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THE ORIENTATION OF THE PRIMARY DONOR
IN BACTERIAL PHOTOSYNTHESIS

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SUMMARY

The triplet state EPR spectra of magnetically aligned whole cells of *Rhodopseudomonas viridis* and *Rhodopseudomonas palustris* display a marked dependence on the orientation of the static EPR field with respect to the alignment field direction. This observation implies that the primary donor species on which the triplets are localized are ordered within the membranes. We have developed a theoretical model for the system to enable calculation of the orientation of the magnetic axes of the primary donor species with respect to the membranes in which they reside. The triplet state spectra are generated by an ensemble of partially ordered magnetic systems and a computer simulation of the experimental results. The triplet orientation is very similar for the two organisms studied, where one axis lies predominantly in the plane of the membrane and the other two axes have approximately equal projections onto the normal to the membrane.
INTRODUCTION

Electron paramagnetic resonance (EPR) techniques have been used extensively in the study of triplet states in photosynthetic bacteria\(^1\). Experiments performed at zero field, and at high field, have focused on the triplet state as a probe into the structure of the reaction center\(^2,3\) and as an indicator in redox titrations of the various components involved in the primary light reactions of bacterial photosynthesis\(^4-6\).

The primary donor (designated \(P\)) in bacterial photosynthesis is a dimeric bacteriochlorophyll species \(^4,7-9\). There is strong evidence that the triplet state readily observed in various photosynthetic bacterial organisms belongs to this dimer\(^10\) but is not part of the main pathway leading to photosynthesis\(^11\). This triplet state forms as the result of a radical pair recombination reaction that occurs between the oxidized primary donor and a reduced initial acceptor (labeled \(I\)). This happens when the electron flow has been blocked at a position immediately following \(1^6,11\).

In this paper we consider the triplet states of two species of photosynthetic bacteria, \textit{Rhodopseudomonas viridis} and \textit{Rhodopseudomonas palustris}.\(^{†}\) Both of these bacteria are prolate ellipsoidal organisms with highly ordered

\(^{†}\text{Rps. palustris differs from Rps. viridis in its pigmentation. Rps. viridis is a bacteriochlorophyll b containing organism, whereas Rps. palustris has bacteriochlorophyll a as its major pigment.}\)
(cylindrical) internal membrane structures\textsuperscript{12-14} (see Fig. 1). Reaction center particles which contain the primary donor are dispersed throughout these membranes. Electron microscope studies suggest that there is some degree of ordering of these particles in the membranes\textsuperscript{12}.

These bacterial organisms tend to align with their longitudinal axis perpendicular to an applied strong magnetic field\textsuperscript{15,16}. This occurs in whole cells as the result of an induced diamagnetic moment within the membrane structures\textsuperscript{15}. Recently, Paillotin \textit{et al}\textsuperscript{16}, using linear dichroism and photoselection techniques on magnetically aligned \textit{Rps. viridis} cells have observed an orientation of the reaction center complexes within the bacterial membranes and have concluded that the primary donor resides in a fixed geometric relation to the membranes\textsuperscript{16}. Two transition moments of the primary donor centered at 970 nm and 850 nm have been calculated to lie parallel to and at an angle greater than 55° to the membrane planes, respectively. Characterization of the two other bacteriochlorophyll molecules in the reaction center of \textit{Rps. viridis} using this technique revealed that they are also coherently arranged.

In the present work we present a triplet state EPR study complementary to the aforementioned linear dichroism investigation. We have magnetically aligned whole cells of \textit{Rps. viridis} and \textit{Rps. palustris} and studied their triplet
state properties using a light modulation technique. By positioning the sample so that the static EPR field is either parallel or perpendicular to the alignment field direction, an orientation effect on the triplet signals is observed. From a knowledge of the distribution of the magnetically aligned cells and their internal membrane structure, we are able to calculate the projections that the triplet magnetic axes make with respect to the normal to the membranes.

Our approach is to construct a computer model that treats the sample of aligned bacterial organisms as an ensemble of partially ordered triplet states. An orientational distribution function that describes the manner and the degree of the system ordering is derived and used in simulating the observed spectra. In addition to the orientation information, zero-field splitting parameters and relative intersystem crossing rate constants for the triplet states are calculated.
MATERIALS AND METHODS

*Rps. viridis* cells were grown according to the method of Eimhjellen, *et al.* Freezen dried *Rps. palustris* was obtained from the American Type Culture Collection (strain ATH 2.1.6) and grown in a culture medium described by Morita and Miyazaki. Both bacteria were harvested separately by centrifugation at 7000×g for 10 min, washed with 0.025 M Tris (pH, 7.5) buffer during the final spin, and stored at -20°C until ready for use. All of the samples utilized in the present work were prepared under a nitrogen atmosphere and contained 0.02 M sodium dithionite, 1.0 × 10⁻⁵ M methyl viologen, 0.05 M glycine (pH, 10.1) buffer and 50% ethylene glycol.

Magnetic alignment of the cells was achieved in the dark by placing the sample between the pole faces of a 21 kG magnet and freezing in a liquid nitrogen flowing cryostat. The sample was stored at 77°C in the dark.

