Radiation Characteristics of *Botryococcus braunii*, *Chlorococcum littorale*, and *Chlorella sp.* Used For CO$_2$ Fixation and Biofuel Production

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**ABSTRACT**

This paper reports experimental measurements of the radiation characteristics of green algae used for carbon dioxide fixation via photosynthesis. Such microorganisms are considered for use in ponds or photobioreactors to consume carbon dioxide present in flue gas of fossil fuel power plants as well as in life support systems for space exploration. The generated biomass can be used to produce not only biofuels but also feed for animal and food supplements for human consumptions. Particular attention was paid to three widely used species namely *Botryococcus braunii*, *Chlorella sp.*, and *Chlorococcum littorale*. Their extinction and absorption coefficients were obtained from normal-normal and normal-hemispherical transmittance measurements over the spectral range from 400 to 800 nm. Moreover, a polar nephelometer is used to measure the scattering phase function of the microorganisms at 632.8 nm. The results can be used for scaling and optimization of CO$_2$ fixation in ponds or photobioreactors as well as in the development of controlled ecological life support systems.
Keywords: radiative transfer; scattering; photobioreactors; carbon dioxide fixation; CO₂ mitigation; flue gas; bioscrubber; controlled ecological life support systems.

1 INTRODUCTION

Intensive use of fossil fuels increases concentration of carbon dioxide in the atmosphere and contributes to world climate changes [1]. For example, 71.4% of the electricity consumed in the US is generated from fossil fuel [2]. Electricity generation alone contributed to 33% of the total CO₂ emission of the country in 2006 which itself represents about 23% of the total world emission [3]. Flue gasses from fossil fuel power plants consist of 4 to 14 vol.% of CO₂ and up to 200 ppm of NOₓ and SOₓ depending on the type of fuel and on the combustion process [4]. Overall, the concentration of CO₂ in the atmosphere in 2006 varied between 360 and 390 part per million by volume (ppmv) during the year and feature a continuous increase year after year [5]. It is predicted that CO₂ levels above 450 ppm in the atmosphere will have severe impact on sea levels, global climate patterns, and survival of many species and organisms [1].

Current technologies for mitigating CO₂ can be divided in three groups namely (1) storage, (2) utilization, and (3) fixation. The most common method of storing CO₂ is monoethanolamine scrubbing [4]. Other storage technologies include (a) underground geological cavity at a depth of 6 to 800 m [6] as well as (b) surface [4] or (c) deep ocean injection [7], as well as (d) desiccant adsorption [8], and (e) molecular sieve technology [9]. Unfortunately, these storage methods suffer from major challenges including (i) the separation and compression of CO₂, (ii) the development of efficient pumping methods, (iii) uncertainties in the long term stability of the stored CO₂, and/or (iv) possible severe negative impact on the environment [4], (v) the capital and energy costs [10].

Utilization technologies either use CO₂ as is from industrial processes or convert it into useful products via some chemical processes. For example, difficult to extract oil and natural gas can be forced out of the ground through injection of CO₂ into the fields [4]. Liquid CO₂ has solvent properties and can be used in various industrial processes as an alternative to organic solvents. CO₂ can be reduced to both liquid such as methanol [11] and gaseous fuels such as methane [12] via thermochemical or electrochemical processes.

Fixation is a biochemical process where CO₂ is stored in a stable organic form through photosynthesis. Terrestrial vegetation and soil as well as the oceans are natural sinks for CO₂ [4]. The methods for increasing the rate of CO₂ sequestration through enhancement of natural sinks are (i) afforestation [13], (ii) ocean fertilization, (iii) rock weathering enhancement, (iv) algae culture in photobioreactors, and (v) artificial photosynthesis. The CO₂ consumption rate of trees vary by tree type and location. Although there are no adverse effects of this option to the ecosystem, locating and dedicating arable land for afforestation can conflict with population growth, freshwater supply, and food production for human consumption [14, 4]. In oceans, microorganisms such as phytoplankton fix CO₂ into biomass at a rate of 50 to 100 Gt-C per year [4]. This is a much higher rate than that of terrestrial vegetation ranging from 5 to 10 Gt-C per year [4]. However, this process is limited by the availability of nutrients such as nitrogen, phosphate, silicate, and iron to the microorganisms [15, 16]. Thus, fertilizing the oceans locally with these limiting nutrients can result in enhanced phytoplankton production and CO₂ uptake [15, 16]. Although promising results were obtained in field experiments [4], this option has excessive interference with the ecosystem and can have fatal impact on other marine life [17]. In addition, the sinking and decaying biomass can release stronger
greenhouse gases to the atmosphere such as methane and nitrogen dioxide [17]. Rock weathering enhancement involves carbonation of silicate rocks containing calcium or magnesium [4]. The final product is calcium or magnesium carbonate which are in solid form [18]. However, this fixation process is very slow making the natural rock weathering process impractical for industrial CO₂ sequestration [19]. Artificial photosynthesis consists of reproducing natural photosynthetic processes in a more straightforward and efficient way [20]. This approach is still in its infancy and efficiency and reliability remain major challenges.

