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Soluto-inertial phenomena: Designing long-range, long-lasting, surface-specific interactions in suspensions

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Equilibrium interactions between particles in aqueous suspensions are limited to distances less than 1 μm. Here, we describe a versatile concept to design and engineer nonequilibrium interactions whose magnitude and direction depends on the surface chemistry of the suspended particles, and whose range may extend over hundreds of microns and last thousands of seconds. The mechanism described here relies on diffusiophoresis, in which suspended particles migrate in response to gradients in solution. Three ingredients are involved: a soluto-inertial “beacon” designed to emit a steady flux of solute over long time scales; suspended particles that migrate in response to the solute flux; and the solute itself, which mediates the interaction. We demonstrate soluto-inertial interactions that extend for nearly half a millimeter and last for tens of minutes, and which are attractive or repulsive, depending on the surface chemistry of the suspended particles. Experiments agree quantitatively with scaling arguments and numerical computations, confirming the basic phenomenon, revealing design strategies, and suggesting a broad set of new possibilities for the manipulation and control of suspended particles.

Significance

Liquid suspensions of micron-scale particles and drops play a ubiquitous role in a broad spectrum of materials of central importance to modern life. A suite of interactions has long been known and exploited to formulate such suspensions; however, all such interactions act over less than a micron in water—and often much less. Here we present a concept to design and engineer nonequilibrium interactions in suspensions, which are particle surface-dependent, may last for hundreds of seconds, and extend hundreds of times farther than is currently possible. The conceptual versatility of the results presented here suggests new capabilities for manipulating suspensions, sorting particles, and synthesizing novel materials and particles.

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liquids, or generally in the vicinity of equilibrating surfaces. Recent years have seen a burst of interest in DP in areas ranging from membrane fouling (41), to transport into dead-end pores (42, 43), to self-propelling particles (44–47), to active matter (48–50).

Soluto-Inertial Beacon

Fig. 1 illustrates the mechanism we propose for this interaction, which requires three key ingredients. First, a particle or structure must act as a beacon that generates a long-lasting solute flux. Second are the suspended objects (e.g., colloidal particles, polymers, or emulsion drops), which may be attracted or repelled from the beacon. Third is the solute whose flux mediates the interaction by driving suspended objects into diffusiophoretic migration. Careful choice of these three ingredients (beacon, solute, and suspended particle) enables the duration, direction, and range of the beacon–suspension interactions to be designed and engineered.

Whether the beacon attracts or repels colloids in suspension depends on how those colloids migrate under the chosen solute flux. Theories for diffusiophoretic mobilities involve the relative excess (or depletion) of the solute near the particle surface, which is forced into motion by solute gradients in the bulk solution. Such theories have been developed for gradients of electrolytes (35, 37) and nonelectrolytes (51), yet difficulties in establishing sufficiently strong, stable gradients have prevented systematic experimental measurements (as is routine for electrophoresis). Recent developments in microfluidics, however, have enabled more direct studies of DP (40, 52–56). In particular, we have recently developed a microfluidic device (56) that enables gradients to be directly imposed, and diffusiophoretic migration to be visualized and measured under various solute and solvent gradients (40).

Fig. 2 highlights the surface specificity of DP under a given solute flux. High- and low-concentration SDS solutions flow through the outer “reservoir” channels of a three-channel device, to establish and maintain an SDS gradient of controllable strength across the central sample channel. Even the direction of migration depends on the specific solute/colloid pair. Fluorescent, sulfonated polystyrene (PS) colloids (Materials and Methods) move diffusiophoretically down SDS concentration gradients (Fig. 2 A and B) (Movie S1), consistent with electro-DP (35, 37), treating the (ionic) surfactant SDS as an electrolyte. By contrast, decane drops (Materials and Methods) migrate up SDS gradients (Fig. 2 C and D) (Movie S2), consistent with nonuniform SDS adsorption onto the droplet surface that creates either surface tension gradients, and thus “soluto-capillary” migration (57), or DP under strong adsorption (58). Irrespective of the detailed mechanism at play, a “soluto-inertial” (SI) beacon designed to emit SDS should attract decane droplets but repel PS particles.