EPR measurements were accomplished using a Varian E-109 spectrometer at X-band with 100 kHz field modulation and equipped with an Air Products Helitron cryostat. The triplet states of the bacteria were detected using a light modulation technique similar to that used by other authors. The output of the EPR system was fed directly to a Princeton Applied Research Model 220 lock-in amplifier. The reference signal for the lock-in was taken from a 33.5 Hz chopper.
Excitation of the bacteria into their triplet states was achieved using a tungsten lamp filtered by 5 cm of water and focused through the 75% transmitting grid of a Varian TM_{110}(E-238) microwave cavity. Light intensity was kept below 25 mW/cm². Experiments were done routinely at 11°K, and no temperature dependence of the ratios given in Table 1 was observed up to 20°K. Microwave power was kept below the saturation level.

Finally, because the experimental signals shown in Figures 2 and 3 are distorted in field position and in intensity owing to sweeping the recorder too quickly, the signal amplitudes used in the computer simulations were not taken from these spectra. Instead, the amplitudes were measured by dialing the magnetic field to coincide with the signal positions and recording the peak heights after a sufficient time for the signals to reach the maximum level. Because the pairs of measured signal intensities were found to be the same within experimental error, the values for the amplitudes are hereafter designated X⁺, Y₁⁺, Y₂⁺ and Z⁺.
RESULTS AND DISCUSSION

Theoretical Model of Triplet State EPR

The Hamiltonian matrix for the triplet state in the zero-field basis is given in the usual form\textsuperscript{21}

\[
\begin{bmatrix}
|T_x> & |T_y> & |T_z>
\end{bmatrix}
\]

\[
\begin{bmatrix}
X & -i\beta H_z & i\beta H_y \\
-i\beta H_z & Y & -i\beta H_x \\
i\beta H_y & i\beta H_x & Z
\end{bmatrix}
\]

where

\[
|T_x> = \frac{1}{\sqrt{2}}|\beta \beta -\alpha\alpha>
\]

\[
|T_y> = \frac{i}{\sqrt{2}}|\beta \beta +\alpha\alpha>
\]

\[
|T_z> = \frac{1}{\sqrt{2}}|\alpha \beta +\beta \alpha>
\]

and \(X, Y, \) and \(Z\)

are the principal values of the spin-dipolar interaction tensor. These quantities are related to the two independent spin parameters \(|D|\) and \(|E|\) by the equations.
\[ X = \frac{1}{3} |D| + |E| \]
\[ Y = \frac{1}{3} |D| - |E| \]
\[ Z = -\frac{2}{3} |D| \]  

The eigenstates and eigenvalues of \( \mathcal{H} \) are clearly dependent upon the orientation of the static EPR field in the principal axis system of the triplet. Once this orientation is specified, the Hamiltonian can be diagonalized numerically to obtain the wavefunctions and energy levels of the system.

Because the experiments were performed in the high field limit \( |gB| \gg |D, |E| \), one expects the eigenstates of \( \mathcal{H} \) to be close to the high-field eigenstates

\[ |T_{+1}\rangle = |\alpha\alpha\rangle \]
\[ |T_{0}\rangle = \frac{1}{\sqrt{2}} |\alpha\beta + \beta\alpha\rangle \]  
\[ |T_{-1}\rangle = |\beta\beta\rangle \]  

The eigenstates of \( \mathcal{H} \) can be expressed as linear combinations of the zero-field states. The appropriate linear combinations depend upon the orientation of the static EPR field, \( \mathcal{H} \), in the principal axis system. Qualitatively, the components of the \( |T_{0}\rangle \) state depend upon the projection of \( \mathcal{H} \) onto the \( x,y \) and \( z \) magnetic axes, \( e.g., \) if \( \mathcal{H} \parallel x \), then \( |T_{0}\rangle = |T_{x}\rangle \), \( etc. \)
When \( \hat{H} \) is not precisely along a magnetic axis, one obtains three energy levels close to \( |T_{+1}\rangle, |T_0\rangle \) and \( |T_{-1}\rangle \) designated \( |T_a\rangle, |T_\beta\rangle \) and \( |T_\gamma\rangle \). This designation is structured so that \( E_a \sim E_{+1}, E_\beta \sim E_0 \) and \( E_\gamma \sim E_{-1} \), and it will be generally true that as a consequence of the high field approximation

\[
|E_\beta - E_a|, |E_\beta - E_\gamma| \sim |g\beta \hat{H}| \text{ for all orientations.}
\]

Ultimately the eigenstates are expressed as

\[
|T_i\rangle = \sum_j |T_j\rangle c_i^j \quad (5)
\]

where \( c_i^j \) are the eigenvector coefficients, which come from the diagonalization of the Hamiltonian matrix (eq. 1).

Because the triplet state being considered is formed by a radical pair mechanism\(^{11}\), at high magnetic fields the light-induced triplet is assumed to be populated in the \( |T_\beta\rangle \) spin sublevel exclusively. This assumption is consistent with the spin polarization pattern of the observed triplet state spectra (see Figs. 2 and 3), which have been discussed in great detail by many authors\(^{11,20,22}\).

