ($z/L > 0$) can suppress large-scale motion. In this case, the spectral peak is shifted to higher frequencies, when compared to neutral or unstable atmospheric stability ($z/L \leq 0$). For a moving observer, the apparent wind speed is the relevant velocity scale to predict the frequency distribution of the turbulent motion that is observed by the EC system. This is illustrated in Fig. B1 in the Appendix.

The high-frequency attenuation is assessed by comparing the normalised cospectra of CO2 (nCo$_{\text{CO2}}$) and sensible heat using the sonic temperature (nCo$_{\theta_s}$). This is based on the assumptions that the cospectra of CO2 and sensible heat are similar (Sahle et al., 2008), the measured nCo$_{\text{CO2}}$ is not attenuated, and the attenuation of the CO2 flux spectrum becomes negligible for low frequencies ($n \leq 0.3$ Hz). The last assumption was tested by using slightly higher and lower frequencies for the loss estimation. The CO2 flux data were corrected by applying a gain ($g_{\text{CO2}}$) computed as the ratio of the cumulative sums (from low to high frequencies) of sensitivities that the cospectra of CO2 and sensible heat are attenuated by the measure.

For this plot, the data set was further reduced by requiring $|\Delta T| = |T_{\text{air}} - T_{\text{sea}}| \geq 1$ K and $|\Delta p\text{CO2}| < 50$ ppm. The gain ($g_{\text{CO2}}$) for this cruise was parameterised as a function of relative wind speed $U$ and the stability function $[H(z/L)]^{3/4}$, with $H = 6.4 \zeta + 1$ taken from Kaimal et al. (1972), as follows:

$$g_{\text{CO2}} \left( U, \frac{z}{L} \right) = A_g \cdot U + B_g \cdot \left[ H \left( z \frac{z}{L} \right) \right]^{3/4} + C_g,$$  

(7)

where $A_g = 0.0038(\pm 0.0026)$(m s$^{-1}$)$^{-1}$, $B_g = 0.37(\pm 0.06)$, and $C_g = 0.61(\pm 0.07)$. This function was used to correct the measured CO2 fluxes.

On average, the correction to the CO2 flux signal was found to be 4 %. For the range of wind speeds ($U \leq 25$ m s$^{-1}$) and stratification (0 ≤ +0.2) on the SOAP cruise, the effect of stratification on the signal attenuation (0–30 %) is larger than the effect of the relative wind speed (0–10 %). It is therefore necessary to predict the attenuation of the closed-path-derived scalar fluxes based on both apparent wind speed and atmospheric stability.

2.8 Gas transfer velocity calculations

The time series of the 3-D wind speed and CO2 mixing ratio were separated into 12 min periods, over which all averages and covariances were calculated. Equation (2) was used to obtain the CO2 fluxes (unit mol m$^{-2}$ s$^{-1}$) which were converted to gas transfer velocities in units of cm h$^{-1}$:

$$k_{\text{Sc}} = \frac{(3600 \cdot 100 \cdot 10^6) F_{\text{CO2}}}{\alpha_{\text{CO2}} \cdot \Delta p\text{CO2}},$$

(8)

where $\alpha_{\text{CO2}}$(mol m$^{-3}$ atm$^{-1}$) is solubility of CO2 in sea water (Weiss, 1974).

In order to account for the influence of the sea surface temperature and salinity, the transfer velocities were normalised.
to a Schmidt number (Sc) of 660, which corresponds to CO$_2$ at 25°C.

\[
k_{660} = k \left( \frac{660}{Sc} \right)^{-n}
\]  

During SOAP, the Schmidt number varied between 820 and 960, for a Schmidt number exponent of \( n = 1/2 \); this corresponds to a normalisation factor \((Sc/660)^{1/2}\) of 1.12 to 1.21. Laboratory studies have shown a smooth transition of \( n \) from 2/3 to 1/2, when the water surface changes from smooth to rough with increasing wind speed (Jähne et al., 1984). The exact shape wind-speed dependence of this transition has been found to depend on surfactant concentration on the water surface (e.g. Frew et al., 2004; Krall, 2013). Esters et al. (2017) showed that assuming a wind-speed-dependent Schmidt number can improve gas transfer velocity parameterisations. For this work, however, the choice of Schmidt number exponent has only small effect on the overall results (for \( Sc = 900, n = 2/3 \) or \( n = 1/2 \) correspond to a change in the normalisation factor from 1.17 to 1.23). For simplicity, \( n = 1/2 \) was used for the whole data set. Equation (9) assumes that the gas transfer velocity is purely interfacial. Bell et al. (2017), however, showed that for \( u_{10N} > 10 \text{ m s}^{-1} \) bubble-mediated transfer becomes significant for the air–sea gas exchange of CO$_2$. Therefore, a more complex Schmidt number/solubility normalisation may be necessary to treat the interfacial and bubble-mediated components of the CO$_2$ gas transfer velocity separately. Due to the small range of Schmidt number variation observed during SOAP, the effect of such a normalisation on the observed wind-speed dependency of \( k_{CO_2} \) should be minor.

