Iterative Self-Dual Reconstruction on Radar Image Recovery

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Abstract

Imaging systems as ultrasound, sonar, laser and synthetic aperture radar (SAR) are subjected to speckle noise during image acquisition. Before analyzing these images, it is often necessary to remove the speckle noise using filters. We combine properties of two mathematical morphology filters with speckle statistics to propose a signal-dependent noise filter to multiplicative noise. We describe a multiscale scheme that preserves sharp edges while it smooths homogeneous areas, by combining local statistics with two mathematical morphology filters: the alternating sequential and the self-dual reconstruction algorithms. The experimental results show that the proposed approach is less sensitive to varying window sizes when applied to simulated and real SAR images in comparison with standard filters.

1. Introduction

Synthetic Aperture Radar (SAR) images allow to monitor natural scenes on the Earth surface due to the proper characteristics of its imagery system, enabling image capturing regardless of solar illumination or weather conditions. Its spectral operation range allows to detect high transmission of the electromagnetic waves in the atmosphere, even in adverse atmospheric conditions (e.g. during precipitations or cloudy sky).

Image analysis of SAR relies on digital image processing techniques as speckle modeling and filtering. Several adaptive speckle removal algorithms address the image in terms of small windows over regions assumed to be uniform (constant gray levels) or textured (abrupt intensity changes). Theoretically, we could control smoothness by modeling the image for particular window sizes, but the estimation of such model parameters in the presence of speckle noise is signal-dependent and non-Gaussian [1].

The methods proposed by Lee [6], Frost et al. [3], Kuan et al. [5] are considered standard algorithms in speckle filtering, therefore they are often reported in performance comparisons as in [2, 9]. The popularity of these filters among remote sensing users resulted in adaptations of the filters to be applied to ultrasound B-scan images, for diagnosis quality improvement. Lee and Kuan filters are widely used to suppress speckle and they present similar performance when evaluated using speckle-noise local statistics as mean and standard deviation in fixed sliding window. These filters can preserve steep edges if the window size is properly chosen. Window size values as high as 11x11 compromise fine details in the image and window size values as low as 3x3 implies in insufficient speckle noise suppression on homogeneous areas. This is a drawback reported in many papers [3, 5, 9, 10, 17], a trade-off between preserving edges and reducing the strength of the noise. Lopes et al. [10] minimized the drawbacks of Frost and Lee filters by exploiting local SAR image statistics and specifying different levels of homogeneity. In addition to [4, 10, 9], we propose a multiscale scheme that maintains fine details for larger windows by using morphological filters combined to Lee filter [7].

Our scheme uses a sliding window, which incorporates local statistics, adapting the Lee filter to include a combination of self-dual reconstruction and the alternating sequential filters. The self-dual filter uses the median filter to obtain marker images for the filtering process. The major contribution of our algorithm is to be fairly insensitive to the choice of the window size in comparison with the Lee filter. In addition, we can easily modify the proposed scheme to include other standard speckle filters (e.g. Frost and Kuan)
to generate marker images. We compare the proposed algorithm with the standard Lee filter quantitatively by using the beta-coefficient and the equivalent number of looks measures, showing that our algorithm outperforms the standard Lee filter.

Section 2 reports previous work in speckle noise modeling and filtering. Section 3 describes the proposed iterative self-dual reconstruction method and evaluates its performance in comparison with the standard formulation in [7]. In Section 4, we present experimental results by using simulated and real SAR images to summarize the advantages and contributions of the novel scheme in Section 5.

2. Speckle Model and Filtering

Two approaches can be adopted to reduce the speckle noise in SAR image: multilook processing and filtering techniques. The former improves the SAR image quality by averaging uncorrelated images from nonoverlapping spectra, consequently producing spatial resolution losses. We adopt the latter approach, which suppresses the speckle noise after the one-look image has been formed. Speckle noise can be described in terms of a multiplicative model [7, 8], given by $z = x. n$, where $z$ describes the amplitude of the noisy observed pixel at the position in linear detection, $x$ is the original signal and $n$ is the noise with unitary mean. The random variables $x$ and $n$ are assumed to be independent.