The effects of triplet state deactivation are incorporated via a simplified version of the models described by Winscom\(^{23}\) and Levanon and Vega\(^{24}\). Their kinetic equation for the triplet sublevel populations as a function of time is

\[
\frac{dn_{T}}{dt} = -\hat{k} \cdot n + A \quad (6)
\]
where

\[
\mathbf{n} = \begin{bmatrix}
    n_\alpha \\
    n_\beta \\
    n_\gamma
\end{bmatrix}
\]  

(7)

gives the steady state populations of the three triplet spin sublevels,

\[
\mathbf{A} = \begin{bmatrix}
    A_\alpha \\
    A_\beta \\
    A_\gamma
\end{bmatrix}
\]  

(8)

represents the populating rates of the three sublevels, and

\[
\mathbf{k} = \begin{bmatrix}
    k_\alpha + W_\alpha \beta + W_\alpha \gamma & W_\alpha \beta & W_\alpha \gamma \\
    W_\beta \alpha & k_\beta + W_\beta \gamma + W_\beta \alpha & W_\beta \gamma \\
    W_\gamma \alpha & W_\gamma \beta & k_\gamma + W_\gamma \alpha + W_\gamma \beta
\end{bmatrix}
\]  

(9)

where \( k_\alpha, k_\beta \) and \( k_\gamma \) are the rate constants for intersystem crossing between the triplet sublevels and the ground state, and the \( W \)'s are the rate constants for spin-lattice relaxation between the triplet spin sublevels.

If only the \( |T_\beta> \) level is populated in the light-modulated generation of the triplet state, one can set \( A_\beta = A_0 \sin(\omega t) \) and \( A_\alpha = A_\gamma = 0 \), where \( \omega \) is the frequency of light modulation. The intersystem rate constants can be
expressed as

\[ k_i = \sum_j |c_j^i|^2 k_j \]  \hspace{1cm} \text{(10)}

\[ i = \alpha, \beta, \gamma \]

\[ j = x, y, z \]

where the \( k_x, k_y \) and \( k_z \) values can be determined experimentally\(^{24,25}\) (e.g. by optical detection of magnetic resonance), or by computer simulation (see below). The absence of a temperature dependence of the triplet spectrum in the temperature region in which the experiments were performed and the observation of substantial spin polarization indicate that spin-lattice relaxation is of negligible importance. It is assumed hereafter that \( k_x, k_y, \) and \( k_z \gg W_{ij} \), and therefore \( W_{ij} = 0 \) in equation (9).

A simplified set of differential equations is now obtained. These are

\[ \frac{dn_\alpha}{dt} = -k_\alpha n_\alpha \]  \hspace{1cm} \text{(11)}

\[ \frac{dn_\beta}{dt} = -k_\beta n_\beta + A_o \sin(\omega t) \]  \hspace{1cm} \text{(12)}

\[ \frac{dn_\gamma}{dt} = -k_\gamma n_\gamma . \]  \hspace{1cm} \text{(13)}

These are easily solved to yield an expression for the population difference between two of the levels. Neglecting
exponential terms that will average to zero in the next step, the result in the limit of low microwave power is

\[ \Delta n_+ = (n_\beta - n_\alpha) \approx n_\beta \]
\[ \Delta n_- = (n_\beta - n_\gamma) \approx n_\beta \]

\[ \Delta n_+ = \Delta n_- = \frac{A_o \sin(\omega t + \phi)}{\left(\omega^2 + k_\beta^2\right)^{1/2}} \]  

where \( \phi \) is the phase difference between the reference and detector signals. In the light-modulation experiment the reference signal given by \( R = B \sin(\omega t) \) multiplies equation (16) and averages over time. Furthermore, because \( k_\beta \gg \omega \) (a chopper frequency of 33.5 Hz is used and \( k \) values for similar bacterial systems are known to be at least an order of magnitude larger \( ^2 \) ) one obtains

\[ \frac{2\pi}{\omega} \int \frac{\omega}{2\pi k_\beta} A_o \sin(\omega t + \phi) B \sin(\omega t) \, dt. \]  

Adjusting the phase difference between the reference and detector signals to be zero (i.e. \( \phi = 0 \) and integrating, equation (17) reduces to

\[ \Delta \bar{n}_\pm = \frac{C}{k_\beta} \]  

where \( C \) is a constant term.

Thus each discrete orientation yields two transitions, one in emission and one in absorption. Since the EPR intensity, \( I \), of a transition is proportional to the population
difference, \( \Delta n_{\pm} \), the calculated amplitudes are weighted by the inverse of the intersystem crossing rate, \( k_\beta \), which depends upon the contributions of \( k_x \), \( k_y \) and \( k_z \) to \( k_\beta \), as described in equation (10).

**Triplet State EPR from a Randomly Ordered Ensemble**

The experimental EPR intensity at a particular static EPR field, \( |H| \), is an ensemble average of the triplet signals from all possible orientations of the magnetic system. For a randomly oriented ensemble we have

\[
\bar{I}(|H|) = \int_0^{\pi/2} \int_0^{\pi/2} I(\theta, \phi, |H|) \sin \theta \, d\theta d\phi
\]

(19)

where \( I(\theta, \phi, |H|) \) is the intensity of the triplet signal at field \( |H| \) when the static EPR field is specified by the angles \( \theta \) and \( \phi \) in the principal axis system of the triplet.

From the previous section two transitions with energies \( \epsilon_1 \) and \( \epsilon_2 \) are obtained by diagonalizing the triplet Hamiltonian matrix [eqn. (1)] with \( H_x \), \( H_y \) and \( H_z \) determined by \( \theta \) and \( \phi \).

The intensity is

\[
I(\theta, \phi, |H|) = \frac{1}{k_\beta(\theta, \phi, |H|)} \{ \exp[-(\epsilon_1 - |H|)^2/\delta^2] - \exp[-(\epsilon_2 - |H|)^2/\delta^2] \}
\]

(20)
where it is assumed that each transition has a gaussian profile with line-width $\delta$, and the intensity associated with $\varepsilon_2$ is negative because this transition is in emission.