3 Discussion of SOAP data analysis

3.1 Effect of the tilt-motion correction on gas transfer coefficients measured underway vs. on station

As described in Sect. 2.3, the eddy covariance data were analysed using the improved tilt-motion correction developed by Landwehr et al. (2015). Figure 3 shows the impact of that correction on the SOAP CO$_2$ transfer velocities, \( k_{660}(CO_2) \). The improved correction has relatively little impact on transfer velocities measured while the ship was on station \( (u_{ship} < 1 \text{ m s}^{-1}) \), giving results that are similar to those previously published by Landwehr et al. (2014). However, the transfer velocities obtained while the ship was underway \( (u_{ship} > 1 \text{ m s}^{-1}) \) were significantly reduced (up to 20 cm h$^{-1}$) using the improved correction. The new tilt-motion correction method eliminates the systematic bias between ship on-station and ship underway data. The corresponding tilt estimates are shown in Fig. A1 in the Appendix.

3.2 Length scale dependence of the streamline coordinate system

Our observation described in Sect. 2.5 suggests that while rotation of the coordinate system into the air stream is crucial to adequately measure the contribution of large eddies, it is counterproductive for the measurement of flux carried...
by small eddies; i.e. it may be that the small-scale turbulence ($\lambda < 1 \text{ m}$) does not adjust its orientation to the new flow direction as efficiently as the large-scale turbulence. Another possible explanation could be that the magnitude of small-scale turbulence may be increased locally as a result of the shear in the tilted and accelerated airflow.

The elevated cospectral energy for $n \geq 1 \text{ Hz}$ is only observed in $nC_{uw}(n)$ while the heat flux spectra of the anemometers’ speed–sound temperature ($C_{uw}(n)$) tend to collapse into the expected $f^{-4/3}$ shape (see Fig. B2 in the Appendix). Due to the projection of the autocovariances of the three components ($u$, $v$, and $w$), the momentum-flux estimate is generally more sensitive to the choice of the coordinate system than the scalar fluxes (see Wilczak et al., 2001). The sensitivity of the $nC_{uw}(n)$ estimate to the tilt increases in the inertial subrange, where the autocovariances of the three velocity components diminish slower with increasing frequency ($f^{-2/3}$). Elevated energy in $nC_{uw}$ at high frequencies has also been observed by Butterworth and Miller (2016a), who observed wind vector tilt angles of up to $15^\circ$ with anemometers mounted on the bow mast of the R/V Nathaniel B. Palmer.

### 3.3 Effect of the airflow distortion corrections on friction velocity

Figure 4 shows the $u_*$ obtained from EC with and without the regression and high-frequency correction applied as a function of the airflow distortion corrected wind speed measured at the bow mast (average of port and starboard anemometer). The corrections lead to a reduction in the friction velocity by about 10 % and to a better correlation with the airflow distortion corrected wind speed measured at the bow mast. The $u_*$ values obtained from EC with and without the regression and high-frequency corrections are 12 and 22 % higher than the $u_*$ (bulk) derived from the bow mast wind speed using the COARE 3.5 (Edson et al., 2013), and a linear fit of $u_*$ (EC) to $u_*$ (bulk) explained 94 and 90 % of the variability, respectively. The neutral drag coefficient ($C_{D10N} = u_{*}^2/\sqrt{10 N}$) computed from the measurements showed no dependence on the true wind direction, which could have indicated an effect of the varying fetch. The measured $C_{D10N}$ varied, however, on average by about ±7 % with the relative wind direction, for relative wind directions within ±90° to the bow. The disagreement with the COARE 3.5 parameterisation is likely due to residual flow distortion errors in either the mean wind speeds or the friction velocities, which were not completely removed by the applied corrections. For the wind speeds, these can originate from (i) errors in the estimated acceleration/deceleration of the relative wind speed; (ii) errors in the estimated horizontal deflection, which will lead to minor in-accuracies in the correction for horizontal ship velocity; and (iii) errors in the estimated uplift, which would introduce bias in the wind-speed normalisation. For the friction velocities, bias in estimates can arise from (i) insufficient removal of the ship-motion signals (MSC and NAV); (ii) small inaccuracies in the tilt estimate; and (iii) uncertainties in the estimation of the elevated cospectral energy for $n \geq 1 \text{ Hz}$.

### 3.4 Wind speeds measured on free-floating catamaran as external reference

During periods of fair weather, wind speed and direction were also measured by an Airmar PB200 marine sonic anemometer at 5.6 m a.s.l. on the mast of a small catamaran. The PB200 has a root mean square (rms) uncertainty of 0.5 m s$^{-1}$ at wind speeds $< 5$ m s$^{-1}$, which increases to 1 m s$^{-1}$ for higher wind speeds. A GPS incorporated in the unit was used to correct the measured speeds for horizontal platform motion. These data can provide an external reference to assess the uncertainties associated with the corrected shipboard measurements. For this comparison, we use data collected when the catamaran was free-floating within 10 km of the ship (i.e. not dragged by the ship or small boat), and when significant wave heights were below 2.1 m. The catamaran measurements were adjusted to 10 m height neutral stability using the $u_*$ and $L$ measured with the shipborne EC system. The same adjustment using the bulk $u_*$ and $L$ derived from the AWS wind-speed measurements would result in slightly lower (<2 %) $u_{10N}$ estimates. Figure 5 shows a comparison of the $u_{10N}$ estimates from the various shipborne wind measurements with those based on the catamaran. Compared to the $u_{10N}$ estimates from the catamaran wind-speed measurements, the EC-based results are 4 % higher while the mean wind-speed-based estimates from the airflow distortion corrected shipborne measurements are 8 and 15 % lower for bow and crow’s nest anemometers, respectively. This shows that the direct EC measurements of $u_*$ enable a better estimate of the undisturbed wind speed.
than the flow distortion corrected wind speeds. Note that for the adjustment of the bow mast wind speeds the estimated height of the undisturbed streamlines ($\zeta$) has been used, which varies between 9 and 12 m a.s.l. If instead the height of the bow anemometer ($\zeta = 12.6$ m) was used to adjust the wind-speed measurements, a 2% lower $u_{10N}$ would be estimated, providing an on average 10% underestimation of the catamaran wind speeds.

