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De-excitation Rates for He\(^+\) (2S) in Collision with Atoms and Molecules.\(^\dagger\)

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ABSTRACT

We have studied the de-excitation of He\(^+\) ions in the 2S metastable state by collision with eleven different target gases. These include noble gases, symmetric linear molecules, water and ammonia. From our data we extract velocity averaged total de-excitation rate constants, \(\langle \sigma v \rangle\), ranging from 1.65(17) \times 10^{-9} to 20.9(21) \times 10^{-9} \text{ cm}^3 \text{ sec}^{-1} \) for helium and ammonia, respectively. In all cases the mean energy of the He\(^+\) ions was \(\approx 0.44\) eV and the target gases had a 300\(^\circ\)K Maxwell-Boltzmann distribution of velocities. The results are consistent with collision induced Lyman-\(\alpha\) emission being a prominent de-excitation mechanism.
I. Introduction

In the past a fair amount of experimental and theoretical effort has been expended on the problem of the de-excitation of hydrogen atoms in the metastable 2S state by near thermal energy collisions with atoms and molecules. Both experimentally and theoretically the problem seems to be tractable, a circumstance which adds the usual synergistic term to the rate of progress. Most recently there has been the experimental work of Kass and Williams,\textsuperscript{1} Czuchlewski and Ryan\textsuperscript{2}, and Comes and Wenning.\textsuperscript{3} Preceding these was the pioneering work of Fite\textsuperscript{4,5} and collaborators. On the theoretical side recent papers by Byron\textsuperscript{6} and Gersten\textsuperscript{6,7} and Slocomb, Miller and Schaeffer\textsuperscript{8} are notable.

In this work we report experimental studies of the nearly analogous problem of collisional de-excitation of He\textsuperscript{+}(2S). Exact analogy fails because the positive charge of the ion plays an important role, but the broad picture of the de-excitation process remains.

Briefly, the current understanding is that the transient electric field seen by the metastable projectile during its passage near a target atom or molecule mixes the 2S and 2P states via the Stark interaction, leaving it with a finite probability of being in one of the 2P states after the collision. Since the lifetime of the 2P state is very short (\(\approx10^{-9}\) sec for H, \(10^{-10}\) sec for He\textsuperscript{+}), the projectile returns to the ground (1S) state emitting a Lyman-\(\alpha\) photon (\(\lambda = 300\)Å for He\textsuperscript{+}) long before it can meet another target.
The interaction potential responsible for the transient field will depend, of course, upon the nature of the target and the charge of the hydrogen-like metastable projectile. In the case of H(2S) in collision with a spherical target (e.g. a noble gas atom) the interaction is, roughly, that of the transient (2S + 2P) quadrupole moment interacting with the electric field produced by the dipole induced in the target by the (2S + 2P) dipole moment. Thus it is proportional to the polarizability of the target and has a $r^{-7}$ dependence on the separation $r$. In the case of molecular collisions the interaction is generally of longer range being via the electric multipole field surrounding the target. Thus for polar molecules the interaction potential is proportional to the molecular dipole moment and falls as $r^{-3}$. When the metastable projectile is charged, as with He$^+(2S)$, one has in addition to consider the interaction induced by the Coulomb field. This yields a potential proportional to the target dipole polarizability and varying as $r^{-4}$.

The de-excitation rates measured in this work are total rates; i.e. they are the sum of the rates for all processes leading to de-excitation of He$^+(2S)$. Since He$^+(2S)$ possesses 40.8 eV of excitation energy, a host of de-excitation mechanisms are possible. The most probable are induced Lyman-$\alpha$ decay as described above and non-radiative de-excitation with simultaneous ionization of the target (Penning ionization); i.e. the process,

$$\text{He}^+(2S) + \text{X} \rightarrow \text{He}^+(1S) + \text{X}^+ + e^-.$$
In addition when the target is a molecule, a number of ion-neutral reactions are possible. Many of these would lead to dissociation and ionization of the target molecule. Very little, if any, information is available for rates of such processes when the projectile is a highly excited metastable ion such as He⁺(2S). We believe, however, that regardless of the target, the induced Lyman-α rate accounts for more than half of the total de-excitation rate. We present some experimental evidence which shows that for collisions with He, it is a prominent process.

II. Experimental Method

The present work is an outgrowth of an experiment⁹ carried out to measure the free lifetime, τ₀, of He⁺(2S). The result of that experiment was τ₀ = 1.922(82) msec. which is in agreement with the theoretical value¹⁰ of 1.899 msec. The same apparatus was used in these experiments with some modifications, principally to allow absolute measurement of target gas pressure increments.