Microalgae growth in photobioreactor addresses many of the above mentioned challenges. They have larger photosynthetic efficiencies than higher plants (e.g., trees or sugar cane) [21]. Kurano et al. [22] has demonstrated that microalgae C. littorale can fix up to 0.85 kg CO₂/m²/day in a 20 liter tubular photobioreactor having a footprint area of 6.6×10⁻² which is equivalent to 25.6 kg C/m²/year compared with 0.3-0.9 kg C/m²/year for trees [14, 23]. Microalgae require 140-200 kg of water per kilogram of C fixed compared with more than 550 kg of water per kg of CO₂ fixed by trees [14]. Unlike for trees, water for microalgae can be low quality (waste water) and even high salinity water both unsuitable for agriculture use or human consumption [14]. Thus, cultivation of these microorganisms in photobioreactors offers a sustainable method for carbon dioxide capture and storage [24, 25, 26, 27] suitable in semi-arid or arid lands without competing with human habitat or agriculture production [14]. In addition, CO₂ fixation using microalgae grown in photobioreactors does not require CO₂ capture, separation (concentration), and, scrubbing of SOₓ and NOₓ prior to using the flue gas from fossil fuel power plants. Finally, microalgae produce value-added by-products which can make the processes more economical. For example, some algal species are already used in medicinal and pharmaceutical products as well as health drinks for their immuno-stimulatory, antioxidant, antiviral, and anticancer activities [28]. Others are incorporated in novel materials or used as fertilizer, in animal feed, in aquaculture, and stock material for biofuels [29, 27].

Challenges in photosynthetic CO₂ mitigation include the relatively low efficiency and scaling of the system from bench top to industrial scale. Biological barriers such as growth inhibition due to excessive CO₂ concentration and tolerance to high temperature, NOₓ and SOₓ or toxic environment can be addressed by screening wild strains or through genetic engineering [30, 31]. Similarly, light availability to optimally perform photosynthesis is essential to achieving the maximum efficiency possible [32, 33]. In order to design, optimize, and scale up photobioreactors to maximize CO₂ fixation and sunlight energy conversion efficiency and thus minimize water usage, one needs to determine the optical properties (or radiation characteristics) of the microalgae of interest. This paper presents the optical properties of some of the most promising algae for CO₂ fixation and production of biofuels and other added-value products. The reported properties will be useful for the scaling and optimization of the CO₂ fixation in ponds or photobioreactors as well as in the development of controlled ecological life support systems (CELSS) for space exploration missions [34, 35].

2 CURRENT STATE OF KNOWLEDGE

CO₂ Consuming Microorganisms

Photosynthesis is a multi-step process by which plants and algae fix carbon dioxide into sugar using sunlight. Particularly, the step of photosynthesis at which CO₂ is converted to sugar with the help of
ATP (adenosine-5’-triphosphate) is known as Calvin cycle. The overall reaction for photosynthesis is given by,

\[
CO_2 + H_2O + \text{light} \rightarrow (CH_2O)_n + O_2
\]  

(1)

Green algae are eukaryotic organisms that can perform photosynthesis. Just like plants, they use water as their electron source, sunlight as their energy source, and CO₂ as their carbon source. In turn they produce oxygen and carbohydrates, protein, and lipids contained within the cells. They are typically more efficient than higher plant at converting solar energy into biomass thanks to their simple cellular structure and the readily available supply of CO₂ and various nutrients dissolved in water. Thus, microalgae can produce 30 times more oil than terrestrial oilseed crops for a given surface area [36].