### 3.5 Regression corrections and the observed correlation between wind forcing and gas transfer

Wind forcing or wind stress ($\tau = \rho_{\text{air}}u_{\ast}^2$) is the major driver of near-surface turbulence and the most important parameter to predict air–sea gas exchange of CO$_2$. In order to assess the corrections that were applied to the direct flux measurements, the measured $k_{660}(\text{CO}_2)$ were parameterised as a polynomial function of $u_\ast$. Least squares regressions of $k_{660}(\text{CO}_2)$ to $u_\ast$ were examined for different levels of corrections applied to the data (Table 1). Linear and quadratic fits gave equivalent goodness of fit for the whole data set and provided very similar results for the wind-speed range ($6 \text{ m s}^{-1} \leq u_{10N} \leq 16 \text{ m s}^{-1}$); therefore, linear fits are used here.

The Deming regression (Deming, 1943) was used, which accounts for errors in observations on both the independent and dependent variables. The ratio of the relative uncertainty ($\sigma_{u_\ast}/u_\ast : [\sigma_{u_{10N}}/u_{10N}]$) was estimated from the standard deviation of the $k_{660}(\text{CO}_2)$ and $u_\ast$ values when these were averaged over 4 h periods. The ratio of relative uncertainty was approximately 6:1 for uncorrected EC results and approximately 2:1 for the EC results with regression corrections applied, respectively. The Deming regression resulted in slightly steeper slopes than the normal linear regression, which only accounts for uncertainty in the dependent variable ($u_\ast$).

The regression corrections applied to the CO$_2$ mixing ratios and 3-D wind-speed measurements significantly improve the $k_{660}(\text{CO}_2)$ to $u_\ast$ correlation, resulting in an increase in $R^2$ from 0.35 to 0.83. These corrections did not significantly change the slope of $k_{660}$ vs. $u_\ast$. The high-frequency loss correction applied to the $k_{660}$ estimates and correction of $u_\ast$ for elevated cospectral energy at $n \geq 1$ Hz did not improve the fit further but slightly increased the slope of $k_{660}$ vs. $u_\ast$ by about 7%. Figure 6 shows a scatter plot of $k_{660}$ and $u_\ast$ for the uncorrected EC results and for the data with all motion regression corrections applied to $F_{\text{CO}_2}$ and $u_\ast$.

Table 1 also shows the results for least squares regressions of $k_{660}(\text{CO}_2)$ to $u_\ast$(bulk), which were derived from the wind speeds measured at the bow mast and at the crow’s nest (AWS).

The corrections applied in the data analysis are summarised in Table 2, which provides the range and mean of the relative bias in the EC friction velocities and CO$_2$ fluxes that were removed by each of the corrections. Most corrections, on average, reduced the results of the EC flux measurements. Only the correction for signal attenuation of the CO$_2$ fluxes in the long sample tubing caused an increase in the CO$_2$ fluxes.

---

**Figure 5.** Scatter of the normalised wind speed ($u_{10N}$) measured by the catamaran ($\zeta = 5.6$ m) and the wind-speed estimates from the ship: (i) from the bow mast friction velocity (converted via COARE 3.5); (ii) from the bow mast wind speed ($\zeta_b = [9 - 12]$ m); and (iii) from the AWS anemometer at the crow’s nest ($\zeta_M = 25.6$ m). The lines indicate the mean ratio of the shipborne wind speeds with those from the catamaran. The ratios are 1.04±0.10, 0.92±0.07, and 0.85±0.08 for the bow mast momentum flux, and the bow mast and crow’s nest wind speeds, respectively.

**Figure 6.** CO$_2$ gas transfer velocity normalised to $Sc = 660$ as a function of $u_\ast$. Shown are the direct EC estimates prior to and after the application of the regression corrections to the CO$_2$ mixing ratios and wind-speed measurements. The lines show linear fits of $k_{660}(u_\ast)$ against $u_\ast$. The linear regression explained 83% of the EC results with the regression corrections applied and 35% without regression corrections.
Table 1. Cumulative effect of various corrections on the relationship of gas transfer and friction velocity. Slope \(a\) and offset \(b\) with standard error (± SE) and coefficients of determination \(R^2\) for linear Deming regression of \(k_{660}(\text{CO}_2)\) with \(u_s\), \((k_{660} = a u_s + b)\) (Deming, 1943). The first five rows feature EC results with increasing level of corrections applied to the data. The two last rows show the results for using \(u_s(\text{bulk})\) derived from the wind-speed (wspd.) measurements on the bow mast and crow’s nest (both were corrected for airflow distortion).