The unperturbed 2S state decays by emission of two electric dipole photons¹¹ with energies such that hν₁ + hν₂ = 40.8 eV. The single photon distribution is then a continuous one with a short wavelength cutoff at λₘᵋₙ = 304 Å and extending to infinite wavelength.
The distribution\textsuperscript{12} rises rapidly from $\lambda_{\text{min}}$ to a peak at $\approx 350\AA$ after which the intensity falls off roughly as $\exp[-(\lambda-350)/430]$.

The method used is based on the following simple ideas. If one has a quantity $N$ of He\textsuperscript{+}(2S) ions confined to some volume containing a density $n_{\text{He}}$ of helium atoms and $n$ of target atoms or molecules then the usual simple first order differential equation applies to the variation of $N$ with time;

$$\frac{dN}{dt} = -N(A+\sigma_{\text{He}} n_{\text{He}} + \sigma n)$$

where $A = 1/\tau_0$, $\sigma_{\text{He}}$ and $\sigma$ are total de-excitation cross-sections for collisions with helium and the target of study; $v$ is the relative collision velocity (here assumed to be the same for each type of collision). The solution is

$$N(t=0) e^{-t/\tau},$$

where

$$\frac{1}{\tau} = A + \sigma_{\text{He}} n_{\text{He}} + \sigma n$$

Thus, if one holds $v$ and $n_{\text{He}}$ constant, a plot of the measured quantities $1/\tau$ vs. $n$ should yield a straight line whose slope is the product $\sigma v$. If one has a unique and known value of $v$ then one could extract $\sigma$. In these experiments, however, one has present a distribution of relative velocities so that the quantity derived from such a plot is $R = \langle \sigma v \rangle$, the velocity averaged product. It turns out that the distribution of $v$ present in the measurements reported here is, to a good approximation, independent of the target, and hence trends in $R$ reflect trends in $\sigma$. 
The technique used to measure $1/\tau$ vs $n$ is as follows. A quantity ($\approx 10^2$) of He$^+(2S)$ ions are created by pulsed electron impact on He gas ($p_{He} \approx 10^{-6}$ Torr) at time $t = 0$. The ions are confined inside an electromagnetic ion trap for a period of 4 msec. During this storage time the He$^+(2S)$ ions make collisions with the He gas and with the target gas at a pressure $p$; single decay photons are detected by windowless electron multipliers and the resulting pulses are stored versus time in 100 channels of a multichannel scalar (40 μsec/channel). At the end of the storage period, all ions are dumped from the trap and a new cycle is begun. Many fill-store-dump cycles are repeated until a decay curve is accumulated with sufficiently small statistical fluctuations to allow determination of a value for $\tau$. This may take from 15 minutes to 2 hours depending on the experimental conditions. The whole process is repeated for different values of $p$ to determine the line $1/\tau$ vs $n$ ($n = p/kT$).

Figure 1 shows the ion trap and photon detectors. The ion trap is a closed cylinder (radius $\approx 15$ cm, length $\approx 30$ cm) whose ends are maintained at a positive potential with respect to the body; the potential difference during these measurements was 2.0 volts. A magnetic field of $\approx 60$ gauss was applied coaxial with the cylinder by means of coils external to the vacuum enclosure. The electrostatic field confines ion motion along the magnetic field, while the magnetic field limits motion perpendicular to the trap axis.
The trap is constructed primarily from oxygen-free high-conductivity copper, stainless steel, and alumina insulators; the vacuum enclosure is entirely of stainless steel. After bake-out pressures of <2 x 10^{-9} Torr have been achieved, however during these measurements the background pressure was more typically ≈ 8 x 10^{-8} Torr. Helium and target gases are admitted to the chamber containing the trap via separate micrometer controlled variable leak valves. These in turn are connected to separate gas handling systems. The micrometer valves allowed sensitive control of $p_{\text{He}}$ and $p$ during the measurements. A quadrupole residual gas analyzer is attached to the chamber and is used to monitor the constituents of the background gas and the purity of the admitted target gas.

Helium ions are created inside the trap by impact from an electron pulse accelerated along the axis. Typically the electron pulse is 4.0 $\mu$A, last 0.75 msec, and has an energy of 225 eV. At a helium pressure of 8 x 10^{-6} Torr this yields about 10^6 ions, of which about 10^3 can be expected to be in the 2S metastable state. At the end of a storage period the trap potentials are altered so that ions are dumped onto a collecting plate (electrode 4 in Fig.1); this allows monitoring of the number of stored ions via the size of the resulting positive current pulse which was displayed on an oscilloscope and averaged via a boxcar integrator. The electron pulse also appears on this electrode during the trap fill time. Of course, background and target gas ions are created by the electron pulse in addition to He ions. However, except for the case when the target gas is $H_2$, 
these ions have too small a charge to mass ratio to be confined and in a fraction of a millisecond leave the trap volume -- only the He ions remain. The heavy ions do compete for space in the trap, however, during the fill period and the transient period during which they leak from the trap, and, since the trap has a finite capacity for confined charge (≈10^7 positive charges), they affect the number of He ions which are ultimately stored for a given electron pulse. One observes a decrease in the number of stored He ions when one holds the electron pulse and p_{He} constant and increases p. This effect is one of the factors limiting the range over which p may be varied for a given target.