The overall spectral lineshape depends upon the zero-field splitting parameters, $|D|$ and $|E|$, and the intersystem crossing rates, $k_x$, $k_y$ and $k_z$. When these are known, eqn. (20) can be evaluated numerically at many field positions to simulate the triplet spectrum.

**Simulation of Random Triplet State Spectra**

The $|D|$, $|E|$, $k_x$, $k_y$ and $k_z$ parameters were adjusted to obtain the best fit to the random triplet state spectra of *Rps. viridis* and *Rps. palustris*. This was accomplished by measuring the amplitudes of the triplet signals at a number of key field positions (see Figs. 2 and 3), calculating ratios, $R_E$, of these amplitudes (see Table 1) and fitting the theoretical spectrum to these ratios.

As a general procedure the $|D|$ parameter was fit first by adjusting it to agree with the separation between the $Z^+$ and $Z^-$ outermost peak positions (Figs. 2 and 3). Then the $|E|$ value was adjusted to the positions of the $X^-$, $Y_1^-$, $X^+$ and $Y^+$ peaks, and the $k_x$ and $k_y$ values were fit to the experimental $Z^+/X^+$ and $Z^+/Y_1^+$ ratios, respectively. Because there is some experimental uncertainty in determining the field corresponding to $Y_1^-$ and $Y_1^+$, the $Y_2^-$ and $Y_2^+$ amplitudes were used as checks on the E parameter. The parameters that best fit the random triplet state spectra of *Rps. viridis* and *Rps. palustris* are given in Table 2. Calculated spectra are displayed in Figs. 4a and 5a.
Triplet State EPR from Partially Ordered Ensembles

Our approach to the calculation of the triplet state EPR spectrum of a partially ordered ensemble is to determine a distribution function, \( D(\theta, \phi) \), specifying the probability that a member of the ensemble has a static EPR field direction whose orientation in the principal axis system of the triplet is between \( \theta \) and \( \theta + d\theta \), \( \phi \) and \( \phi + d\phi \). The EPR intensity given by equation (19) now becomes

\[
\bar{I}(|\mathbf{H}|) = \int_{\theta}^{\theta+d\theta} \int_{\phi}^{\phi+d\phi} I(\theta,\phi,|\mathbf{H}|) D(\theta,\phi) \, d\theta \, d\phi. \tag{21}
\]

The details of the method of calculation of \( D(\theta,\phi) \) are presented in a separate publication\(^{26}\) which treats both the general case and the specific one of magnetically aligned \textit{Rps. viridis} cells. In the present paper the derivation of \( D(\theta,\phi) \) will be discussed qualitatively and the interested reader is referred to reference [26] for a mathematically rigorous approach.

As discussed previously the bacteria used in these experiments are approximately prolate ellipsoids (see Fig. 1). The internal membranes form concentric, roughly cylindrical sheets having a common axis with the longitudinal axis of the cell. The reaction center particles, which contain the paramagnetic species giving rise to the light-induced triplet state spectra are imbedded in these membranes.
Three axis systems which will be useful in characterizing the distribution of the magnetic systems are now defined (see Fig. 1):

1) The **laboratory axis system** is one in which the static EPR field has fixed components. The orientation of various members of the ensemble of spin systems is specified with respect to this fixed reference frame.

2) The **principal magnetic axis system** is the coordinate system in which the dipolar Hamiltonian $\mathcal{H} = S \cdot \hat{D} \cdot S$ is diagonal. It is related to the intermediate axis system by a fixed set of Euler angles, $\alpha'$, $\beta'$ and $\gamma'$.

3) The **intermediate axis system** serves as a bridge between the laboratory frame and the principal magnetic axis system. One can think of the magnetic system as being enclosed in a cube. The unit vectors of the intermediate axis system lie along three joined edges of the cube. The magnetic system is fixed within the cube, so that an Euler rotation matrix, $A(\alpha', \beta', \gamma')$, will bring the magnetic axis system into coincidence with the intermediate axis. This transformation is the same for every member of the ensemble.

The ensemble of magnetic systems is generated by performing a set of symmetry operations on an initially superimposed on the laboratory axis system. These symmetry operations can be derived from a consideration of the orienting process.
and the morphology of the organism. The ensemble so generated is an ensemble of intermediate axis systems. It will be necessary later to transform to the principal axis system.

As mentioned before, the 21 kG magnetic field axis aligns the cells so that their longitudinal axes lie in a plane normal to the alignment field. Because this is the only restriction, there are still two symmetry operations which can be performed on the cells; rotation $\chi$ about the alignment field and rotation $\mu$ about the longitudinal axis of the cell. These operations are illustrated in Fig. 1.

Linear dichroism$^{15}$, photoselection$^{16}$, and the present experiments suggest that the reaction center particles are highly ordered within the membranes. A convenient and physically reasonable convention is that the membrane surface defines a unique axis normal to it. This analysis hypothesizes a random distribution of $\wedge$ about this direction and therefore generates a third symmetry operation $\lambda$ (see Fig. 1). The theoretical analysis is greatly facilitated by choosing the membrane normal to be coincident with the $z$ axis of the intermediate axis system.

If the above ordering were perfect, i.e. the cells were perfect ellipsoids, the membranes perfect cylinders, the alignment in the magnetic field complete, and the unique reaction center particle axis always $0^\circ$ from the normal, it would be easy to generate the ensemble from the above symmetry
operations. However, it is necessary to take into account deviations from these conditions. The most significant deviations are likely to be imperfections in the cell shape and membrane surface. This can be described by a tilt of the membrane normal from the perfect cylinder normal. We call this tilt the wobble angle, \( w \), (see Fig. 1).