<table>
<thead>
<tr>
<th>Corrections applied</th>
<th>Slope (a) (± SE) ((\text{cmh}^{-1} \text{ms}^{-1})^{-1})</th>
<th>Offset (b) (± SE) ((\text{cmh}^{-1}))</th>
<th>(R^2)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Basic EC</td>
<td>114.7 (±6.1)</td>
<td>-11.2 (±2.2)</td>
<td>0.35</td>
</tr>
<tr>
<td>EC +... + (x)(\text{CO}_2), regr.</td>
<td>98.2 (±2.7)</td>
<td>-6.4 (±1.0)</td>
<td>0.75</td>
</tr>
<tr>
<td>EC +... + MSC regr.</td>
<td>94.9 (±2.4)</td>
<td>-6.7 (±0.9)</td>
<td>0.77</td>
</tr>
<tr>
<td>EC +... + NAV regr.</td>
<td>97.6 (±2.3)</td>
<td>-6.5 (±0.8)</td>
<td>0.83</td>
</tr>
<tr>
<td>EC +... + high-freq. cor.</td>
<td>104.8 (±2.3)</td>
<td>-7.3 (±0.8)</td>
<td>0.83</td>
</tr>
<tr>
<td>Bow mast wspd.</td>
<td>114.3 (±3.0)</td>
<td>-5.0 (±0.9)</td>
<td>0.78</td>
</tr>
<tr>
<td>Crow’s nest (AWS) wspd.</td>
<td>109.4 (±2.4)</td>
<td>-3.7 (±0.7)</td>
<td>0.76</td>
</tr>
</tbody>
</table>

Table 2. Corrections to the EC data listed in the order in which they were applied. The second column indicates to which data the correction is applied. In the third column, the range of bias is given in percent of the corrected value, with negative numbers indicating that the corrected value was underestimated by the uncorrected observation. The mean and standard deviation of the relative corrections for the SOAP data are provided in the fourth column. The fifth column provides applicable references.

<table>
<thead>
<tr>
<th>Name (abbreviation)</th>
<th>Applied to</th>
<th>Range of relative bias</th>
<th>Mean (± SD)</th>
<th>References</th>
</tr>
</thead>
<tbody>
<tr>
<td>Tilt-motion correction ((rPF))</td>
<td>((u, v, w))</td>
<td>(u_s); -50 to +500 %</td>
<td>+80 (±50) %</td>
<td>Edson et al. (1998) Landwehr et al. (2015)</td>
</tr>
<tr>
<td>Motion regression ((MSC))</td>
<td>((u, v, w))</td>
<td>(u_s); -50 to +110 %</td>
<td>+3 (±10) %</td>
<td>Prytherch et al. (2015) (with modifications)</td>
</tr>
<tr>
<td>Speed/heading regression ((NAV))</td>
<td>((u, v, w))</td>
<td>(u_s); -30 to +120 %</td>
<td>+5 (±9) %</td>
<td>This work</td>
</tr>
<tr>
<td>High-frequency elevated energy</td>
<td>n(\text{Co}_{u,w})</td>
<td>(u_s); 0 to +6 %</td>
<td>+2 (±1) %</td>
<td>This work</td>
</tr>
<tr>
<td>High-frequency (^a\text{Regression with motion, } x_{\text{H}_2\text{O}}, T)</td>
<td>(x_{\text{CO}_2})</td>
<td>(F_{\text{CO}_2}); -100 to +50 % ([-200 to 300%])</td>
<td>+1.5 (±20) % ([-14 (±40)%])</td>
<td>Miller et al. (2010) (with modifications)</td>
</tr>
<tr>
<td>High-frequency (^b\text{Loss correction}) ((\times = x_{\text{CO}_2}))</td>
<td>n(\text{Co}_{u,x})</td>
<td>(F_{\text{CO}_2}); -30 to +0 %</td>
<td>-4 (±5) %</td>
<td>Marandino et al. (2007) Blomquist et al. (2010)</td>
</tr>
</tbody>
</table>

\(^a\) For the motion regression applied to the \(\text{CO}_2\) mixing ratios, the bias ranges are given for the two cases that the MSC was or was not (noted in square brackets) applied to the 3-D wind speeds.

3.6 Correlation between transfer velocity and different wind-speed estimates

In order to study how airflow distortion influenced the relationship between \(k_{660}\) and \(u_s\), the relative anomaly from the fit prediction \((\delta k = k\text{meas}/k_{660}(u_s) - 1)\) was calculated and bin averaged over 25° wind direction sectors (Fig. 7). No difference was observed when using first-, second-, or third-order polynomials to fit the data. For the airflow distortion corrected wind speed from the AWS anemometer, the anomalies showed a strong directional pattern spanning more than 25% variation. This can be attributed to airflow distortion effects (including height displacement), which were not properly accounted for by the LES model. The AWS wind speed explains 77% of the variability in \(k_{660}\). For the \(u_s(\text{bulk})\) calculated from the bow mast wind speeds (corrected for airflow distortion and effective measurement height), the directional variability is considerably reduced and the correlation explains 79% of the variability in \(k_{660}\). The \(u_s\) values derived from the eddy covariance momentum-flux measurements exhibited the least directional variability in the \(\delta k\) and explained 83% of the variability in \(k_{660}\).