As is indicated in Fig.1, the cylindrical portion of the trap is made up of two half cylinders 2a and 2b; this allows application of an alternating potential between them (while maintaining a common dc potential) which can excite resonant motion of the stored ions at their cyclotron frequency. At resonance the ions gain energy from the ac field until they strike the electrodes or chamber walls; thus one observes a drop in the ion dump-pulse amplitude when the applied frequency is in resonance. In addition to the cyclotron resonance, one observes resonance at the frequency of motion along the trap axis (z-motion) and at the magnetron frequency (frequency of drift of the cyclotron orbit center about the trap axis). To excite the z-motion resonance it is more convenient to apply the ac potential between electrodes 1 and 2a, 2b connected together.

Observation of the z-motion resonance allows determination of
the effective harmonic potential well depth, \( W \), along the \( z \)-axis. Thus \( W = \frac{k z^2}{2q} \) where \( k = m(2\pi f_z)^2 \) and \( z_m \) is the maximum amplitude of \( z \)-motion, \( q \) the ion's charge, \( m \) its mass, and \( f_z \) the \( z \)-motion frequency. For helium ions with trap potentials as described above, \( f_z \) was measured to be \( f_z = 7.98(50) \) kHz. With \( z_m = 12.9 \) cm one obtains \( W = 87(11) \) eV.

The photon detectors are two BNI 9642/2 eighteen-stage CuBe Venetian blind electron multipliers. To prevent metastable helium atoms (\( 2^3S_1 \) and \( 2^1S_0 \)) as well as metastable background and target gas atoms or molecules from reaching the multipliers, their view of the storage volume is covered by aluminum foils 18 mm in diameter and 800 Å thick. The foils have a transmission varying between 10% and 70% over the region 200 to 700 Å. The Al-foil, CuBe-multiplier combination responds to \( \approx 2\% \) of the radiation over the range 300 to 500 Å which strikes the Al foil. The two light pipes are Pyrex tubes coated internally with a 1000 Å thickness of gold; they enhance the count rate by about a factor of 4 over the case with no light pipes.

To establish that the observed decay is that from \( \text{He}^+(2S) \) microwave power (\( \approx 150 \) mW) at the Lamb-shift frequency (14.045 GHz) is broadcast into the trap volume via a wave-guide horn. This converts a large fraction (more than 80%) of the 2S ions to the \( 2P_{1/2} \) state from which they immediately decay, destroying the 2S decay curve. The microwave power is generated by a Varian X-12 klystron and may be on-off modulated via a pin-diode switch under control of the data collection logic system.
One typical data cycle consists of the following sequence:
a 0.75 msec fill period during which the electron pulse is on, a
delay period of 0.8 msec during which the microwave power may or may
not be applied, a storage period of 4 msec during which counts from
the multipliers are accumulated versus time in 100 channels of the
memory unit, and a 75 μsec ion dump period. Data are stored in two
separate 100 channel blocks of the memory unit corresponding to the
microwave power being on or off during the delay period. Usually
the microwave power is switched on or off every 5000 data cycles.
The time base for the system is derived from a 100-kHz crystal
oscillator.

The pressure, p, was measured by a nude Bayard-Alpert ionization
gauge calibrated against a Datametrics model 1023 capacitance
manometer. For most of the targets, p ranged from zero to \( \approx 3.0 \times 10^{-6} \)
Torr. The highest sensitivity of the capacitance manometer is \( 10^{-4} \)
Torr full scale, thus the ion gauge was calibrated at pressures \( \approx 10 \)
times those used in taking the de-excitation data; this procedure is
valid due to the highly linear response of the ion gauge and the fact
that one requires only the slope of the ion gauge response versus
absolute pressure. Put another way, to measure \( R \) one need only
determine \( \Delta(1/\tau)/\Delta n \) which in turn requires only measurement of
absolute pressure increments \( \Delta p \). Typical calibrations would consist
of setting \( p \) to ten different values ranging from \( 1.0 \) to \( 10.0 \times 10^{-5} \)
Torr as read by the ion gauge and noting the corresponding capacitance
manometer readings. The data was fit by the method of least squares
to the straight line form,
\[ p = M p_I + C, \]  

(4)

where \( p_I \) is the ion gauge reading and \( M \) and \( C \) were varied to make the fit. For each determination of \( R \), requiring about one day's data collection, there were made at least one and often two calibrations of the ion gauge. We found that generally the calibration constant \( M \) remained unchanged from day to day to within a few per cent and that the statistical error of the fitted \( M \) for a given set of calibration data was usually much less than 5%.