Having identified suitable combinations of solute and suspended particles, we now turn to the beacon itself. The beacon must be designed to emit a long-lived solute flux, because the longer the beacon takes to equilibrate with its surrounding solution, the longer the diffusiophoretic interaction lasts. We achieve this long-lived flux by developing the solute analog of “thermal inertia,” wherein materials with high volumetric heat capacity resist changes in temperature and thus maintain long-lasting heat flux. SI beacons can be made from materials that strongly partition the solute, so that solute within the beacon (C_in) equilibrates at a concentration that exceeds the concentration in the neighboring solution (C_out) by a large partition coefficient K, giving C_out = K * C_in, where K >> 1 (59).

With such a choice, a beacon loaded with solute that is placed in a solute-free suspension equilibrates over long time scales, as demonstrated and described in Proof of Principle, ensuring a long-lived solute outflux (and thus SI interaction). Therefore, the key physicochemical property required of the SI beacon is that it strongly partitions whatever solute has been selected to attract or repel the colloids of interest.

Proof of Principle

Fig. 3 shows proof-of-principle demonstrations of the SI interaction described above, and specifically confirms the range, duration, and particle surface-specificity. Fig. 2 suggests that an SI beacon that emits SDS will repel PS colloids, and attract decane drops. SDS is known to associate with polyethylene glycol (PEG) (60, 61), suggesting that PEG hydrogels will strongly
partition SDS, and thus function as SI beacons. Fig. 3A shows a cylindrical SI beacon of radius $R \approx 200 \mu m$ created by photo-polymerizing a PEG-diacylate (PEG-DA) precursor solution in situ within a microfluidic device by exposure to masked, ultraviolet light (56, 62, 63), then flushing unreacted precursor from the device.

The experimental procedure is shown schematically in Fig. 3 B–D. An SI beacon is initially loaded by immersion in a 5-mM SDS solution (Fig. 3B). The SDS loading solution is then flushed by flowing in a suspension of colloids and/or drops (Fig. 3C). The SDS that had partitioned into the SI beacon is no longer in equilibrium with the surrounding solution, and therefore diffuses out of the SI beacon to equilibrate. The resulting SDS concentration gradient persists as long as SDS outfluxes from the SI beacon (Fig. 3D), within which suspended colloids and/or drops migrate diffusiophoretically.

Fig. 3 E–I reveals this system to behave as predicted: PEG-DA beads partition SDS, and therefore establish a long-lived, long-ranged SDS flux that effectively repels PS colloids but attracts decane drops. In particular, PS particles are repelled from the SI beacon (down the SDS gradient), forming a 300- to 400-μm-thick particle-free region around the beacon (Movie S3). PS particle migration is evident for at least 1,000 s, by which time most of the particles have migrated out of the microscope field of view. The particle surface specificity of SI interactions is verified by following the same procedure but introducing decane droplets instead of PS colloids. As expected, decane droplets experience a long-range, long-lasting SI attraction toward the beacon, moving up the imposed SDS gradient as shown by the streak lines in Fig. 3I and Movie S4. The range and duration in this case is comparable to that observed with PS particles. Notably, the SI interaction range (here 100–1,000 μm) is $10^2$–$10^4$ times larger than the Debye screening length that limits the electrostatic interaction.

**SI Model**

Having shown that the SI effect can be exploited to generate and direct diffusiophoretic motion in suspensions, we now develop a model of this behavior, focusing initially on spherical SI beacons to avoid the mathematical subtleties of 2D diffusion. A spherical SI beacon is initially loaded by immersion in a loading solution of concentration $C_{S0}^B$, and thus equilibrates with some beacon concentration $C_{S0}^B = KC_{S0}^E$. When suspended in a solute-free environment ($C_{S} = 0$), the solute in the beacon $C_{S}(t)$ diffuses out into the surrounding solution. We assume that the solute concentration within the beacon evolves rapidly enough that intrabeacon concentration gradients can be neglected [$C_{S}(r,t) = C_{B}(t)$], and that the concentration within the beacon $C_{B}(t)$ changes on time scales much slower than are required for $C_{S}(r,t)$ to evolve. Under these quasi-steady assumptions, the concentration field around a spherical, SI beacon of radius $R$ that partitions solute with a partition coefficient $K$ obeys

$$C_{S}(r,t) = \frac{C_{B}(t)}{K} \frac{R}{r}$$  \hspace{1cm} [1]