The imperfections introduce some uncertainty into the value of this angle. This problem is treated phenomenologically by defining a distribution function, \( g(w) \), which gives the probability that a member of the ensemble has a particular wobble, \( w \). For the calculation this function is taken to be a Gaussian

\[
g(w) = \cos w \exp(-w^2/\Delta^2)
\]

where \( 1.7\Delta \) equals the full width at half maximum and is hereafter referred to as the disorder parameter, and the \( \cos w \) provides the proper volume element for the integration.
The problem now is to obtain $\mathcal{D}(\theta, \phi)$ in eqn. (21) by a consideration of $g(w)$. It suffices to calculate $\mathcal{D}'(\theta', \phi')$, the distribution function of having static EPR field components specified by $\theta'$ and $\phi'$. It is then a simple matter to calculate $\mathcal{D}(\theta, \phi)$ of eq. (21) from $\mathcal{D}'(\theta', \phi')$ using the fixed geometrical relation between the intermediate axis system and the principal axis system.

The intuitive way to approach this is to ask the question:

Given a member of the ensemble with the static EPR field specified by $\theta'$ and $\phi'$, what is the value of $w$ which generated this orientation? Unfortunately, one can not answer this question directly; because of the three other symmetry operations, $w$ is not uniquely defined by $\theta'$ and $\phi'$.

This suggests, however, that one could express $\mathcal{D}'(\theta', \phi')$ as an integral over $g(w)$ and some other function which gives the probability that the ensemble member was generated via a wobble, $w$. Such an expression can be obtained by a formal coordinate transformation. This procedure is outlined by Friesner et al.\textsuperscript{26} The final expressions for the cases of the static EPR field parallel and perpendicular to the alignment field direction are given below.

$$\mathcal{D}'(\theta') = \sin\theta' \int_{\cos w = 1}^{\cos w = \cos \theta'} \left(1 - \frac{\cos^2 w}{\cos^2 \theta}\right)^{-1/2} \frac{g(w)}{\cos w} \, dw$$

(23)

$$\mathcal{D}'(\theta') = \sin\theta' \int_0^{\pi/2} \frac{g(w)}{\cos w} \cdot G(\theta', w) \, dw$$

(24)
where

\[ G_\pm(\theta', \omega) = \frac{2}{\sqrt{[1 \pm \sin(\theta' + \omega)][1 \pm \sin(\theta' - \omega)]}} K(k_\pm) \]  

(25)

and

\[ k_\pm = \left\{ \frac{\pm [2\sin(\theta' - \omega) + \sin(\theta' + \omega)]}{[1 \pm \sin(\theta' + \omega)][1 \pm \sin(\theta' - \omega)]} \right\} \]

(26)

\(K(k_\pm)\) is the complete elliptic integral of the first kind, and

\[ G(\theta', \omega) = \begin{cases} 
G_+(\theta', \omega) & \text{for } [\sin(\theta' - \omega) + \sin(\theta' + \omega)] > 0 \\
G_-(\theta', \omega) & \text{for } [\sin(\theta' - \omega) + \sin(\theta' + \omega)] < 0
\end{cases} \]

Note that \(D'\) has been reduced to an axial form, i.e. depends only on \(\theta'\). Intuitively, this is what one would expect, since there is ordering in only one angular parameter, \(\omega\). Because both \(D'_\parallel(\theta')\) and \(D'_\perp(\theta')\) can be evaluated numerically, one can then use equation (21) to simulate the parallel and perpendicular triplet spectra of \(Rps. \ viridis\) and \(Rps. \ palustris\).

Simulation of Partially Ordered Triplet State Spectra

The results of the previous section gives the distribution function for the ensemble of intermediate axis systems. To use eqn. (21) one needs the probability distribution function in the principal axis system. This is obtained as follows: The static EPR field orientation is characterized by \(\theta\) and \(\phi\) in the principal axis system. The angle, \(\theta'\), between the membrane normal and the static EPR field is derived from the relation

\[ \cos \theta' = \mathbf{n} \cdot \mathbf{H}(\theta, \phi) \]

(28)
Then

\[ \theta' = \cos^{-1} [n \cdot \hat{H} (\theta, \phi)] \quad (29) \]

or

\[ \theta' = \cos^{-1} [n \cdot \hat{H} (\theta, \phi)] \]

Then

\[ \psi(\theta, \phi) = \frac{\sin \theta \cdot \psi'(\theta')}{\sin \theta'} = \frac{\sin \theta \cdot \psi' \{\cos^{-1} [n \cdot \hat{H} (\theta, \phi)]\}}{\sin \theta'} \quad (30) \]

where \( \sin \theta \) is the Jacobian for the transformation of the distribution function from the intermediate axis system to the principal axis system. \( ^{26} \)

The variable parameters to be determined in this simulation are the disorder parameter, \( \Delta \), [eqn. (22)] and the orientation of the normal to the membrane in the principal axis system. The latter is determined by projections of the normal on the three magnetic axes and designated \( X_n, Y_n \) and \( Z_n \) (only two of which are independent). The \( |D|, |E|, k_x, k_y \) and \( k_z \) values determined by the random simulation were held constant.