In the absence of a precise model for the original signal $x$, the noisy version of the signal is used to estimate the a priori mean $\bar{x}$ and variance $\sigma_z^2$ of the original signal from the local mean $\bar{z}$, and local variance $\sigma_z^2$ in a 5x5 window [8]. In other words, the local mean is $\bar{z} = \bar{x} \cdot \bar{n}$ and the estimated variance is $\hat{\sigma}_z^2 = \frac{\sigma_z^2 - \bar{x}^2 \cdot \bar{n}^2}{1 + \sigma_n^2}$. The $\hat{\sigma}_z^2$ is the estimated variance of the original image and $\bar{n}$ is the unitary mean of the speckle noise. The speckle noise variance, $\sigma_n^2$, is an important parameter considered in designing speckle filters [7, 10]. It measures the speckle strength, and it can be determined over featureless areas [8] by $\sigma_n^2 = \frac{\sigma_z^2}{2}$. Lee [6] developed a widely used local linear minimum square error filter which is derived from the speckle model. This filter assumes that speckle is a random variable following a multiplicative noise with unitary mean, where $\bar{x}$ is the minimum mean square estimate of $x$. The noisy pixel is updated by the expression $\tilde{x} = \bar{x} + k (z - \bar{z})$, where $\bar{x}$ is the local mean estimated on the sliding window, $z$ is the observed pixel and $k$ is the kernel of the filter ranging between 0 and 1, given by $k = \frac{\sigma_n^2}{\sigma_z^2 + \sigma_n^2}$.

To perform speckle noise filtering, local statistics are computed over a fixed neighborhood (e.g. 5x5 window). Usually, the larger the window size, the lesser the performance of the speckle filters concerning edge and fine details preservation.

The proposed filter scheme considers mathematical morphology techniques, which here unfolds in three main principles: alternating sequential filter (ASF), self-dual reconstruction and the Lee filter. This approach leads to the iterative Reconstruction from Lee filter (IRLee), capable of overcoming imprecisions when edges and fine detail preservation are necessary.

2.1. Alternating Sequential Filter

ASF is a sequence of alternate opening ($\gamma$) and closing ($\phi$) operations for windows of increasing size. These filters transform dark and bright regions differently depending on the initial operation: an opening or a closing to start the filtering process. An ASF of order $i$ is a composition following one of the 4 different forms: $M_i = m_1 m_{i-1} \ldots m_2 m_1$, $R_i = r_i r_{i-1} \ldots r_2 r_1$, $N_i = n_1 n_{i-1} \ldots n_2 n_1$, $S_i = s_1 s_{i-1} \ldots s_2 s_1$, with $m_i, n_i, r_i, s_i$ defined in terms of opening and closing operators as $m_i = \gamma_i \phi_i, \ r_i = \phi_i' \gamma_i, \ n_i = \phi_i \gamma_i, \ s_i = \gamma_i \phi_i'$. The parameter $i$ represents the size of the window for morphological filtering.

An ASF cannot be self-dual due to the inherent asymmetry in its definition $N_i \neq M_i$ [13]. This technique is widely used for filtering radar images [14], but their final result depends on the initial operator to start the sequence of transformations with no guarantee of preservation of thin structures in the presence of strong noise level. A self-dual filter [16] could be applied to overcome initial condition dependence. This motivated the use of self-dual reconstruction to avoid such an initial operator dependency and to preserve thin details. The self-dual morphological reconstruction is reviewed in the next section.

2.2. Self-dual Reconstruction

Morphological reconstruction by dilation (or erosion) is an operator that removes dark (or bright) regions from a marker image constrained by a mask image. Particularly, self-dual reconstruction combines reconstruction by using dilation and erosion to achieve the same treatment to dark and bright regions of the image. The self-dual reconstruction $R_g^d(f)$ of a marker image $f$ constrained by a mask image $g$ is defined by:

$$[R_g^d(f)](x) = \begin{cases} [R_g^d(f \land g)](x), & \text{if } f(x) \leq g(x). \\ [R_g^d(f \lor g)](x), & \text{otherwise} \end{cases} \quad (1)$$

where $R^d$ and $R^c$ correspond to the morphological reconstruction by dilation and erosion, respectively.