This concentration field gives rise to a diffusion-limited solute flux $\dot{J} = 4\pi DR C_{B}(t)/K$ out of the beacon, where $D$ is the diffusion coefficient of the solute. This outflux must equal the rate at which solute molecules are lost from the beacon,

$$\dot{J} = \frac{4\pi DR C_{B}(t)}{K} = -\frac{d}{dt} \left[ \frac{4\pi R^2}{3} C_{B}(t) \right],$$  \hspace{1cm} [2]

which can be solved to give the beacon concentration

$$C_{B}(t) = C_{B0} \exp \left( -\frac{3t}{2D} \right).$$  \hspace{1cm} [3]

Eq. 3 reveals a natural SI time scale,

$$\tau_{SI} \approx K \frac{R^2}{3D}$$  \hspace{1cm} [4]

over which SI beacons emit solute, which exceeds the diffusion time scale $\tau_D = R^2/D$ by the partition coefficient $K$, and may thus be many orders of magnitude longer when $K \gg 1$.

We now investigate the range over which colloidal particles migrate diffusiophoretically under the concentration gradient set by the SI beacon. Diffusiophoretic migration velocities under electrolyte gradients are predicted (35, 51) to obey

$$u_D = D_D \nabla \ln C_{S},$$  \hspace{1cm} [5]

where $D_D$ is the diffusiophoretic mobility of the particle, whose magnitude and sign both depend on the surface chemistry of the particle and solute. Using Eq. 5 for the quasi-steady concentration field around a spherical SI beacon (Eq. 1) reveals colloids to migrate under a quasi-steady SI outflux with velocity...
decaying with distance like \( r^{-1} \). Several features are notable: The SI migration velocity \( (i) \) is independent of \( C_B(t) \), the instantaneous concentration of solute in the beacon, \( (ii) \) decays slowly with distance from the SI beacon, and \( (iii) \) is particle surface-specific, as determined by \( D_{DP} \).

Quantitative Measurements of Migration Velocity

Trajectories of individual particles can be extracted from micrograph series, allowing particle velocities to be measured directly in space and time. Fig. 4 shows raw (Inset) and scaled velocity profiles at different times, around cylindrical SI beacons of two different radii \( R_p = 130 \mu m \) and \( 200 \mu m \).

No steady-state concentration profile exists for 2D structures like the SI beacons shown in Fig. 3. We therefore solve the transient mass transport problem analytically and numerically using COMSOL Multiphysics, under the same quasi-steady assumptions described in SI Model: Concentration fields \( C(r,t) \) in bulk solution evolve much more rapidly than in the SI beacon (Supporting Information and Fig. S1), and so we impose a quasi-steady boundary condition \( C_B(t) \). Guided by the scaling arguments for spherical SI beacons, we scale distance by the beacon radius \( R_p \), time by the diffusion time \( R_p^2/D_{SDD} \) of dissolved SDS, and concentrations by a concentration scale \( C_0 \). In cylindrical coordinates, the nondimensionalized diffusive mass transport equation in the radial direction is given by

\[
\frac{\partial \tilde{C}}{\partial \tilde{t}} = \frac{\partial}{\partial \tilde{r}} (\tilde{r} \frac{\partial \tilde{C}}{\partial \tilde{r}}),
\]

where \( C_0 = C(r(t=1),t=1) \) and \( t = (R_p^2/D_{SDD}) \). The diffusivity \( D_{SDD} \) of aqueous SDS below the critical micelle concentration is taken as \( 780 \mu m^2/s \) (64). The concentration field \( \tilde{C}(\tilde{r},\tilde{t}) \) is then computed by enforcing \( \tilde{C}(\tilde{r}=1,\tilde{t}) = 1 \) and \( \frac{\partial \tilde{C}}{\partial \tilde{r}}(\tilde{r} \to \infty,\tilde{t}) \to 0 \). The analytical solution (Supporting Information and Fig. S2) is in good agreement with the numerical model. The DP migration velocities of suspended particles can then be computed at any position and time from \( \tilde{C}(\tilde{r},\tilde{t}) \) using Eq. 5, and are simply proportional to \( \sqrt{\ln C_0} \).