This study focuses on three microorganisms of particular interest for CO₂ mitigation and biofuel productions namely (i) Botryococcus braunii (ii) Chlorella sp., (iii) Chlorococcum littorale [37, 25]. B.braunii is a pyramid shaped planktonic microalga. Although it is a unicellular species, B.braunii forms colonies that are held together by lipid biofilms [38]. It is interesting for its high lipid content in the form of hydrocarbon (25 to 76%) which can be converted into biofuels [39, 40, 36, 41]. It grows in freshwater and can be used as feedstock for hydrocracking in oil refinery to produce gasoline, kerosene, and diesel [42]. Moreover, Chlorella sp. is a unicellular green algae, ellipsoidal in shape with an average major and minor diameter of 12 and 9.5 μm, respectively. It has a high oil content (28 to 32%) and is widely considered for CO₂ sequestration due to its fast growth rate under large CO₂ concentrations [41, 43, 44]. The marine green algae C.littorale is a spherical unicellular strain with cells of diameter about 10 μm. It is of interest for its tolerance to high CO₂ concentrations and the fact that it can grow to very large cell density [45, 46]. Hu et al.[46] have demonstrated a CO₂ consumption rate of 16.7 g of CO₂ per liter of a flat-plate photobioreactor per day at a light intensity of 2000 μmol/m²/s at 25°C and cell density of 80 kg/m³.

The US Department of Energy Aquatic Species Program performed from 1978 to 1996 concluded the following [36]: (1) “significant potential land, water, and CO₂ resources exist to support this technology”, (2) culture of biofuel producing algae is likely to be performed in open ponds due to the low cost required to make this technology competitive. Recently, air lift photobioreactors have been demonstrated at pilot scale to reduce CO₂ emissions of a 20 MW natural gas fired cogeneration power plant [47] and a 1060 MW combined cycle gas turbine power plant [48].

**Radiation Transfer Through Microorganisms Suspensions**

Solar radiation transfer within absorbing, scattering, and non-emitting media, such as microorganism suspensions in photobioreactors or open ponds, is governed by the radiative transport equation (RTE). The RTE is a semi-empirical integro-differential equation derived from energy conservation considerations. For a given wavelength λ, it is expressed in terms of dimensionless optical coordinates as [49],

\[
\frac{dI_{\lambda}}{d\tau_{\lambda}} = -I_{\lambda}(\tau_{\lambda}, \hat{s}) + \frac{\omega_{\lambda}}{4\pi} \int_{4\pi} I_{\lambda}(\tau_{\lambda}, \hat{s}_i)\Phi_{\lambda}(\hat{s}_i, \hat{s})d\Omega_i
\]  

(2)

where \(I_{\lambda}\) is the spectral radiance (often called spectral intensity [49]) expressed in Wm⁻²μm⁻¹sr⁻¹. Here, \(\hat{s}\) is the unit vector in the line-of-sight direction and \(d\Omega_i\) is the solid angle around \(\hat{s}_i\). The dimensionless optical thickness \(\tau_{\lambda}\) and the single scattering albedo \(\omega_{\lambda}\) are defined, respectively, as

\[
\tau_{\lambda} = \int_0^s (\kappa_{\lambda} + \sigma_{\lambda})ds = \int_0^s \beta_{\lambda}ds
\]  

(3)
\[
\omega = \frac{\sigma}{\kappa + \sigma} = \frac{\sigma}{\beta}
\]  
(4)

where \(\kappa, \sigma,\) and \(\beta (= \kappa + \sigma)\) are the absorption, scattering, and extinction coefficients, respectively and expressed in \(m^{-1}\). The scattering phase function \(\Phi(\hat{s}_i, \hat{s})\) represents the probability that the radiation propagating in direction \(\hat{s}_i\) be scattered in direction \(\hat{s}\), and is normalized such that

\[
\frac{1}{4\pi} \int_{4\pi} \Phi(\hat{s}_i, \hat{s}) d\Omega_i = 1 
\]  
(5)

Note that, in the ocean optics literature, the variables \(\kappa, \sigma, \beta,\) and \(\Phi\) are often denoted by \(a, b, c,\) and \(\beta\), respectively [50, 51, 52]. In the present study, the nomenclature commonly used in the radiative heat transfer community is employed [49].