Figure 2 shows decay data for \( \text{He}^+(2S) \) at three different \( \text{He} \) gas pressures. This data was used to determine \( R_{\text{He}} \). The data are the difference between counts accumulated with microwave power on and off. Each point is the sum of three 40 \( \mu \text{sec} \) channels. About one hour data collection time was required to obtain each curve. The lines through the data are least squares computer fits to the function \( Ae^{-t/\tau} + B \), where \( A \), \( B \), and \( \tau \) are varied to make the fit. The constant background term \( B \) was always consistent with zero. Similar sets of curves were obtained for each of the target gases studied, although the pressure range for most was \( \approx 10 \) times less due to the drop off of the number of stored \( \text{He} \) ions with increasing \( p \) as mentioned previously.

Figures 3, 4, and 5 show \( 1/\tau \) vs \( p \) data representative of that used to determine \( R \) values for all of the targets studied. Several such curves were obtained for each target and the results were determined from an average of the slopes measured by computer fit to the data.
III. Results

Table 1 contains the results of our measurements. The errors are the larger of one standard deviation of the mean of each set of measurements for a given target or 10% of the mean. In addition to the values of \( R \) we have included the ratios \( R/\sigma_{\text{He}} \). This quantity is equal to the ratio \( \sigma/\sigma_{\text{He}} \) if the cross sections have the same dependence on relative velocity and the relative velocity distribution is the same for both targets. The latter is a good approximation since the mean energy of the stored \( \text{He}^+ \) ions is about one half the ion trap well depth, i.e. \( \approx 0.44 \) eV, whereas the mean energy of the targets is \( 300^\circ\text{K} \) thermal, \( \approx 0.025 \) eV. One can then regard the distribution of relative velocities to be essentially equal to the distribution of \( \text{He}^+ \) ion velocities which was the same for all the measurements. The greatest error would occur for the case of \( \text{H}_2 \) where the correction would increase the mean relative velocity by about 3%. One does not expect, however, that the cross sections have the same velocity dependences except among the group including the noble gases and \( \text{CCl}_4 \).

We have also included in Table 1 effective cross sections, \( \sigma_{\text{eff}} \), obtained from \( R \) by dividing by the velocity \( v = 4.6 \times 10^5 \) cm/sec equivalent to a \( \text{He} \) ion of \( 0.44 \) eV energy. These are intended only to indicate the range and size of the de-excitation cross-sections for \( \text{He}^+(2S) \) at this energy.

An essentially exponential decay of ground state \( \text{He}^+ \) ions versus storage time was noted during these measurements; its decay time
varied linearly with pressure $p$ and hence is consistent with the existence of some single collision loss mechanism. In the case of noble gas targets the rate constant for this process was always quite small; $\leq 5\%$ of $R$. We hypothesize that possibly due to the departure of the trap geometry from a perfect quadrupole shape, certain regions of phase space can lead to ion loss. Such a loss mechanism would be proportional to the ion-atom momentum transfer cross-section and could conceivably explain the effect.

In the case of molecular targets the loss rate of ground state He$^+$ ions was observed to be considerably larger. In particular $N_2$, $O_2$ and $CO_2$ were studied. We observed loss rate constants of 1.4(3), 1.1(3), and 1.5(4) in units of $10^{-9}$ cm$^3$ sec$^{-1}$ respectively for these targets. The rates for $N_2$ and $O_2$ are in agreement with reaction rates measured by Ferguson et al$^{13}$ and Sayers and Smith$^{14}$ for the processes,

$$\text{He}^+ + N_2 \rightarrow \text{He} + N^+ + N + .3 \text{ eV},$$

and

$$\text{He}^+ + O_2 \rightarrow \text{He} + O^+ + O + 5.9 \text{ eV}.$$ 

These authors studied the above reactions in He afterglows. Any reactions similar to the above and involving He$^+$(2S) ions would of course be included in the measured values of $R$. We assume that the small loss rate mechanism ($\leq 5\%$ of $R$) noted for ground state ions on noble gases if present for He$^+$(2S) collisions with these and other targets is no larger and the quoted values of $R$ contain no correction for it.
We point out that for a perfect trap geometry one might expect some ion loss due to elastic collisions which allow a "random walk" of the ion orbit across the magnetic field or leakage along the trap axis. The latter collisions would be most probable while the ion is at one extreme of its z trajectory. Both of these processes would require multiple collisions on the average to cause loss of an ion because of the cross sectional size of the orbit (≈ 5 cm) in comparison to the trap diameter, and the small energy transfer available (≈ .025 eV) per collision. A multiple collision loss process would imply a non-exponential decay curve if it were present to any significant degree as well as a non-linear relationship between any fitted 1/τ and p. Neither of these appear in our data to well within the limits indicated by the quoted errors.