The diffusiophoretic mobility \( D_{DP} \) of PS particles under SDS gradients is not known a priori. To compare the measured and calculated SI migration velocities, we normalize all measured or calculated velocities by a single value, corresponding to the maximum value that was measured or calculated,

\[
\bar{u} = \frac{u}{u_{\text{max}}} = \frac{\sqrt{\ln C_0}}{\text{max}} \sqrt{\ln C_0}
\]

So long as \( D_{DP} \) is constant, normalizing velocities in this way enables direct comparisons between measured and calculated velocity profiles at different times, irrespective of the single (unknown) parameter \( D_{DP} \).

Fig. 4 shows the nondimensional radial velocity profiles of PS colloids measured in experiments with SI beacons of radii \( R_p = 200 \mu m \) and \( R_p = 130 \mu m \) (empty red points). Each differently colored set of data corresponds to a finite time window, and depict the time evolution of the measured velocity profile around the beacon. Appropriate nondimensionalization allows the experimental data to be compared with the SI model, the predictions from which are plotted as solid lines corresponding to each of the experimental time intervals shown. When properly scaled according to the SI arguments presented above, measured velocity profiles show excellent agreement, in space and time, not only between the two different-sized SI beacons but also between the experimental measurements and the SI model predictions. This collapse justifies our choice of the length, time, and velocity scales as well as confirms that the mass transport model coupled with the quasi-steady state assumption captures the observed SI migration phenomenon quantitatively. It should be noted that, although the velocity profile appears increasingly flat as time progresses, it remains nonzero in both the SI model and the experiment. The success of the scalings for the SI time scale (Eq. 4) and distance scale \( R_p \), along with the quantitative agreement between theory and experiment in Fig. 4, underscores the quantitative capability to design a long-range, long-lasting suspension interaction.

Discussion and Conclusion

The general SI strategy described here shares many features in common with previous observations involving DP, specifically involving reacting or dissolving interfaces. Derjaguin et al. (35) elucidated the existence and influence of DP on latex film formation onto salt-soaked surfaces. Prieve (36) and coworkers noted an analogy with chemically reacting systems, e.g., as steel dissolution drives the diffusiophoretically accelerated deposition of latex particles. More recently, McDermott et al. (65) showed that calcium carbonate particles dissolving in unsaturated aqueous solutions act as diffusioporesmic micropumps, driving flows along neighboring surfaces. Zheng and Pollack (66) reported long-range exclusion near hydrogel boundaries, and Florea et al. (67) revealed ion exchange reactions to form a colloidal exclusion zone near membrane surfaces.

We have established a conceptual framework for the design and engineering of long-range, nonequilibrium interactions in suspension whose magnitude and direction depends on the surface chemistry of the suspended particles. Our results highlight the versatility and generality enabled by combining the slow, SI release of solute with the diffusiophoretic migration of suspended particles. The direction and speed of suspended particle
migration can be controlled by appropriate choice of solute, and the range and duration of the SI interaction can be tuned by choosing size and material of the SI beacon to maximize the partition coefficient. With the specific PEG-DA (beacon)–SDS (solute) system, we have revealed that SI interactions last for tens of minutes and extend over hundreds of microns. Moreover, fairly simple scaling arguments and numerical computations capture the quantitative and qualitative characteristics of SI interactions. Although specific experiments here used relatively large SI beacons held fixed in place, analogous physics and scaling arguments should also hold for freely suspended beacons, although beacon sedimentation introduces additional complexity. The generality of the SI concept naturally suggests a variety of new directions and applications, including the in situ separation and collection of particular suspended colloids, accelerated or triggered flocculation of emulsions and suspensions, layer-by-layer deposition, and other novel synthesis strategies.