Self-dual or self-complementary morphological filters have proven to be useful in speckle noise reduction as in [16], especially on radar data, where there is no clear distinction between background and foreground in the images and motivated several other works in noise filtering. Self-dual operators are based upon the assumption that the tar-
geted image structures are image extrema [15], not considering statistical properties, assumption that neglects the multiplicative model of the speckle noise.

A common approach to remove speckle noise is the use of the original noisy image as a mask, while a marker image is obtained by processing the original one with a median filter, which does not incorporate any speckle statistics [15]. The median filter removes noise and, subsequently, the reconstruction attempts to restore degraded fine details but it fails at those entirely removed by the filter.

We noticed that thin structures could be preserved in the filtering process when combining multiscale parameters to the reconstruction process. We design a novel scheme that a set of Lee filters of increasing window size, as a sequential filter, with self-dual reconstruction to obtain speckle removal and preservation of thin details of the image. The closing and opening operations in the ASF are substituted by the Lee filter to smooth the image, while the speckle statistics component guarantees the preservation of image details during the reconstruction process as it follows.

3. Methodology

Our method adapts the Lee filter with morphological reconstruction by performing adequate noise removal with image statistics, and maintaining fine image details. We propose that the window size increases in each iteration according to the relation: \( W_n = W_1 + 2 \times (n - 1) \), for \( W_1 \) corresponding to the minimum window size (3x3) and \( n \) \( (n \geq 1) \) corresponds to the number of the current iteration. Thus, the second iteration generates a Lee filtered marker image with a 5x5 window \( (W_2) \), the third with a 7x7 window \( (W_3) \), the fourth with a 9x9 window \( (W_4) \) and so on.

The implemented algorithm denoted Iterative Reconstruction from Lee (IRLee) filter of order \( n \) is described as follows:

\[
IRLee_n(f) = \begin{cases} 
R_{L_n(f)}(f), & \text{for } n = 1 \\
R_{L_{n-1}(IRLee_{n-1}(f))}(f), & \text{for } n > 1
\end{cases}
\]

where \( L_n(f) \) denotes the Lee filter applied to an image \( f \) using a window of size \( W_n \).

The IRLee filtering starts by considering the IRLee0 image to be the original one (speckled image), then the Lee filter is applied to the IRLee\( n-1 \) image, generating a marker image \( L_n \) and the final IRLee\( n \) image is obtained by the reconstruction process using the original image as a mask. Here, instead of estimating the standard deviation of the speckle noise \( \sigma_n \) in each IRLee image we keep it constant for every iteration. We assume that some pixel values in each iteration are still affected by the multiplicative noise and therefore we can use the same \( \sigma_n \) parameter for the Lee filter with a larger window. This assumption is motivated by the self-dual reconstruction filter effect obtained when it is applied to the previous Lee filtered image. The self-dual reconstruction filter modifies several pixel values turning them into values closer to their correspondents in the mask image.

The Lee’s filter does not preserve fine details when considering large windows, resulting in increased blurring effect over the marker images. The self-dual reconstruction minimizes this drawback by considering an iterative process that preserves fine details, in spite of the blurring effect created in the Lee filtered marker images. Next sections use IRLee to refer to the filter whose marker images are generated by using Lee filter, and IRLMedian when the marker images are generated by using the median filter.

3.1. Speckle Filtering Validation

We compared the proposed approach with other filters by considering measures related to edge preservation and speckle strength reduction. We demonstrate the efficacy of the IRLee filter by calculating the standard deviation to the mean ratio \((\beta_w)\), followed by the verification of the speckle noise strength in the filtered images, given by [8] \( \beta_w = \frac{\sigma_w}{\mu_w} \).

The sample mean \((\mu_w)\) and standard deviation \((\sigma_w)\) can be estimated over a window \( w \) comprising \( N \) pixels in a homogeneous area of the filtered SAR image.