In addition to measuring R values as described above, we did some experiments to determine whether or not the collision induced Lyman-alpha decay is a prominent decay mechanism for collisions with helium atoms. This was done by studying the variation of the normalized metastable decay rate, at a fixed time after creation of the ions, versus helium pressure.

The differential equation for decay of the He⁺(2S) population N may be rewritten as,

\[ \frac{dN}{dt} = S_r + S_{nr}, \]

where \( S_r \) and \( S_{nr} \) are rates for radiative and non-radiative processes respectively. For the case of impact on helium atoms one has,

\[ S_r = -N(A + \sigma_r v_n) \]

\[ S_{nr} = -N\sigma_{nr} v_n \]

where A is the free ion decay rate, \( n = n_{He} \), and \( \sigma_r \) and \( \sigma_{nr} \) are cross sections for radiative and non-radiative de-excitation. The normalized
rate of photon emission, $G = \frac{S_r}{N(t=0)}$, at time $t$ after creation of 2S ions at $t=0$ is given by,

$$G = (A + \sigma_r \nu_r) e^{-t(A + \sigma_r \nu_r + \sigma_{nr} \nu_n)}$$

The actual measured normalized rates $F$, would be given by,

$$F = K(A + \xi Dp) e^{-t(A + Dp)}$$

where,

$$D = \frac{(\sigma_r \nu_r + \sigma_{nr} \nu_n)/kT}{\xi}, \quad \text{and}$$

$$\xi = \eta \sigma_r \nu_r / (\sigma_{r} \nu_r + \sigma_{nr} \nu_n).$$

$K$ is a proportionality constant involving detector geometry and efficiency factors, $p = p_{He}$ and $\eta$ is the relative efficiency of the detectors for collision induced versus free decay photons. $\eta$ is most probably not unity since each free decay produces two photons with a continuous single photon spectrum whereas collision produced photons are produced one/decay and are at the Lyman-$\alpha$ wavelength 304Å. The quantity $\xi$, if $\eta=1.0$, is a measure of the fraction of de-excitation collisions which produce a photon. In the above the products $\sigma_r \nu_r$ and $\sigma_{nr} \nu_n$ may be replaced by velocity averaged products.

We have measured $F$ versus $p$ at $t=1$ msec in an attempt to learn something about the size of $\xi$. Figure 6 shows a plot of the data. The two curves are $F$ vs $p$ for $\xi = 0.0$ and $\xi = 1.0$ using the measured value of $D = R_{He}/kT$, $T = 300\, ^\circ K$, and adjusting $K$ by eye to give the best fit for $\xi = 1.0$. The data is consistent with $0.5 \leq \xi \leq 1.5$. It is reasonable to assume that $0 < \eta \leq 2$. Thus for collisions of He$^+(2S)$ on helium atoms we conclude that at least 25% of the de-excitation collisions produce photons.
IV. Discussion

In the following we discuss our results primarily in terms of the mechanism of induced Lyman-α decay. This is done because it is most probably the predominant de-excitation mode and to some extent one can apply the theory already developed for H(2S) de-excitation to the He⁺(2S) collisions studied here.

Spherical Targets

If one takes as the interaction potential between the He⁺(2S) ion and a target with polarizability α the form,

\[ U(r) = -\frac{e\alpha}{2r^4} \]  

with \( r \) the internuclear separation and \( e \) the electronic charge, then a simple dimensional argument shows that the induced Lyman-α decay rate should be given by

\[ R = C(\alpha \mu)^{1/2} \]  

where \( C \) is a constant of proportionality and \( \mu \) is the matrix element \( \langle <2P|z_e|2S> \rangle \), \( z_e \) being the \( z \) coordinate of the He⁺ electron. (The "natural" \( z \)-axis is along the inter-nuclear axis.) We have calculated \( R \) using the potential above and straight line trajectories using the sudden approximation. The sudden approximation is applicable because of the short duration of the collision, \( \approx 10^{-13} \) sec, in comparison to the \( 2S - 2P_{1/2}, 2P_{3/2} \) fine structure periods, \( \approx 10^{-10}, \approx 10^{-11} \) sec. The small impact parameter cut off is the usual one, i.e. that value \( B_0 \) such that \( P(B_0) \) (the probability of the ion being in one of the 2P states after collision) is equal to one. The cross section is then

\[ \sigma = \pi B_0^2 + 2\pi \int_{B_0}^{\infty} b P(b) db \]  

The result of the calculation is

\[ R = 6.84(e^2\alpha \mu \nu/h)^{1/2} \]
For He\(^+\), \(\mu = 1.5 a_0\), where \(a_0\) is the Bohr radius.