Equation (2) indicates that the absorption and scattering coefficients, or the extinction coefficient and the single scattering albedo, together with the scattering phase function are major parameters needed to solve the radiation transfer equation and predict light transfer in photobioreactors or ponds for simulation, design and optimization purposes. However, these characteristics are strongly dependent on wavelength and difficult to predict from electromagnetic wave theory given the complex morphology of the microorganisms and their various chromophores.

The extinction and absorption coefficients of microorganisms as well as the scattered intensity can be directly measured experimentally. Agrawal and Mengić [53] offered a comprehensive review of the experimental techniques for measuring these parameters. The radiation characteristics of aquatic microorganisms have been measured and reported in the literature with particular applications to ocean optics [50, 54], solar radiation conversion to algae [55, 56] and more recently for photobiological hydrogen production [57, 58].

Under single scattering regime, the radiation characteristics of microorganisms are linearly dependent on concentration [59]. Thus, it is more convenient to use the extinction and absorption cross-sections, denoted by \(E_{ext,\lambda}\) and \(A_{abs,\lambda}\), respectively, and expressed in \(m^2\). They are defined as [59],

\[
E_{ext,\lambda} = \frac{\beta}{N} \quad \text{and} \quad A_{abs,\lambda} = \frac{\kappa}{N} 
\]  
(6)

where \(N\) is the concentration of the microorganisms expressed in number of cells per \(m^3\) of liquid medium. Similarly, the scattering coefficient \(\sigma\) and the scattering cross-section \(S_{sca,\lambda}\) expressed in \(m^2\) are defined as,

\[
\sigma = \beta - \kappa \quad \text{and} \quad S_{sca,\lambda} = \frac{\sigma}{N} = E_{ext,\lambda} - A_{abs,\lambda} 
\]  
(7)

The extinction coefficient \(\beta\) is obtained from normal-normal transmittance measurements of dilute suspensions [49]. A large body of literature exists on measuring the absorption coefficient \(\kappa\) both in the field (in situ) and in the laboratory [60, 61, 62]. In situ measurements usually deal with extremely small concentrations of microorganisms and setups are designed to overcome this difficulty by increasing the path length of the sample.

To the best of our knowledge, this work presents, for the first time, experimental measurements of the radiation characteristics of microalgae considered for CO\(_2\) fixation and biofuel production over the spectral range from 400 to 800 nm as well as their scattering phase function at 632.8 nm.
3 MATERIALS AND METHODS

Microorganism Cultivation and Sample Preparation

The freshwater species *B. braunii* UTEX 572 and *Chlorella sp.* UTEX EE90 were purchased from the culture collection of algae at the University of Texas at Austin, TX, USA (UTEX) and received as living cultures on agar slants. They were cultivated in Modified Bold 3N Medium. The salt water species *C. littorale* MBIC 10280 was purchased from the Japanese Society for Culture Collection (JSCC, Japan) and received as a living culture in liquid medium. *C. littorale* was cultivated in 5% F/2 medium [63]. All strains were grown under an irradiance of 2,000 to 3,000 lux provided by fluorescent light bulbs (Ecologic by Sylvania, USA). Samples were taken from actively growing cultures of each strain during their exponential growth phase. In order to eliminate the absorption and scattering by the nutrient media, the microorganisms were centrifuged at 2,000 rpm for 5 minutes, washed, and suspended in phosphate buffer saline (PBS) solution.

Figure 1 shows micrographs of the three species considered. In addition, the cell size distribution has been quantified for each strain using a 100 µm deep hemacytometer (Hausser Scientific, USA, Model 1490) and the image processing and analysis software Image J [64]. The software approximates the cells as ellipsoids and reports the primary and secondary axes as major and minor diameters. More than 400 cells were counted for each strain. Figure 2 shows the number frequency of the major and minor diameters of the cells for all strains with bins 0.1 µm in width. Table 1 summarizes the average major and minor diameters and the associated standard deviation for each

![Micrographs](image)

Figure 1: Micrographs of (a) *B. braunii*, (b) *Chlorella sp.*., and (c) *C. littorale*.
strain. It also reports the average (i) circularity defined as $C = 4\pi A/P$ where $A$ and $P$ are the projected area and perimeter of the cell, and (ii) the Feret diameter defined as the longest distance between two points along the perimeter of a particle [64].