The fitting procedure was done as follows: Ratios of the experimentally observed amplitudes were calculated for the parallel and perpendicular cases (see Table 1). Values for \( Z_n \) and \( \Delta \) were chosen, and plots of the theoretical minus experimental ratios, \( (R_T - R_E) \), verses \( X_n \) were made (see Figs. 6 and 7), \( X_n \) being varied between 0.1 and 0.9. Then in a systematic fashion \( \Delta \) was varied between 0.1 and 1.6, and \( Z_n \) was varied between 0.1 and 0.9. A set of parameters were sought for which the graphs indicated \( (R_T - R_E) = 0 \) within experimental error for all six ratios.

The best solution for \( R_{ps. \ viridis} \) is given in Table 3. As shown in Fig. 6 all six curves cross zero near \( X_n = .67 \) where \( Z_n = 0.10 \) and therefore \( Y_n = 0.74 \). These numbers are easily converted into the angles that the three principal
axes make with the normal by the relations \( \theta_X = \cos^{-1} \frac{x}{n} \), etc. 
\( \Delta = 0.4 \) represents the disorder in the system as defined by eqn. (22). The calculated spectra for the static EPR field parallel and perpendicular to the alignment field are shown in Figs. 4b and 4c.

For the \textit{Rps. palustris} organism the solution in Table 3 indicated a geometry similar to \textit{Rps. viridis}. A larger value for \( \Delta \) was necessary however, to simulate the \textit{Rps. palustris} triplet state spectra, and this most likely reflects a distortion of the cells away from their ellipsoidal shape or a less complete alignment in the magnetic field. Nevertheless, the spectra were simulated (see Figs. 5b and 5c), and Fig. 7 shows that \((R_T - R_L) = 0\) for all six ratios for the parameters, \(X_n = 0.69\), \(Y_n = 0.69\), \(Z_n = 0.25\) and \(\Delta = 0.6\) given in Table 3.

Typical sets of non-solution curves for \textit{Rps. viridis} and \textit{Rps. palustris} are given in Figs. 8 and 9. Clearly, no point along the abscissa provides a solution as previously defined.

CONCLUSION

A simulation of the random experimental spectra of these triplet states provides an alternate method to those of other groups\(^{24,25,27}\) for measuring their static and kinetic parameters. The \(|D|\) and \(|E|\) parameters extracted from this work do not differ appreciably from previous measurements by other groups\(^{5,27}\). The kinetic constants for the two species of bacteria have not yet been experimentally determined by
other methods. In principle, optical detection of magnetic resonance can provide a more accurate determination of the rate constants. However, there have been serious discrepancies in the values for these decay constants reported by different groups for similar systems\textsuperscript{2,27}. Our method provides an independent measurement of the relative values of $k_x$, $k_y$ and $k_z$.

It is interesting to note that the kinetic constants extracted from these measurements and given in Table 2 display a different trend for \textit{Rps. viridis} (i.e., $k_y > k_x > k_z$) than for \textit{Rps. palustris} (i.e., $k_x > k_y > k_z$). The factors controlling these trends are beyond the scope and focus of the present work; they have been dealt with in detail in previous publications\textsuperscript{28,29}.

Models for the orientation of the triplet magnetic axes of the primary electron donor with respect to the membranes in \textit{Rps. viridis} and \textit{Rps. palustris} are given in Fig. 10. Figs. 2 and 3 show that the effect of orientation on the triplet state spectra for the two organisms is very similar. Therefore, it is not surprising that the calculation yields similar geometries for the triplet magnetic axes in the two species. Perhaps more remarkable is the fact that a unique orientation of the triplet magnetic axes exists in two different bacterial organisms having chemically distinct primary donors.

For both \textit{Rps. viridis} and \textit{Rps. palustris} only one region of the three dimensional space spanned by the three independent parameters, $X_n$, $Z_n$ and $\Delta$, gave a solution to the
orientation problem within experimental error. This region of solution was approximated by a rectangular parallelepiped with boundary conditions given in Table 4. The region of solution was relatively large for Rps. palustris since the orientation effect was small. The larger orientation effect in Rps. viridis led to a correspondingly smaller region of solution for this organism. The error limits that appear involve the repeatability of the experimental measurements as stated in the legend of Table 1. Our investigation of the light intensity dependence, microwave power dependence and temperature dependence of the amplitude ratios given in Table 1 led us to the conclusion that systematic errors from these sources were negligible.

These results represent the first report of an oriented triplet state in photosynthetic systems. It is therefore appropriate to contrast our technique with other methods of extracting orientation information; e.g., linear dichroism. First, our method provides a good quantitative estimate for the degree of disordering of the system; this is reflected in the narrow range of acceptable values for $\Lambda$. The determination of the disorder parameter from linear dichroism experiments is much more uncertain. Secondly, we obtain information about the orientation of magnetic axes rather than optical transition moment directions. This information provides an independent set of data which can be used in conjunction with optical measurements to locate the bacteriochlorophyll monomers of the special pair within the membranes.

The problem of the orientation of the dimer pair in the photosynthetic membrane can be divided into two parts:

1) The relative orientation of the two bacteriochlorophyll monomers. This can be specified by five angles and the center-to-center distance, $R_{12}$.
2) Orientation of the dimer pair with respect to the membrane surface. This is specified by three angles.

In this paper we have determined two of the three angles needed to orient the dimer pair in the membrane. The third angle may not be uniform over the ensemble, (e.g. if the dimer pair has no preferred orientation about the normal to the membrane). It may be possible to combine our results with the linear dichroism studies to investigate this question more quantitatively.