Figure 7 shows a plot of the measured values of \(R\) versus \(a^{1/2}\) for the targets He, Ar, Kr, Xe, and CCl\(_4\). (CCl\(_4\) is essentially spherical; its lowest order multipole moment is the octupole.) Values of \(a\) were taken from Rothe and Bernstein.\(^{17}\) One sees that the values fall well along a straight line, however they are about 50\% below the sudden approximation calculation. (We used \(v = 4.6 \times 10^5\) cm/sec in the calculation.) In view of the extreme over simplification of the calculation we regard the discrepancy as insignificant. We point out that any He\(^+\)(2S) loss mechanism proportional to the momentum transfer cross section would also be proportional to \(a^{1/2}\). In the figure we include values of \(\sigma_d v\) where \(\sigma_d\) is the momentum transfer cross section calculated from the formula of Eliason and Hirschfelder;\(^{18}\)

\[
\sigma_d = 0.553 (4\pi e/v) \cdot (a/M)^{1/2}
\]

where \(M\) is the reduced mass of the collision pair. The line through the experimental points is a least squares fit of \(R = k a^{1/2}\) which gave \(k = 4.14 \times 10^3\) cm\(^3\)/sec\(^{-1}\).

Kocher, Clendenin, and Novick\(^{19}\) in their time-of-flight work on the free life-time of He\(^+\)(2S) report a value of 
\(\sigma = 10\pi a_0^2 = 8.8 \times 10^{16}\) cm\(^2\) for the total de-excitation cross section of 15 eV ions on helium. This corresponds to a rate of \(\approx 2.4 \times 10^{-9}\) cm\(^3\)sec\(^{-1}\). A \(v^{1/2}\) scaling of our result would predict \(R = 4.0 \times 10^{-9}\) cm\(^3\)sec\(^{-1}\) at 15 eV.
Lipworth and Novick in reporting their measurement of the He$^+$ 2S - 2P$_{1/2}$ fine structure (Lamb shift) give the results of calculations of the cross sections, $\sigma_r$, for induced Lyman-$\alpha$ decay and, $\sigma_i$, for Penning ionization of He by He$^+(2S)$ ions with a mean velocity of $1.05 \times 10^5$ cm/sec. Their values are $\sigma_r = 34.4 \pi \alpha_o^2 = 3.03 \times 10^{-15}$ cm$^2$ and $\sigma_i = 15.9 \pi \alpha_o^2 = 1.40 \times 10^{-15}$ cm$^2$, yielding a total cross section of $4.43 \times 10^{-15} = 44.3$ Å$^2$. This is quite close to the value of $\sigma_{\text{eff}}$ listed in Table I for He although our estimated relative velocity is more than 4 times the value used by Lipworth and Novick in their calculation.

**Linear Symmetric Molecules**

In the case of impact on molecules one expects both the polarization and the molecular multipole fields to contribute to the Lyman-$\alpha$ de-excitation rate. For the linear symmetric molecules H$_2$, N$_2$, O$_2$, and CO$_2$ the lowest order non-vanishing multipole moment is the quadrupole. Thus one would expect that the transient electric field mixing the 2S and 2P states would be the sum of that due to the polarization of the target and its quadrupole field as a first approximation. The polarization field will in general be the sum of two dipole fields arising from induced moments $e \alpha || \cos \theta/r^2$ and $e \alpha \perp \sin \theta/r^2$ where $\theta$ is the angle between the molecular axis and the line between the collision partners; $\alpha ||$ and $\alpha \perp$ are the polarizabilities for fields oriented parallel and perpendicular to the molecular axis. A calculation, then, requires the net electric field averaged over all molecular orientations. We do not carry out such a program here but have calculated the polarization and quadrupole field de-excitation rates as if they were acting separately. Because the two fields are not everywhere parallel,
the net effect is not simply the sum of the two, but should lie between the sum and the absolute value of the difference. The polarization field de-excitation rate, $R_p$, was calculated using the constant determined from the measurements on the spherical targets together with the mean polarizabilities $\bar{\alpha} = (2\alpha_\perp + \alpha_\parallel) / 3$. The quadrupole field de-excitation rate was calculated using the relation $R_q = \sigma_q v$ ($v = 4.6 \times 10^5$ cm/sec), and