Microorganism concentrations were determined using calibration curves that relate the optical density (OD) at 750 nm of a microorganism suspension to both the dry cell weight $X$ (in kg/m$^3$) and the number of cells per unit volume of liquid $N$ (in cells/m$^3$). The optical density is defined at 750 nm as $OD = -\log_{10}(T_{750}/T_{750,PBS})$, where $T_{750}$ and $T_{750,PBS}$ are the transmittances at 750 nm of the microorganism suspended in PBS and of PBS alone, respectively. The calibration curves were created by measuring the dry cell weight and the number of cells per unit volume for a given value of OD. First, the OD of the microorganisms was measured at 750 nm in disposable polystyrene cuvettes with path length of 10 mm [27] using a UV-Vis spectrophotometer (Cary-3E by Varian, USA). Then
Table 1: Mean diameters, their standard deviations, circularity, and Feret diameter along with parameters associated with the Henyey-Greenstein asymmetry factor for the scattering phase function of CO₂ consuming microorganisms investigated.

<table>
<thead>
<tr>
<th></th>
<th>B. braunii</th>
<th>Chlorella sp.</th>
<th>C. littorale</th>
</tr>
</thead>
<tbody>
<tr>
<td>Average major diameter (µm)</td>
<td>13.3</td>
<td>12.0</td>
<td>9.6</td>
</tr>
<tr>
<td>Standard deviation of major diameter (µm)</td>
<td>4.3</td>
<td>4.9</td>
<td>3.9</td>
</tr>
<tr>
<td>Average minor diameter (µm)</td>
<td>10.3</td>
<td>9.5</td>
<td>8.1</td>
</tr>
<tr>
<td>Standard deviation of minor diameter (µm)</td>
<td>2.5</td>
<td>2.9</td>
<td>2.3</td>
</tr>
<tr>
<td>Circularity</td>
<td>0.85</td>
<td>0.86</td>
<td>0.91</td>
</tr>
<tr>
<td>Feret diameter (µm)</td>
<td>14.1</td>
<td>12.8</td>
<td>10.4</td>
</tr>
<tr>
<td>Chl a (g/kg dry cell)</td>
<td>183.99 ± 16.35</td>
<td>19.21 ± 0.72</td>
<td>18.42 ± 0.43</td>
</tr>
<tr>
<td>Chl b (g/kg dry cell)</td>
<td>135.05 ± 10.81</td>
<td>28.93 ± 2.37</td>
<td>50.08 ± 0.24</td>
</tr>
<tr>
<td>Total Chl (g/kg dry cell)</td>
<td>319.04 ± 24.01</td>
<td>48.14 ± 2.95</td>
<td>68.50 ± 0.26</td>
</tr>
<tr>
<td>H-G asymmetry factor g</td>
<td>0.986</td>
<td>0.979</td>
<td>0.970</td>
</tr>
</tbody>
</table>

the cells were counted using the hemacytometer and Image J software. Finally, the microorganism suspensions were filtered through mixed cellulose filter membranes with 0.45 µm pore size (HAWP-04700 by Millipore, USA) and dried at 85°C over night. The dried filters were weighed immediately after being taken out of the oven on a precision balance (model AT261 by Delta Range Factory, USA) with a precision of 0.01 mg. Figure 3 shows calibration curves for N and X versus OD at 750 nm using a 1 cm path length cuvette. It enables conversion between these commonly used units. The cell number density combined with microorganism shape, size distribution, and chlorophyll content is important for theoretically predicting radiation characteristics of algal suspensions [65].

Finally, the chlorophyll a and chlorophyll b concentrations were determined for each strain using the ethanol extraction method developed by Wintermans and De Mots [66]. Measurements were performed at least at four different times between two consecutive transfers. The chlorophyll a and chlorophyll b, and total chlorophyll concentrations, expressed in gram of chlorophyll per kilogram dry cell of microorganism, are reported in Table 1 for the three microorganisms considered. B. braunii features significantly larger Chl a and Chl b concentrations as also suggested by the calibration curves shown in Figure 3. C. littorale has Chl a concentration similar to that of Chlorella sp. but larger Chl b concentration. C. littorale algae are also smaller and it remains unclear how their radiation characteristics will compare.