Based on these results, the \(k_{660}\) values measured on SOAP are best reported as a function of the directly measured \(u_s\) (EC). This result might apply to other shipborne EC gas flux studies where disagreement between direct and bulk estimates of the momentum flux has been recorded. For example, on the R/V \(\text{Knorr}\) bow mast, \(u_s\) measured (EC)
at 13.6 m a.s.l. agreed well with the COARE prediction $u_*$ when plotted against $u_{10N}$ derived from an anemometer at 15.5 m a.s.l. When $u_{10N}$ was derived from the 13.6 m a.s.l. anemometer, the COARE prediction substantially underestimated the measured $u_*$ (EC) across a range of wind speeds (Bell et al., 2013, supplementary info). Scaling $k$ (EC) with $u_*$ or $u_{10N}$ (EC) instead of $u_{10N}$ (bulk) avoids uncertainties arising from height and stability corrections as well as potential bias arising from airflow distortion effects that might affect EC and mean wind-speed measurements differently.

4 Discussion of SOAP gas transfer velocities

4.1 SOAP gas transfer velocity as a function of friction velocity

The SOAP data set consists of 1155 measurements (231 h), ranging in wind speed ($u_{10N}$) from 3 to 23 m s$^{-1}$, with the majority of the data (95%) between 5 and 16 m s$^{-1}$. The SOAP gas transfer velocities are highly correlated with wind forcing and wind speed. For the observed range of wind speeds, the relationship to friction velocity is well described by a linear fit to the measured (EC) $u_*$ (Fig. 8).

$$k_{660} = 104.8(\pm2.3) \times u_* - 7.3(\pm0.8),$$

where the units of $k_{660}$ and $u_*$ are cm h$^{-1}$ and m s$^{-1}$, respectively. The fit explains 83% of the observed variability in the gas transfer velocity. For the wind-speed range 5–19 m s$^{-1}$, Eq. (10) predicts the wind-speed binned data within 1 standard deviation. As noted in Sect. 2.6, regressions with higher-order polynomials do not improve the fit. The SOAP gas transfer velocities exhibit much less scatter as a function of wind speed than previous CO$_2$ EC flux studies (Edson et al., 2011; McGillis et al., 2001), providing for a more precise estimate of the wind-speed dependence.

Equation (10) should not be interpreted as physical law but rather as empirical parameterisation for the wind-speed range 5–19 m s$^{-1}$. Extrapolation of this linear $k$ vs. EC $u_*$ relationship outside of the wind-speed range of the SOAP data set is not recommended, because there are physical reasons why this relationship might not hold. At lower wind speeds, buoyancy-driven processes may contribute significantly to gas transfer (Soloviev, 2007; Fredriksson et al., 2016). In fact, Eq. (10) slightly underestimates the wind-speed binned data for $u_{10N} < 5$ m s$^{-1}$ and would predict negative $k_{660}$ for $u_* \leq 0.07$ m s$^{-1}$ ($u_{10N} \leq 2.3$ m s$^{-1}$). However, since our estimations of the Richardson number ($Ri = B_0 w \nu_w u_* w$) remained below the critical value of $Ri \approx 0.004$, which was suggested by Fredriksson et al. (2016), we do not expect significant contribution of buoyancy-driven processes to the gas exchange rates observed during SOAP. Here, $B_0 w$, $\nu_w$, and $u_* w$ are the water-side surface buoyancy flux, kinematic viscosity of sea water, and water-side friction velocity, respec-
vatively. At higher wind speeds, wave breaking and bubble-driven gas transfer are expected to contribute to gas transfer of CO$_2$ and other sparingly soluble gases (Woolf, 1997; Fairall et al., 2011; Bell et al., 2017). Surprisingly, there is no evidence in the SOAP data for an increase in the slope of the $k_{660}$ vs. $u_s$ relationship at high wind speeds. If anything, the limited SOAP data available at the highest wind speeds appear to be biased low relative to the linear regression.

4.2 Comparison of SOAP results to previous gas transfer parameterisations

Most previously published gas transfer parameterisations are based on $u_{10N}$. In order to compare Eq. (10) with the $u_{10N}$-based parameterisations, the measured (EC) $u_s$ was converted to $u_{10N}$ using Eqs. (4), (5), and (6). The linear $u_s$ dependency observed on SOAP corresponds to wind-speed dependence that is greater than unity but less than quadratic (Fig. 9). At low to intermediate wind speeds ($u_{10N}$ of 4–14 m s$^{-1}$), the SOAP gas transfer coefficients are 0–20% larger than the quadratic Sweeney et al. (2007) parameterisation. Above 14 m s$^{-1}$, however, the SOAP observations are lower than Sweeney et al. (2007); e.g. at $u_{10N} = 20$ m s$^{-1}$, the Sweeney et al. (2007) parameterisation predicts 15% higher gas exchange than observed during SOAP. The SOAP gas transfer observations agree well with the Coupled Ocean–Atmosphere Response Experiment gas transfer model (COAREG 3.1) bulk flux model at low wind speeds ($u_{10N} < 11$ m s$^{-1}$; Fairall et al., 2011). At higher wind speeds, COAREG 3.1 predicts greater gas exchange than observed during SOAP. At wind speeds ($u_{10N}$) of 13, 16, and 20 m s$^{-1}$, COAREG yields 16, 45, and 90% higher gas transfer velocities than observed during SOAP, respectively. The recent high-latitude Southern Ocean EC measurements from Butterworth and Miller (2016b) agree with the observations from SOAP within the uncertainties of both data sets.