Materials and Methods

Device Fabrication. A single inlet/outlet microfluidic device is used, with a large central circular chamber (Fig. 3). A corexy-motorized controlled laser cutter (Trotec Speedy 100) cuts the channel into 60-µm-thick stock tape. The cut tape is then stuck to a Petri dish, which is used as a master for making a polydimethylsiloxane (PDMS) replica of the design. The PDMS master is used to fabricate the device in “microfluidic stickers” (N0A–81; Norland Adhesive) (68). The central chamber has a radius of 2 mm, and the inlet and outlet channels are 500 µm wide. A glass cover slide is used to seal the device, with holes drilled to provide access to the inlet and outlet tubing. A PDMS inlet is ozone-bonded to the cover slide to provide support for inlet and outlet pins and tubings. The device is then baked at 80 °C for at least 4 h to strengthen bonding.

Sample Preparations. SDS solutions are prepared by diluting a 10 mM SDS (Sigma Aldrich) stock solution in deionized water. PEG-DA precursor solution is prepared by mixing 33% (v/v) polymer (PEG) (700-Da-DA) (Sigma–Aldrich) with 4% (v/v) of the photoinitiator (2-hydroxy-2-methylpropiophenone; Sigma–Aldrich) in deionized water; 0.25% vol/vol fluorescent PS beads, 1 µm in diameter (FS03F, Bangs Laboratories), are suspended in clear deionized (DI) water to form the PS suspension. The decane emulsion is prepared by first adding 0.5% vol/vol fluorescent yellow 1315C dye (Keystone) to decane (Sigma–Aldrich); 1% vol/vol of the dyed decane is vortexed for 30 s with a 1-µm SDS solution (in DI water) and then sonicated for 15 s to create 1- to 2-µm decane droplets in water.

Experimental Setup. PEG-DA gels are used as SI structures and fabricated using the microscope projection lithography technique (62, 69). A UV lamp is set to 1,000–2,000 W/cm² (measured at an empty objective slot). A 1,000–mW UV exposure is then used with a 10× objective. Then a 500-ms UV exposure is used with a 10× objective and the objective of MagnaScant (Nikon TE2000U). The hydrogel SI structure is initially loaded with a fixed concentration (5 mM) of SDS, by maintaining flow in the channel for 20 min. SDS solution is then flushed out by displacing with the suspension of PS particles or decane drops. The inlet is pressurized to 500 mbar, and the channel is flushed for 5 s before reducing the pressure to 20 mbar. The focus is adjusted to the center of the channel using a 10× objective. Void fraction imaging is started (with an 100× fluor 685 fluorescence sensor) and flow in the channel is stopped using the technique described in ref. 40. In each experiment, images are recorded for 1,000 s at 1 frame per second, with 0.1-s exposure times.

Data Analysis. The 2D particle trajectories are extracted from the fluorescence micrograph series using algorithms adapted from those of Crocker and Grier (70) and implemented in the R programming language, previously used for analysis of bright-field micrographs (71). For each image series, a background image was calculated by finding the time-averaged brightness for each pixel. This background was subtracted from each image in the series. Images were further processed with a spatial band-pass filter and a local background subtraction to eliminate pixel noise and long wavelength brightness fluctuations. This processing has the added benefit of removing out-of-focus particle images, allowing the analysis to focus on particles in the microscope’s focal plane. A brightness-weighted centroiding approach is used to identify candidate particle positions, and a brightness-weighted centroiding over the particle diameter is performed to obtain particle coordinates with subpixel precision. Finally, trajectories are obtained by linking particle positions between frames in the acquired videos.

The PS particles explore all three dimensions on the timescale of the experiment. However, due to the axisymmetry of the concentration gradient, 2D tracking in the x–y plane is sufficient to observe and explore the diffusion-dominated particle motion in the channel. The particle direction are obtained from frame-to-frame displacements, and velocity profiles are calculated by averaging the velocities within annular regions of 50 pixels width with the origin fixed at the center of the channel. The concentration profile evolves with time and, therefore, so does the velocity profile, and, as such, velocity profiles are calculated independently over 4.5-s (for R = 130 µm) and 10-s (for R = 200 µm) intervals throughout the experiment. Splitting the experiment into chunks in this way provides more samples in each annular bin, improving the statistics of averaging and suppressing noise in the velocity profiles.

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