The equivalent number of looks \((ENL)\) after filtering provides a quantitative evaluation of the degree of speckle smoothing [9], supposing that an ideal filter would give an infinite \( ENL \) for a plain homogeneous area. This measure over homogeneous areas also accounts for the speckle noise strength and is defined for amplitude SAR images in [8] as \( ENL = \left( \frac{0.5227}{\sigma_w} \right)^2 \), where 0.5227 is the value of the \( \sigma_n \) for an amplitude one-look SAR image.

The beta coefficient or speckle index represented by \( \beta_w \) and \( ENL \) are useful measures to evaluate speckle noise filters. In addition, we also evaluate edge preservation by using the A coefficient, namely [12]

\[
A = \frac{\Gamma(\Delta S - \Delta \bar{S}, \bar{S} - \bar{\Delta S})}{\sqrt{\Gamma(\Delta S - \Delta \bar{S}, \Delta \bar{S} - \Delta S), \Gamma(\Delta S - \Delta \bar{S}, \bar{S} - \bar{\Delta S})}}
\]

where \( \Delta S \) and \( \bar{\Delta S} \) are the high-pass filtered versions of an original image \((S)\) and the denoised one \((\bar{S})\), respectively, obtained with a 3x3 pixel standard approximation of the Laplacian operator and the function \( \Gamma(S_1, S_2) = \sum_{i=1}^{K} S_{i1} \cdot S_{i2} \).

4. Experimental Results

This section describes the image processing results by running the proposed morphological speckle filter using artificial and real SAR images. We evaluated the results using...
Lee filter as in [7, 8] and its major modification, the proposed algorithm IRLee by measuring the $\beta_w$ and ENL to evaluate the speckle noise reduction and the A coefficient measure edge preservation. Due to lack of real segmentation of the SAR images, we calculated the A coefficient only for a synthetic image. The correlation measure, $A$, should be close to unity for an optimal edge preservation effect whereas low values of $\beta_w$ (close to zero) in homogeneous areas imply low speckle fluctuations.

Figure 1b displays the $A$ values calculated for the processed images using the Lee and IRLee filters over the filtered versions of the noisy image in Figure 1a. In Figure 1b, the curve of $A$ values for the Lee filter shows that the edges are not preserved ($A$ tends to values close to zero) as the window’s size increases. This is an evidence that the use of the Lee filter with an analyzing window with dimensions greater than $5 \times 5$ does not guarantee edge preservation. This effect is not observed for the IRLee filter in the same graphic, where the $A$ values asymptotically approximate $A=0.22$ as the number of iterations of the proposed algorithm increases. It implies that the blurring effect over the homogeneous areas increases but the edge smearing is stable. This effect appears in Figure 2 to demonstrate the good performance of the proposed technique over the standard method, according to edges preservation while reducing speckle noise.

Figure 3a presents an amplitude (square root of the intensity) SAR image over Thetford, England, which was obtained by the Canadian airborne C-SAR in slant-range projection. It is a nominal 7-looks image, and the estimated number of looks (ENL), used in the forthcoming tests, was of 6.7, VV polarization and spatial resolution of 6m.

In Figure 3b, we present the $\beta_w$ values calculated for the processed images using the Lee and IRLee filters over the image in Figure 3a. The filtering process ended up with an analyzing window comprising $21 \times 21$ pixels, or ten iterations. The $\beta_w$ values were calculated in a $15 \times 15$ window ($W$) over a homogeneous area of the original image and its corresponding filtered versions. Figure 4 displays the results of the proposed algorithm when using the median and Lee filters to obtain marker images for the IRLee filtering process. We can visually observe from these results that our approach outperformed the one which uses the standard median filter. The same results can be observed when applying these two methods to the image in Figure 5a, where the blurring effect on the processed images can be observed in Figure 6.
The $\beta_w$ values, observed in Figures 3b, 5b, decrease exponentially as the window size, or the number of iterations, increases in the two methods. However, the $\beta_w$ values (solid lines) obtained from the Lee filter denote that homogeneous areas tend to be created more quickly when using only this standard filter. These values are lower than the ones obtained on the $IR\text{Lee}$ filtered images (dashed lines). Thus, using a larger window size (e.g. $9 \times 9$) in the Lee filter features such as edges and fine details will be vanished insofar as the speckle noise will be suppressed. This effect can be observed in Figures 4 and 6, which illustrate the increasing blurring effect on the images filtered with the standard Lee filter. Differently, the Iterative Reconstruction from Lee filter ($IR\text{Lee}$) suppresses speckle noise while effectively preserves image features (edges) with increasing filtering window size.