Experimental Procedure and Analysis

In measuring the radiation characteristics, the following assumptions were made: (1) the microorganisms were well mixed (i.e., randomly distributed) and randomly oriented, (2) for all measurements, the path length and the concentration of the samples were such that single scattering prevails, i.e., photons underwent one scattering event at most as they travel through the suspension, (3) the scattering phase function had azimuthal symmetry and was only a function of the polar angle [49]. Moreover, the scattering phase function for large particles does not vary significantly with wavelength at scattering angles less than 15° [50]. Most of the scattered light is in the forward direction and phase function measurements taken at 632.8 nm can be used as a first order approximation for modeling light transfer in photobioreactors over the photosynthetically active region (PAR) ranging
Figure 3: Calibration curves showing cell density and dry weight concentration as functions of optical density (OD) at 750 nm and for 10 mm path length for (a,b) B.braunii, (c,d) Chlorella sp., and (e,f) C.littorale.
from 400 to 700 nm.

The scattering phase function at 632.8 nm was measured by a polar nephelometer. Details of the experimental setup and the associated analysis have been reported elsewhere [57] and need not be repeated. Validation was performed with Latex microspheres 5 and 19 µm in diameter and randomly oriented fibers 17 microns in diameter and about 1 cm long to treat them as infinitely long. Good agreement was observed between experimental data and results predicted from the Mie theory for spheres [67] and infinitely long and randomly oriented cylinders [68].

The extinction coefficient $\beta_\lambda$ of each species was measured from normal-normal transmittance measurements $T_{\lambda,X}$ over the spectral range from 400 to 800 nm using a UV-VIS-NIR spectrophotometer (Shimadzu, USA, Model UV-3101PC). The results were corrected for the portion of the light scattered in the forward direction and detected by the spectrophotometer in directions other than the normal direction due to the finite size of the acceptance angle [58]

Finally, the absorption coefficient $\kappa_\lambda$ was determined from the hemispherical transmittance measurements performed with an integrating sphere [55] combined with the same UV-VIS-NIR spectrophotometer used for measuring $\beta_\lambda$. The measurements were corrected for scattering errors using the analysis suggested by Davies-Colley [51]. The experimental setups and analysis for measuring $\beta_\lambda$ and $\kappa_\lambda$ were validated for polystyrene microspheres with diameter of 5 µm and standard deviation of 0.6 µm supplied by Duke Scientific Corp., USA (Part No: 2005A). Experimental results were in good agreement with predictions from Mie theory assuming polystyrene to be non-absorbing. Details of the experimental setup, analysis, and validation can be found in Refs.[57, 58].

4 RESULTS AND DISCUSSION

All normal-normal and normal-hemispherical transmittance measurements were performed twice and the arithmetic average of the results is reported. The relative difference between the replica measurements was less than 0.9% over the entire spectral region considered and for all microorganisms.

Cross-sections of *B. brauni*

Figures 4(a), (c), and (e) show the absorption $\kappa_\lambda$, extinction $\beta_\lambda$, and scattering $\sigma_\lambda$ coefficients of *B. brauni* measured at three different microorganism concentrations, namely $6.6986 \times 10^{10}$, $1.2796 \times 10^{11}$, and $2.2544 \times 10^{11}$ cells/m$^3$ in the spectral region from 400 to 800 nm.

Figure 4(a) shows that *B. brauni* have absorption peaks at 435, 475, and 676 nm. The peaks at 435 and 676 nm correspond to the absorption peaks of in vivo chlorophyll *a* [69]. In addition in vivo chlorophyll *b* has absorption peaks at 475 and 650 nm [69]. Thus, the absorption peak at 475 nm and the peak broadening around 650 nm observed in Figure 4(a) can be attributed to the presence of chlorophyll *b*. The chlorophyll *a* and *b* pigments are responsible for absorbing solar radiation and generating electrons that drive the metabolic reactions of the microorganisms.

In addition, Figures 4(b), (d), and (f) show the spectral absorption, extinction, and scattering cross-sections $A_{abs,\lambda}$, $E_{ext,\lambda}$, and $S_{sca,\lambda}$ over the spectral region from 400 to 800 nm. The cross-sections $A_{abs,\lambda}$, $E_{ext,\lambda}$, and $S_{sca,\lambda}$ collapse on a single line for the two largest microorganism concentrations considered. This demonstrates that multiple scattering is negligible for the concentrations considered as assumed in the data analysis. Some wiggles in $S_{sca,\lambda}$ and $E_{ext,\lambda}$ can be
Figure 4: The (a) absorption $\kappa_{\lambda}$, (c) extinction $\beta_{\lambda}$, and (d) scattering $\sigma_{\lambda}$ coefficients and the corresponding (b) absorption $A_{\text{abs},\lambda}$, (e) extinction $E_{\text{ext},\lambda}$, and (f) scattering $S_{\text{sca},\lambda}$ cross-sections of *B. braunii* over the spectral range from 400 to 800 nm at three different microorganism concentrations.