The SAGE dual tracer ($^3$He/SF$_6$) experiment was conducted in March/April 2004 in the same area as SOAP (Ho et al., 2006, 2007; Smith et al., 2011). In order to compare these data to SOAP, we corrected the QuikSCAT wind-speed measurements after Boutin et al. (2009) and converted to $u_s$ using the COARE 3.5 drag coefficient. The transfer velocities were corrected for enhancement of $k$ due to wind-speed variability following Wanninkhof et al. (2004), which leads to a 3–25% reduction of the $k$ values (Smith et al., 2011). The SAGE $k_{660}$ values were converted to $k_{660}$ using Eq. (9) with $n = 0.5$. The data from SAGE cover the wind-speed range ($u_{10N} = 7–16$ m s$^{-1}$). A linear fit to the SAGE data yields

$$k_{660} = 101.6(\pm16.4)u_s - 5.7(\pm7.9),$$

(11)
with $k_{660}$ and $u_*$ in cm h$^{-1}$ and m s$^{-1}$, respectively. The slope and intercept of this relationship are in very good agreement with the SOAP linear fit.

Smith et al. (2011) provided a quadratic fit of the SAGE data to wind speed ($k_{600} = 0.294u_{10N}$). Converting this fit to $u_*(COARE 3.5)$ yields a goodness of fit similar to that of Eq. (11) ($R^2 = 0.80$ and $R^2 = 0.81$, respectively). However, above 16 m s$^{-1}$, the SAGE quadratic relationship greatly overestimates the SOAP results. (Fig. 10).

Due to the lower $u_{10N}$ estimated by the AFD-corrected wind-speed measurements on SOAP (at the bow mast and crow’s nest), the usage of those would lead to about 20% and 10% higher $k_{660}$ values at $u_{10N} = 10$ m s$^{-1}$ and $u_{10N} = 20$ m s$^{-1}$, respectively.

5 Conclusions

Direct eddy covariance CO$_2$ and momentum-flux measurements made aboard the R/V Tangaroa during the SOAP experiment have been reanalysed using a series of established and new corrections for platform motion, airflow distortion, and sensor cross sensitivity. The wind-speed measurements from a free-floating catamaran correlated better with $u_{10N}$, which was derived from the measured $u_*$ using the COARE 3.5 drag coefficient, than with $u_{10N}$ values derived from wind speeds, which were measured on the ship and corrected for airflow distortion using a LES model. Reprocessing the SOAP data resulted in CO$_2$ gas transfer velocities with considerably less scatter than prior studies using similar instrumentation. The improved SOAP data set exhibits a strong linear correlation between CO$_2$ transfer velocity and friction velocity over a wind speed ($u_{10N}$) range of 5–19 m s$^{-1}$. This result is surprising, and suggests that the contribution of bubble-mediated CO$_2$ gas transfer may be overestimated in current physically based gas transfer models, or that a reduction of the interfacial gas transfer at high wind speeds may offset the bubble-mediated enhancement (e.g. Soloviev, 2007).

Data availability. Data availability requests can be made by email to bward@nuigalway.ie.
Appendix A: Vertical tilt and uplift estimation

Figure A1. Estimates of the vertical tilt of the wind vector from the starboard side anemometer as a function of the relative wind direction: (i) using the true wind speed in the double rotation (DR) tilt correction, as done in Landwehr et al. (2014) (orange dots); (ii) using the apparent wind speed as suggested by Landwehr et al. (2015) (blue circles); (iii) using the radial planar fit (Landwehr et al., 2015) (blue line); (iv) from the LES model of the R/V Tangaroa (Popinet et al., 2004) (red dashed line).

When the air stream approaches the ship, the streamlines are distorted by the bluff body. This leads to an uplift of the airflow passing over the ship, the streamlines can be estimated with

\[
\tilde{z} = z - \tilde{z}_{nont} \]

where \( \tilde{z}_{nont} \) is a function of the non-dimensional characteristic non-dimensional frequency is given by

\[
\langle \tilde{u}_w \rangle = \frac{A f}{f_0} \left( \frac{f_0}{f} \right)^C, \]

with

\[
A = 0.88, \quad B = 1.5, \quad C = 2.1, \quad f_0 = 0.1 \left[G\left(\tilde{z}\right)\right]^{3/4}, \]

where \( G \) is a function of the non-dimensional stability parameter \( \tilde{z} \). The squares of the residuals (weighted with the standard deviation of the frequency weighted cospectra averages) were minimised by varying \( A, B, C, f_0 \) and \( n_0 = f_0 \tilde{z} \). For all intervals with unstable to neutral stability \( \tilde{z} \leq 0 \) and \( G(\tilde{z}) = 1 \), the original height of the measured streamlines can be estimated with

\[
\tilde{z} = 0.1 \frac{\tilde{z}_{bow}}{f_0} = 0.1 \frac{U}{n_0}, \]

where \( \tilde{z}_{bow} = 12.6 \) m is the nominal measurement height above mean sea level. The estimates of \( \tilde{z} \) were bin averaged over 15° absolute wind direction bins (assuming symmetry over the ship’s main axis). The results are plotted in Fig. A2 and compared with the uplift estimates from the LES model (Popinet et al., 2004).
For wind direction at 0° to the bow, the resulting $\bar{z}$ agreed (within the uncertainties) with the predictions of the LES simulation (Popinet et al., 2004). For $20^\circ \leq |\alpha| \leq 60^\circ$, the fit to cospectra indicates a higher uplift than the LES model, while for $|\alpha| \geq 60^\circ$ the observed uplift is lower than predicted by the LES model.