Our results, in combination with the linear dichroism work, set some conditions in the relative orientation of the two monomers. However, there are not enough independent conditions to determine the six unknown coordinates for this part of the problem. We therefore intend to combine the present work and linear dichroism measurements with circular dichroism and optical detection of magnetic resonance data to obtain a coherent and self-consistent picture of the structure of the reaction center in bacterial photosynthesis. The use of these techniques in combination will over-determine the solution to this very important problem and therefore, allow us to propose a structure for the relative orientation of the two bacteriochlorophyll monomers with respect to each other and to specify the orientations of the dimer pair with respect to the membrane in which it resides.
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REFERENCES


TABLE 1

Experimental Amplitude Ratios

$Z^\pm, X^\pm, Y_1^\pm$ and $Y_2^\pm$ refer to the amplitudes (in arbitrary units) of the triplet peaks as defined in the Materials and Methods section. The errors represent the range of possible values for the ratios as deduced from the repeatability of the amplitude measurements.

<table>
<thead>
<tr>
<th>$Rps. \ viridris$</th>
<th>$Z^\pm/X^\pm$</th>
<th>$Z^\pm/Y_1^\pm$</th>
<th>$Z^\pm/Y_2^\pm$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Random</td>
<td>-1.6 ± .1</td>
<td>-5.8 ± 1.0</td>
<td>5.8 ± 1.0</td>
</tr>
<tr>
<td>Parallel</td>
<td>-1.2 ± .1</td>
<td>-4.1 ± .7</td>
<td>2.5 ± .3</td>
</tr>
<tr>
<td>Perpendicular</td>
<td>-1.7 ± .1</td>
<td>-9.6 ± 1.7</td>
<td>9.6 ± 1.7</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>$Rps. \ palustris$</th>
<th>$Z^\pm/X^\pm$</th>
<th>$Z^\pm/Y_1^\pm$</th>
<th>$Z^\pm/Y_2^\pm$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Random</td>
<td>-2.1 ± .1</td>
<td>-3.6 ± .3</td>
<td>4.2 ± .4</td>
</tr>
<tr>
<td>Parallel</td>
<td>-1.8 ± .2</td>
<td>-2.5 ± .2</td>
<td>2.5 ± .2</td>
</tr>
<tr>
<td>Perpendicular</td>
<td>-2.2 ± .1</td>
<td>-4.7 ± .5</td>
<td>6.1 ± .8</td>
</tr>
</tbody>
</table>
Zero-Field Splitting Parameters and Relative Rate Constants for Intersystem Crossing.

The $|D|$ and $|E|$ zero-field splitting parameters are given in cm$^{-1}$ units. $k_x$, $k_y$, and $k_z$ refer to rate constants for depopulation of the triplet spin sublevels associated with the $X^\pi$, $Y^\pi$ and $Z^\pi$ triplet peaks as defined in the Materials and Methods Section. The errors in the $|D|$ and $|E|$ values are calculated from the repeatability of the signal position determinations. The errors in the rate constants amount to no more than ±0.5 and arise from the range of acceptable $k$ values which fit the random spectrum.

|          | $|D|$                  | $|E|$                  | $k_x$:$k_y$:$k_z$ |
|----------|------------------------|------------------------|-------------------|
| *Rps. viridis* | 0.0153 ± 0.0002  | 0.0037 ± 0.0002  | 7.5:10.0:1.0    |
| *Rps. palustris* | 0.0183 ± 0.0002  | 0.0035 ± 0.0002  | 9.0:6.0:1.0    |
TABLE 3

Orientation Parameters for the Primary Donors in Photosynthetic Bacteria

\(X_n, Y_n, \text{ and } Z_n\) are the calculated projections of the \(x''\), \(y''\) and \(z''\) principal magnetic axes onto the normal to the membrane. \(1.7\Delta\) is the distribution width (in radians) of the "wobble" angle, \(w\). The values in parentheses are the angles between the normal to the membrane and the principal magnetic axes. They are related to the projections by \(\theta_X = \cos^{-1}X_n\), etc. The values were determined by the best fit of the theoretical spectra to the experimental ratios given in Table 1.

<table>
<thead>
<tr>
<th></th>
<th>(X_n)</th>
<th>(Y_n)</th>
<th>(Z_n)</th>
<th>(\Delta)</th>
</tr>
</thead>
<tbody>
<tr>
<td>(Rps. \text{ viridis})</td>
<td>0.67(48°)</td>
<td>0.74(42°)</td>
<td>0.10(84°)</td>
<td>0.40</td>
</tr>
<tr>
<td>(Rps. \text{ palustris})</td>
<td>0.69(46°)</td>
<td>0.69(46°)</td>
<td>0.25(76°)</td>
<td>0.60</td>
</tr>
</tbody>
</table>
### TABLE 4

Boundary Conditions for the Regions of Solution

The regions of solution are given by a rectangular parallelepiped, the dimensions of which are determined by \( X_n \) and \( Z_n \) which are the projections of the \( x" \) and \( z" \) magnetic axes onto the normal to the membrane, and \( \Delta \) which is the disorder parameter as defined in the text. No solution outside these regions fell within experimental error.