observed for the smallest concentration resulting in relative difference less than 10% with the other two concentrations. This could be attributed to interferences within the cuvette occurring at low
concentrations. Interferences do not occur for larger concentrations as the reflected beam is absorbed by the microorganisms and its intensity is much smaller than the incident beam. Overall, Figures 4(b), (d), and (f) establishes that (1) the cross-sections $A_{\text{abs},\lambda}$, $E_{\text{ext},\lambda}$, and $S_{\text{sca},\lambda}$ are independent of concentration $X$, (2) scattering dominates over absorption at all wavelengths between 400 and 800 nm.

**Cross-sections of Chlorella sp.**

Figures 5(a), (c), and (e) show the absorption $\kappa_\lambda$, extinction $\beta_\lambda$, and scattering $\sigma_\lambda$ coefficients of *Chlorella sp.* measured at three different concentrations, namely $2.9153 \times 10^{11}$, $3.1711 \times 10^{11}$, and $3.8985 \times 10^{11}$ cells/m$^3$ in the spectral region from 400 to 800 nm. Here also, absorption peaks are apparent at 435, 475, and 676 nm corresponding to Chl $a$ and Chl $b$ as previously discussed for *B.brauni*. The difference lies in amplitude of the cross-sections which are smaller for *Chlorella sp.* for all wavelengths considered. This can be attributed to the fact that *Chlorella sp.* has smaller Chl $a$ and Chl $b$ concentrations than those of *B.brauni* as evident from Table 1. Indeed, *Chlorella sp.* has 90% and 78% less Chl $a$ and Chl $b$ concentrations than *B.brauni*, respectively.

**Cross-sections of C.littorale**

Figures 6(a), (c), and (e) show the absorption $\kappa_\lambda$, extinction $\beta_\lambda$, and scattering $\sigma_\lambda$ coefficients of *C.littorale* measured at three different concentrations, namely $3.2624 \times 10^{11}$, $3.6708 \times 10^{11}$, and $4.8106 \times 10^{11}$ cells/m$^3$ in the spectral region from 400 to 800 nm. The same absorption peaks at 435, 475, and 676 nm corresponding to chlorophyll $a$ and chlorophyll $b$ are observed along with trends similar to those observed for *B.brauni* and *Chlorella sp.* for the extinction and scattering cross-sections.

The absorption cross-section of *C.littorale* is the smallest of the three microorganisms considered. Its scattering cross-section is larger than that of *Chlorella sp.* by 15% but smaller than that of *B.brauni* by 40% to 50%. This can be attributed to the complex and non-intuitive relationships between $A_{\text{abs},\lambda}$, $E_{\text{ext},\lambda}$, and $S_{\text{sca},\lambda}$ and the chlorophyll concentrations and microorganisms size and shape.

Finally, Figure 7 compares the spectral extinction coefficients $E_{\text{ext},\lambda}$ and single scattering albedos $\omega_\lambda$ of *B.brauni*, *Chlorella sp.*, and *C.littorale* as a function of wavelength between 400 and 800 nm. A slight increase in $E_{\text{ext},\lambda}$ with wavelength can be observed for all algae with a dip between 670 and 680 nm. The extinction coefficient of *Chlorella sp.* falls within 10% of that of *C.littorale* while that of *B.brauni* is larger than the others by at least 40% and up to 70% over the spectral range of interest. On the contrary, the single scattering albedos of the three microorganisms fall within less than 8% of each other. In all cases, $\omega$ is larger than 0.7 indicating that scattering dominates over absorption.