Appendix B: Shape of the cospectra

The size distribution $nCo_{uw}(\lambda)$ of the turbulent energy depends on the stability parameter $\zeta$ (Kaimal et al., 1972). In an EC system, however, the turbulence is recorded as time series. The frequency distribution $nCo_{uw}(f)$ reflects the size distribution depending on the relative velocity ($f \sim \lambda U$). For a stationary observer, $U = |u|$, the true wind speed, but for a moving observer it is necessary to take the observer’s velocity ($v_{obs}$) into account ($U = |u + v_{obs}|$). This is illustrated in Fig. B1, where average normalised cospectra are shown for three scenarios:

a. with $u_a = 9.3 \text{ m s}^{-1}$, $v_{obs,a} = 0 \text{ m s}^{-1}$,
   $\Rightarrow U_a \approx 9.3 \text{ m s}^{-1}$,

b. with $u_b = 9.3 \text{ m s}^{-1}$, $v_{obs,b} = 4 \text{ m s}^{-1}$,
   $\Rightarrow U_b \approx 13.5 \text{ m s}^{-1}$,

c. with $u_c = 13.0 \text{ m s}^{-1}$, $v_{obs,c} = 0 \text{ m s}^{-1}$,
   $\Rightarrow U_c \approx 13.5 \text{ m s}^{-1}$.

This provides $u_a \approx u_b \approx 9.3 \text{ m s}^{-1}$ and $U_b \approx U_c \approx 13.5 \text{ m s}^{-1}$. The average cospectra from cases (b) and (c) are similar and shifted to higher frequencies when compared to case (a). This shows that the relative wind speed $U$, rather than the true wind speed $u$, determines the frequency distribution of the turbulent energy.

Figure B2 shows the normalised cospectra of the momentum CO$_2$ and sensible heat flux grouped for atmospheric stability as a function of the non-dimensional frequency (using $U$, $L$, and the directional dependent estimates of $\bar{z}$). As described in Sect. 2.5, for $f > 1$, the energy observed in $nCo_{uw}$ is higher than expected from the universal shape. The estimated effect on $u_a$ was however relatively small (0–6 %, on average 2 % overestimation; see Fig. B3). However, in general, the cospectra exhibit Kaimal-like shapes, mostly follow a $-4/3$ slope, and shift to higher frequencies for $\zeta > 0$, as expected. Note that the shown spectra are only weighted with the corresponding EC flux and do not therefore collapse in the inertial subrange.

Appendix C: Flux calculations and data quality assessment

The data were separated in 12 min intervals, over which all averages and fluxes were computed. For the correlation of CO$_2$ fluctuations measured in the closed-path analyser with $w'$, the optimal time lag was found by searching for the maximum covariance $\langle w'(t) x_{CO_2}(t+\delta t) \rangle$ within a reasonable range of $\delta t = 0–3$ s. For both IRGAs (dryA and dryB), the average optimal time lag was $\langle \delta t \rangle = 1.50(\pm 0.15)$ s. Individual $\delta t$ that deviated more than two samples from $\langle \delta t \rangle$...
were defaulted to \(\delta t = (\delta t)\). This was the case only for periods of relatively low \(CO_2\) fluxes and during the high-wind-speed event \(\text{doy} = (60.76\text{–}60.80)\), where residual-motion-related signals led to a strong correlation between \(w\) and \(x_{CO_2}\) at \(\delta t = 0\).

Power and cospectra are computed as fast Fourier transforms (FFTs). All spectra are smoothed and downsampled using linearly increasing averaging intervals in the frequency domain.

The quality control of the data was performed in different levels. For stage-A momentum flux, data were rejected when any of the following criteria were fulfilled:

- The vector average of the instantaneous course/heading vector was smaller than 0.90 (1 indicates a perfectly stable course). This corresponds to a maximum standard deviation of the heading of 25\(^\circ\).

- The measured relative wind direction to the bow \(|\langle\alpha\rangle|\geq 110\(^\circ\).

- The true relative wind direction to the bow \(|\langle\alpha_{\text{true}}\rangle|\geq 125\(^\circ\).

- Measured average relative wind speed \(\langle u_{mc}\rangle\leq 1\text{ m s}^{-1}\).

- Data from 20 February 2012 at 18:30 UTC to 21 February 2012 at 06:00 UTC were excluded due to malfunctioning of the starboard anemometer.

- The momentum flux computed over the 12 min period was more than 30\% different from the average momentum flux computed over five subintervals of 2.4 min.