$$\sigma_q = 4.206(\epsilon_0 q/h\nu)^{2/3}$$

from the work of Slocomb, Miller, and Schaeffer (SMS); $q$ is the molecular quadrupole moment. The values used for $q$ are those recommended by Stogryn and Stogryn. Table 2 contains the results of these calculations. The conclusions one can draw from these results are limited. However, one sees that the sizes of the two effects are comparable; it is probably accidental that the polarization rate is in agreement with the experimental rates for H$_2$ and N$_2$ and nearly so for O$_2$. The case of CO$_2$ more clearly requires the existence of both mechanisms.

Kocher, Clendenin, and Novick$^{19}$ have also reported a value of $\sigma = 50\alpha_0^2 = 4.40 \times 10^{-15}$ cm$^2$ for the total de-excitation cross section for 15 eV He$^+$ (2S) on N$_2$. This corresponds to a rate of $11.8 \times 10^{-9}$ cm$^3$ sec$^{-1}$.

Water and Ammonia

The theoretical treatment of these collisions would follow the discussion in the previous section with the addition of the electric dipole fields arising from the large dipole moments of these molecules.
(1.84 and $1.47 \times 10^{-18}$ esu cm for water and ammonia$^{21}$). Using mean polarizabilities$^{17}$ of 1.45 and $2.16 \times 10^{-24}$ cm$^{-3}$ for water and ammonia one obtains $5.0$ and $6.1 \times 10^{-9}$ cm$^3$ sec$^{-1}$ for the de-excitation rates due to the polarization field alone.

The electric dipole fields alone would yield, for water, $39.6 \times 10^{-9}$ and for ammonia, $31.5 \times 10^{-9}$ cm$^3$ sec$^{-1}$ using the method of SMS; the results of Gersten's method are larger by a factor of $3^{1/2}$.

An effective quadrupole moment of $1.0 \times 10^{-26}$ esu cm$^2$ (appropriate for both molecules) would yield a rate of $3.5 \times 10^{-9}$ cm$^3$ sec$^{-1}$ using the method of SMS and a factor of $3^{1/3}$ larger from the work of Gersten.

Calculations of the octupole components of the water molecule yield values $\approx 10^{-34}$ esu cm$^3$ which would imply a rate, if acting alone of $0.60 \times 10^{-9}$ cm$^3$ sec$^{-1}$. In all of the above a relative velocity of $4.6 \times 10^5$ cm/sec has been assumed.

The experimental values of the total de-excitation rate (Table I) for water and ammonia are considerably less (about 50%) than the rates calculated for the permanent dipole fields and listed above. This may reflect partial cancellation of the dipole field by the induced dipole and higher order multipole fields. In any case the measured values await a complete calculation of the Lyman-$\alpha$ de-excitation rates for impact of He$^+$ (2S) on these molecules before a more meaningful comparison can be made.
References

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TABLE I. Results of He\(^+\)(2S) de-excitation rate measurements.

<table>
<thead>
<tr>
<th>Target</th>
<th>R (10^{-9}\text{cm}^3\text{sec}^{-1})</th>
<th>R/R(_{\text{HE}})</th>
<th>(\sigma_{\text{eff}}^a) (Å(^2))</th>
</tr>
</thead>
<tbody>
<tr>
<td>He</td>
<td>1.65(17)</td>
<td>1.00</td>
<td>37.</td>
</tr>
<tr>
<td>Ar</td>
<td>4.99(65)</td>
<td>3.02(50)</td>
<td>112.</td>
</tr>
<tr>
<td>Kr</td>
<td>6.3(10)</td>
<td>3.82(72)</td>
<td>143.</td>
</tr>
<tr>
<td>Xe</td>
<td>8.7(14)</td>
<td>5.24(55)</td>
<td>196</td>
</tr>
<tr>
<td>CCl(_4)</td>
<td>13.3(13)</td>
<td>8.1(12)</td>
<td>302.</td>
</tr>
<tr>
<td>H(_2)</td>
<td>3.68(37)</td>
<td>2.23(32)</td>
<td>83.</td>
</tr>
<tr>
<td>N(_2)</td>
<td>5.51(55)</td>
<td>3.34(48)</td>
<td>125.</td>
</tr>
<tr>
<td>O(_2)</td>
<td>6.07(61)</td>
<td>3.68(53)</td>
<td>137.</td>
</tr>
<tr>
<td>CO(_2)</td>
<td>11.3(16)</td>
<td>6.9(12)</td>
<td>258.</td>
</tr>
<tr>
<td>H(_2)O</td>
<td>18.5(19)</td>
<td>11.2(16)</td>
<td>420.</td>
</tr>
<tr>
<td>NH(_3)</td>
<td>20.9(21)</td>
<td>12.6(18)</td>
<td>473.</td>
</tr>
</tbody>
</table>

\(a\sigma_{\text{eff}} = R/v, v = 4.6\times10^5\text{cm/sec}\)
TABLE II. Comparison of experimental de-excitation rates, \( R \), with polarization, \( R_p \), and quadrupole, \( R_q \), rates. \( \bar{\alpha} \) and \( q \) are the mean polarizability and quadrupole moment used in calculating \( R_p \) and \( R_q \).