Comparative experiments obtained for the $IR\text{Lee}$ filter also included the real SAR image displayed in Figure 7a. It was acquired by the JERS-1 satellite over the Tapajos National Forest, Para, Brazil, with spatial resolution of 18m, nominal look angle of 35 degrees and 3-looks (nominal).

![Figure 7](image1.png)

Figure 7. (a) JERS image taken over the Tapajos National Forest, in Brazil; (b) $\beta_w$ values calculated to $IR\text{Lee}$ filtered images by using the Lee filter parameter $\sigma$, estimated in each iteration and by using $\sigma$, constant in all iterations. Figure 7b illustrates the behavior of the $IR\text{Lee}$ filter when estimating the equivalent number of looks in the iterated filtered SAR images (Figure 3a and Figure 7a) and when using the same $ENL$ in all iterations. These results motivated us to adopt $\sigma$ constant over all iterations for comparison purposes. In [11] Oliver and Quegan reported that difficulty in estimating the equivalent number of looks in iterated filtered images where $ENL$ is expected to increase as iterations proceed. According to the authors the estimation becomes difficult as it varies across the image.

Figure 8a displays a 4-looks RADARSAT-1 image acquired in the ScanSAR wide mode, swath width of 150 km and polarization HH, radar incidence angle of 27° and with 12.5 m spatial resolution, corresponding to a region of the North coast of Rio Grande do Norte (RN), Brazil. In this image the white square encompasses bright points over the upper target on the right side which consist of oil platforms in the ocean. Figure 8b corresponds to a detail image which contains small targets as oil platforms in the ocean, to be preserved in the final result due to their importance in the image interpretation. Figures 8c and 8d present the results using the median and Lee filter, respectively, to obtain the marker images for the iterative process. Figure 9 quantifies the ability of our method to preserve and enhance details while reducing the noise. Figure 9 depicts an image profile from the target on the right of images presented in Figures 8c and 8d. These patterns show that the blurring effect applied to the original image (solid line) using the median filter to generate the markers (IRMedian - dashed line) attenuates the pattern more than the Lee filter in the method. According to these results, targets are better preserved using our method ($IR\text{Lee}$ in dash-dotted line), as Figure 8d displays. The top-left targets almost disappeared from Figure 8c, demonstrating that targets vanish when the marker image does not take into account the statistical model of the speckle noise.

![Figure 8](image2.png)

Figure 8. (a) Original 4-looks RADARSAT-1 image; (b) Oil platforms in the area inside the white square; (c) Filtered area inside the white square using the median filter to obtain the marker image for our method; (d) Filtered area inside the white square using the Lee filter to obtain the marker image for our method.

5. Concluding Remarks

We introduced the Iterative Reconstruction from Lee filter ($IR\text{Lee}$), a morphological iterative filter for SAR images, which takes into account the multiplicative model and speckle statistics. The proposed algorithm incorporates the multiplicative speckle model to the marker images, providing a more adequate morphological filter than the standard self-dual filter with respect to edge enhancement and preser-

![Figure 9](image3.png)

Figure 9. Image profile from the target illustrate on the right of Figures 8c and 8d.
An ideal speckle filter should reduce noise while preserving edges and fine details. The standard Lee’s filter can reduce speckle effects but it also smears edges. The IRLee algorithm is an effective filter in reducing speckle noise from uniform areas and in enhancing and preserving edges, enabling larger windows to be used, with consequent lower impact on edges. Note that although we have adopted the Lee filter to generate marker images, other speckle filters might be feasible. The comparative results between the Lee filter, the standard self-dual filter and the proposed scheme pointed out the importance of incorporating speckle statistics of SAR images to improve filtering in multiscale scenarios. We are currently investigating other filters to generate marker images at lower time computing.

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