This removed approximately 30\% of the total number of 2222 available measurements. Only a fraction of 2\% were excluded solely based on the stability test.

The \(CO_2\) flux data were discriminated based on the following stage-A criteria:

- The momentum flux failed the stage-A quality control.

- The air–sea \(CO_2\) concentration difference was low (\(|\Delta p_{CO_2}| \leq 30\text{ ppm}\).

- The rms of \(x_{CO_2}\) was larger than 0.3 ppm (the total median and restricted median and mean values of the rms were 0.07 ppm and 0.06 ppm for LI-7500 dryA and dryB, respectively).

- Strong stable atmospheric conditions (\(\frac{\theta}{\zeta} \geq +0.2\)) were excluded to reduce the uncertainty introduced by the high-frequency loss correction (see Sect. 2.7).

This removed 45\% of the total number of available measurements. Further, a total of eight measurements with negative transfer velocities were excluded.

The quality control stage B was mainly based on the shape of the cumulative sum of normalised cospectra (\(F_{\text{sum}}\)) as a function of the non-dimensional frequency with stability correction \(f = n \frac{\Delta t n}{\delta t} \left[ G\left(\frac{f}{\delta t}\right) \right]^{-2/3}\), where \(G\) is taken from Kaimal et al. (1972), to account for the shift of the spectra to higher frequencies for \(\frac{\theta}{\zeta} \gg 0\). Intervals where any of the following criteria were fulfilled for the normalised along-wind momentum-flux cospectrum were excluded:

- \(F_{\text{sum}} \leq -0.2 @ f = 0.03\text{ Hz}\)

- \(F_{\text{sum}} \geq +0.7 @ f = 0.03\text{ Hz}\)

- \(F_{\text{sum}} \geq +0.9 @ f = 0.1\text{ Hz}\)

- \(F_{\text{sum}} \leq +0.8 @ f = 1\text{ Hz}\)

- \(\text{min}(F_{\text{sum}}) \leq -0.2\)

- \(\text{max}(F_{\text{sum}}) \geq 1.1\)

- \(\text{min}(nCo_{\text{norm}}) \leq -1\)

- \(\text{max}(nCo_{\text{norm}}) \geq 2\)

The same filter was applied to the heat flux cospectra which were used for the estimation of the high-frequency flux loss in Sect. 2.7.

Accounting for the lower signal-to-noise ratio in the CO2 flux spectra and the effects of high-frequency attenuation, only the last four of the above criteria were applied as additional filters on the CO2. For both the momentum and CO2 flux, stage B removed about 6\% of the data that had passed the respective stage A.

Using \(\bar{z}, U, \text{ and } L\) with Eq. (A1) allows to estimate how much of the turbulent flux signal would be expected to be outside of the observed frequency range of \(1/720\) to \(5\text{ Hz}\).
Based on Eq. (A1), 98.3% of the theoretical momentum-flux spectrum was resolved for $U \approx 15 \text{ m s}^{-1}$ and $z_L \geq 0$. Between 98 and 98.3% of $\text{nCo}_{uw}^K$ were resolved for $15 \text{ m s}^{-1} \leq U \leq 25 \text{ m s}^{-1}$. Thus, the theoretical loss cause by the limited measurement frequency of 10 Hz was always less than 2%. Even for low wind speeds ($U \leq 3 \text{ m s}^{-1}$) and unstable stratification, the theoretically resolved fraction was not lower than 96%. The chosen flux-averaging time of 12 min was therefore adequate to resolve the turbulent air–sea fluxes.

Appendix D: Differences in wind-speed and momentum-flux estimates from the two bow mast anemometers

The relative difference between the momentum-flux/wind-speed measurements of the port and starboard anemometer illustrates the small-scale variability of the flow distortion effects but also gives an indication of the absolute flow distortion errors in the measurement of each anemometer. Figure D1 shows the relative difference of the port and starboard anemometer measurements of friction velocity and wind speed as a function of the relative wind direction. The wind speed as well as the friction velocity estimates from the two anemometer agree well with each for bow on relative wind directions. However, for increasing relative wind direction, the windward anemometer reads up to 7 and 6% higher wind speed $U$ and friction velocity $u_*$ than the leeward anemometer, respectively. The airflow distortion correction with the model results from Popinet et al. (2004) removes only 30% of the relative difference in the wind-speed measurements from the two bow mast anemometers. The MSC and NAV regression corrections clearly reduce relative differences observe in the $u_*$ measurement from the two anemometers to within ±2% for most wind direction sectors and most of the measurements. With all corrections applied, the relative difference in the $u_*$ estimates from the two anemometers is less than half of the relative difference of the wind-speed estimates.

Figure D1. Relative differences of starboard and port side measurements of $u_*$ and wind speed as a function of the relative wind direction calculated as (stbd–port) / (stbd+port) and averaged over 15° wind direction bins. The plot shows $\delta u_*/\langle u_* \rangle$ for only motion- and tilt-corrected wind speeds (grey dashed open circles) and with all regression corrections applied (blue filled circles), respectively. The relative differences of the wind-speed measurements, with and without airflow distortion correction applied, are shown as open and filled green diamonds, respectively. The black dashed line indicates the fraction of data observed in each wind direction sector. The error bars show the standard error of the mean values.
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