**Scattering Phase Functions of All Strains**

Finally, the scattering phase functions of the three microorganisms of interest were measured using the nephelometer described in details in Refs.[57]. Due to the finite size of the probe and the beam, data could only be obtained for scattering angle $\Theta$ up to 140° where the probe does not block the incident beam. Figure 8 shows the scattering phase functions of *B.brauni*, *Chlorella sp.*, and *C.
Figure 5: The (a) absorption $\kappa_{\lambda}$, (c) extinction $\beta_{\lambda}$, and (d) scattering $\sigma_{\lambda}$ coefficients and the corresponding (b) absorption $A_{\text{abs},\lambda}$, (d) extinction $E_{\text{ext},\lambda}$, and (f) scattering $S_{\text{sca},\lambda}$ cross-sections of *Chlorella sp.* over the spectral range from 400 to 800 nm at three different microorganism concentrations.

*littorale* measured by the nephelometer along with the Henyey-Greenstein scattering phase function (HG). The latter is given by [49],
Figure 6: The (a) absorption $\kappa_\lambda$, (c) extinction $\beta_\lambda$, and (d) scattering $\sigma_\lambda$ coefficients and the corresponding (b) absorption $A_{\text{abs},\lambda}$, (d) extinction $E_{\text{ext},\lambda}$, and (f) scattering $S_{\text{sca},\lambda}$ cross-sections of *C. littorale* over the spectral range from 400 to 800 nm at three different microorganism concentrations.

$$\Phi_{HG} = \frac{1 - g^2}{[1 + g^2 - 2g\cos\Theta]^{3/2}} \quad (8)$$
Figure 7: Average extinction coefficient and single scattering albedo of \( B.braunii \), \( Chlorella \ sp. \), and \( C.littorale \) between 400 and 800 nm.

Figure 8: The scattering phase function of (a) \( B.braunii \), (b) \( Chlorella \ sp. \), and (c) \( C.littorale \) at 632.8 nm obtained experimentally and the corresponding HG approximation.

where \( g \) is the Henyey-Greenstein asymmetry factor defined as the mean cosine of the experimentally measured scattering phase function and was computed for each strain. Its values for each strain are
summarized in Table 1.

5 CONCLUSION

This paper has been concerned with experimental measurements of the radiation characteristics of three species of CO$_2$ consuming algae with large oil and protein content namely B.brauni, Chlorella sp., and C.littorale. Such data are difficult to predict theoretically and are essential to the design and scaling of industrial systems for CO$_2$ fixation and biofuel production as well as for controlled ecological life support systems. Experimental results establish that for all strains, scattering dominates over absorption. The magnitude of the extinction and scattering cross-section are functions of the size, shape, and chlorophyll content of each strains in a non-trivial manner. Absorption peaks at 435, 475, and 676 nm corresponding to chlorophyll $a$ and chlorophyll $b$ have been clearly identified.

NOMENCLATURE

\begin{align*}
A_{abs,\lambda} & \quad \text{spectral absorption cross-section } [\text{m}^2] \\
E_{ext,\lambda} & \quad \text{spectral extinction cross-section } [\text{m}^2] \\
g & \quad \text{Henyey-Greenstein asymmetry factor} \\
I_\lambda & \quad \text{radiance (intensity) } [\text{W/m}^2.\mu\text{m.sr}] \\
L & \quad \text{cuvette path length } [\text{m}] \\
n & \quad \text{refractive index} \\
N & \quad \text{Microorganism cell density } [\#/\text{m}^3] \\
OD & \quad \text{optical density} \\
\hat{s} & \quad \text{local spatial coordinate unit vector} \\
S_{sca,\lambda} & \quad \text{spectral scattering cross-section of microorganisms } [\text{m}^2] \\
t & \quad \text{sample thickness } [\text{m}] \\
T & \quad \text{transmittance } [%] \\
X & \quad \text{microorganism concentration } [\text{kg/m}^3] \\
x & \quad \text{size parameter} \\
\beta & \quad \text{extinction coefficient } [1/\text{m}] \\
\Theta & \quad \text{scattering angle } [\text{rad}] \\
\kappa & \quad \text{absorption coefficient } [1/\text{m}] \\
\lambda & \quad \text{wavelength } [\text{nm}] \\
\Omega & \quad \text{solid angle } [\text{sr}] \\
\sigma & \quad \text{scattering coefficient } [1/\text{m}] \\
\tau & \quad \text{nondimensional optical thickness} \\
\Phi & \quad \text{scattering phase function} \\
\lambda & \quad \text{refers to wavelength} \\
h & \quad \text{refers to normal-hemispherical measurements} \\
HG & \quad \text{refers to Henyey-Greenstein phase function}
\end{align*}
PBS refers to phosphate buffer saline solution

References