<table>
<thead>
<tr>
<th>Target</th>
<th>( \bar{\alpha}^{a} ) (( \text{A}^{3} ))</th>
<th>( (10^{-26} \text{esu cm}^{2}) )</th>
<th>( (10^{-9} \text{cm}^{3} \text{sec}^{-1}) )</th>
<th>( R^{c} )</th>
<th>( R_p )</th>
<th>( R_q^{d} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \text{H}_2 )</td>
<td>0.806</td>
<td>0.651</td>
<td>3.68(37)</td>
<td>3.72</td>
<td>2.65</td>
<td></td>
</tr>
<tr>
<td>( \text{N}_2 )</td>
<td>1.74</td>
<td>-1.52</td>
<td>5.51(55)</td>
<td>5.46</td>
<td>4.66</td>
<td></td>
</tr>
<tr>
<td>( \text{O}_2 )</td>
<td>1.57</td>
<td>-0.39</td>
<td>6.07(61)</td>
<td>5.19</td>
<td>1.88</td>
<td></td>
</tr>
<tr>
<td>( \text{CO}_2 )</td>
<td>2.59</td>
<td>-4.3</td>
<td>11.3(16)</td>
<td>6.67</td>
<td>9.32</td>
<td></td>
</tr>
</tbody>
</table>

\(^{a}\text{Ref. 17} \quad ^{b}\text{Ref. 21} \quad ^{c}\text{See Table I.} \quad ^{d}\text{Using method of SMS(Ref.8)} \)
Figure Captions

Fig. 1. Sketch of the ion trap and photon detectors. The magnetic field is along the trap axis. The half cylinders 2a and 2b are maintained negative with respect to electrodes 1 and 3 during the storage period. The hot filament F is pulsed negative to accelerate electrons into the trap for creation of the He ions. The zig-zag pattern is a web of thin copper wires to give high transparency for the decay photons, while maintaining the cylindrical electrode geometry. The rectangular shape in the center of the figure represents the end of the microwave horn located outside the cylinder. Power radiated from this horn drives the 2S-2P_{1/2} transition.

Fig. 2. Representative He\(^+\)(2S) decay curves for three different pressures of He. The lines are computer fits. The curves have been adjusted slightly vertically so that the lines meet at t=0. The ordinate is correctly scaled for the data at 7.0 \times 10^{-6} \text{Torr}.

Fig. 3. \(1/\tau\) vs pressure plots for He\(^+\)(2S) collisions with H\(_2\) and He. The lines are least squares computer fits.

Fig. 4. \(1/\tau\) vs pressure plots for He\(^+\)(2S) collisions with He, Ar, Kr, Xe, and CCl\(_4\). The curves have been separated vertically for clarity since the slopes are the quantities of interest. The lines are least squares computer fits. The line for He is that shown in Fig. 3.
Fig. 5. $\frac{1}{\tau}$ vs pressure plots for He$^+(2S)$ collisions with H$_2$, N$_2$, O$_2$, CO$_2$, H$_2$O, and NH$_3$. The curves have been separated vertically for clarity since the slopes are the quantities of interest. The lines are least squares computer fits. The line and points for H$_2$ are the low pressure end of the plot shown in Fig. 3.

Fig. 6. Plot of the normalized count rate for He$^+(2S)$ in collision with He at $t = 1$ msec after creation of the ions versus He pressure. The upper and lower curves are plots of the function $F$ for $\xi = 1.0$ and $0.0$, respectively. The data indicates that at least 25% of the collisions produce countable photons.

Fig. 7. Plot of experimental values of the He$^+(2S)$ total de-excitation rate versus the square root of the polarizability of the targets He, Ar, Kr, Xe, and CCl$_4$. The dashed line is the result of a sudden approximation calculation. The triangles are momentum transfer rates for $v = 4.6 \times 10^5$ cm/sec. The solid line is a least squares straight line fit to the data.
Fig. 1
Fig. 2
Fig. 3
Fig. 4
Fig. 5
Fig. 6
Fig. 7
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