<table>
<thead>
<tr>
<th>Species</th>
<th>( 0.65 &lt; X_n &lt; 0.75 )</th>
<th>( 0.0 &lt; Z_n &lt; 0.15 )</th>
<th>( 0.3 &lt; \Delta &lt; 0.5 )</th>
</tr>
</thead>
<tbody>
<tr>
<td><em>Rps. viridis</em></td>
<td>( 0.5 &lt; X_n &lt; 0.7 )</td>
<td>( 0.0 &lt; Z_n &lt; 0.3 )</td>
<td>( 0.4 &lt; \Delta &lt; 0.8 )</td>
</tr>
</tbody>
</table>
FIGURE CAPTIONS

1) Axis system and symmetry operation definitions. x, y and z define the laboratory axis system; x', y' and z' the intermediate axis system; x", y" and z" the principal magnetic axis system. L is the long axis direction of the cell. χ, ν and λ are rotations about the indicated axes. \( H_A \) is the alignment field direction, and \( H_\parallel \) and \( H_\perp \) show the static EPR field directions used in the present experiments. Insert displays a section of the cylindrical membrane surface. The wobble angle, \( w \), is defined as the angle between the membrane normal, z', and the perfect cylinder normal, N, (i.e. N \perp L).

2) *Rhodopseudomonas viridis* experimental triplet state spectra.
   a) Spectra of randomly ordered, chemically reduced whole cells was taken with the following conditions: sweep time, 8 min; modulation frequency, 100 kHz; modulation amplitude, 16 Gauss; receiver gain, 32; temperature, 11°K; microwave power, 10 \text{uwatts}; microwave frequency, 9.077 GHz; light modulation frequency, 33.5 Hz; recorder time constant, 3 sec.
   b) Spectra taken with the static EPR field parallel to the alignment field. The other conditions are the same as a)
   c) Spectra taken with the static EPR field perpendicular to the alignment field. The other conditions are the same as a).
3) *Rhodopseudomonas palustris* experimental triplet state spectra.

   a) Spectra of randomly ordered, chemically reduced whole cells was taken with the following conditions:
sweep time, 8 min; modulation frequency, 100 kHz;
modulation amplitude, 16 Gauss; receiver gain, 63;
temperature, 110K; microwave power, 10 μwatts;
microwave frequency, 9.077 GHz; light modulation
frequency, 33.5 Hz; recorder time constant, 3 sec.

   b) Spectra taken with the static EPR field parallel to the alignment field. The other conditions are the same as a).

   c) Spectra taken with the static EPR field perpendicular to the alignment field. The other conditions are the same as a).

4) *Rhodopseudomonas viridis* computer simulated triplet state spectra assuming a) random, b) parallel and c) perpendicular orientations of the static EPR field direction with respect to the alignment field direction. Spectra are normalized to the $|Z^-| + |X^-|$ peak amplitudes.

5) *Rhodopseudomonas palustris* computer simulated triplet state spectra assuming a) random, b) parallel and c) perpendicular orientations of the static EPR field directions with respect to the alignment field direction. Spectra are normalized to the $|Z^-| + |X^-|$. 
6) *Rhodopseudomonas viridis* plots of theoretical amplitude ratio minus experimental amplitude ratio, $R_T - R_E$, versus the projection, $X_n$, of the $x''$ principal magnetic axes onto the normal to the membrane for $Z_n = 0.10$ and $\Delta = 0.40$.

7) *Rhodopseudomonas palustris* plots of theoretical amplitude ratio minus experimental amplitude ratio, $R_T - R_E$, versus the projection, $X_n$, of the $x''$ principal magnetic axes onto the normal to the membrane for $Z_n = 0.25$ and $\Delta = 0.60$.

8) *Rhodopseudomonas viridis* plots of theoretical minus experimental amplitude ratios versus the projection, $X_n$, of the $x''$ principal magnetic axes onto the normal to the membrane for a typical non-solution region (i.e. one lying outside the experimental error).

9) *Rhodopseudomonas palustris* plots of theoretical minus experimental amplitude ratios versus the projection, $X_n$, the $x''$ principal magnetic axes onto the normal to the membrane for a typical non-solution region (i.e. one lying outside the experimental error).

10) Orientation of the triplet magnetic axes of the primary donors in *Rhodopseudomonas viridis* and *Rhodopseudomonas palustris* with respect to the cylindrical membrane surface. $\theta_X$, $\theta_Y$, $\theta_Z$ and $\Delta$ are given in Table 3.
Rhodopseudomonas viridis

a) Random

b) Parallel

c) Perpendicular

Magnetic field strength (gauss)
Rhodopseudomonas palustris

(a) Random

(b) Parallel

(c) Perpendicular

Magnetic field strength (gauss)

XBL7810-4290
Rhodopseudomonas viridis

a) Random

b) Parallel

c) Perpendicular

Magnetic field strength (gauss)

Fig 4
Rhodopseudomonas palustris

a) Random

b) Parallel

c) Perpendicular

Magnetic field strength (gauss)
Rps. viridis
\[ \Delta = 0.4 \]
\[ Z_n = 0.1 \]
Rps. palustris

$\Delta = 0.6$

$Z_n = 0.25$

\[ \perp Z/y_2 \]

\[ \perp Z/y_1 \]

\[ \parallel Z/x_2 \]

\[ \parallel Z/x_1 \]

\[ \perp Z/x \]
Rps. viridis
\[ \Delta = 0.1 \]
\[ Z_n = 0.35 \]
Rps. palustris

$\Delta = 0.7$

$Z_n = 0.40$

$Z = 0.7$

$Z_n$
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