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Collision Energy Dependence of Moments of Net-Kaon Multiplicity Distributions at RHIC


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Fluctuations of conserved quantities such as baryon number, charge, and strangeness are sensitive to the correlation length of the hot and dense matter created in relativistic heavy-ion collisions and can be used to search for the QCD critical point. We report the first measurements of the moments of net-kaon multiplicity distributions in Au+Au collisions at $\sqrt{s_{NN}} = 7.7, 11.5, 14.5, 19.6, 27, 39, 62.4, \text{and} 200 \text{ GeV}$. The collision centrality and energy dependence of the mean ($M$), variance ($\sigma^2$), skewness ($S$), and kurtosis ($\kappa$) for net-kaon multiplicity distributions as well as the ratio $\sigma^2/M$ and the products $S\sigma$ and $\kappa\sigma^2$ are presented. Comparisons are made with Poisson and negative binomial baseline calculations as well as with UrQMD, a transport model (UrQMD) that does not include effects from the QCD critical point. Within current uncertainties, the net-kaon cumulant ratios appear to be monotonic as a function of collision energy.
I. INTRODUCTION

One primary goal of high energy heavy-ion collisions is to explore the phase structure of strongly interacting hot, dense nuclear matter. It can be displayed in the quantum chromodynamics (QCD) phase diagram, which is characterized by the temperature ($T$) and the baryon chemical potential ($\mu_B$). Lattice QCD calculations suggest that the phase transition between the hadronic phase and the quark-gluon plasma (QGP) phase at large $\mu_B$ and low $T$ is of the first order [1, 2], while in the low $\mu_B$ and high $T$ region, the phase transition is a smooth crossover [3].

The manuscript is organized as follows. In section II, we define the observables used in the analysis. In section III, we describe the STAR (Solenoidal Tracker At RHIC) experiment at BNL and the analysis techniques. In section IV, we present the experimental results for the moments of the net-kaon multiplicity distributions in Au+Au collisions at RHIC BES energies. A summary is given in section V.

II. OBSERVABLES

Distributions can be characterized by the moments $M$, $\sigma^2$, $S$, and $\kappa$ as well as in terms of cumulants $C_1$, $C_2$, $C_3$, and $C_4$ [36].

In the present analysis, we use $N$ to represent particle multiplicity in one event and $\Delta N_K (N_{K^+} - N_{K^-})$ the net-kaon number. The average value over the entire event ensemble is denoted by $\langle N \rangle$. Then the deviation of $N$ from its mean value can be written as $\delta N = N - \langle N \rangle$. The various order cumulants of event-by-event distributions of $N$ are defined as:

$$C_1 = \langle N \rangle$$
$$C_2 = \langle \delta N^2 \rangle$$
$$C_3 = \langle \delta N^3 \rangle$$
$$C_4 = \langle \delta N^4 \rangle - 3\langle \delta N^2 \rangle^2$$

The moments can be written in terms of the cumulants as:

$$M = C_1, \sigma^2 = C_2 - C_1, S = \frac{C_3}{(C_2)^{3/2}}, \kappa = \frac{C_4}{(C_2)^2}$$

In addition, the products of moments $\kappa \sigma^2$ and $S \sigma$ can be expressed in terms of cumulant ratios:

$$\kappa \sigma^2 = \frac{C_4}{C_2}, S \sigma = \frac{C_3}{C_2}$$

III. DATA ANALYSIS

The results presented in this paper are based on the data taken at STAR [37] for Au+Au collisions at $\sqrt{s_{NN}}$
and mass-squared (\(E\)) are used to identify \(K^+\) and \(K^-\). Combined with the path length (\(L\)) of a particle from the primary vertex of the collision. 

Combined with the path length (\(L\)) measured in the TPC, one can directly calculate the velocity (\(v\)) of the particles and their rest mass (\(m\)) using:

\[
\beta = \frac{v}{c} = \frac{L}{ct} \tag{8}
\]

\[
m^2c^2 = p^2 \left( \frac{1}{\beta^2} - 1 \right) = p^2 \left( \frac{c^2t^2}{L^2} - 1 \right) \tag{9}
\]

In this analysis, we use mass-squared cut \(0.15 < m^2 < 0.4 \text{ GeV}^2/c^4\) to select \(K^+\) and \(K^-\) within the \(p_T\) range \(0.4 < p_T < 1.6 \text{ GeV}/c\) to get high purity of kaon sample (better than 99%). For the \(p_T\) range \(0.2 < p_T < 0.4 \text{ GeV}/c\), we use only the TPC to identify \(K^+\) and \(K^-\).

The collision centrality is determined using the efficiency-uncorrected charged particle multiplicity excluding identified kaons within pseudorapidity \(|\eta| < 1.0\) measured with the TPC. This definition maximizes the number of particles used to determine the collision centrality and avoids self-correlations between the kaons used to calculate the moments and kaons in the reference multiplicity [41]. Using the distribution of this reference multiplicity along with the Glauber model [42] simulations, the collision centrality is determined. This reference multiplicity is similar in concept to the reference multiplicity used by STAR to study moments of net-proton distributions [29], where the reference multiplicity was calculated using all charged particles within

The STAR detector has a large uniform acceptance at midrapidity (\(|\eta| < 1\)) with excellent particle identification capabilities, i.e., allowing to identify kaons from other charged particles for \(0.2 < p_T < 1.6 \text{ GeV}/c\). Energy loss (\(dE/dx\)) in the time projection chamber (TPC) and mass-squared (\(m^2\)) from the time-of-flight detector (TOF) [39] are used to identify \(K^+\) and \(K^-\). 

To utilize the energy loss measured in the TPC, a quantity \(n\sigma_X\) is defined as:

\[
n\sigma_X = \frac{\ln[(dE/dx)_{\text{measured}}/(dE/dx)_{\text{theory}}]}{\sigma_X} \tag{7}
\]

where \((dE/dx)_{\text{measured}}\) is the ionization energy loss from TPC, and \((dE/dx)_{\text{theory}}\) is the Bethe-Bloch [40] expectation for the given particle type (e.g., \(\pi, K, p\)). \(\sigma_X\) is the \(dE/dx\) resolution of TPC. We select \(K^+\) and \(K^-\) particles by using a cut \(|n\sigma_{Kaon}| < 2\) within transverse momentum range \(0.2 < p_T < 1.6 \text{ GeV}/c\) and rapidity \(|y| < 0.5\). The TOF detector measures the time of flight (\(t\)) of a particle from the primary vertex of the collision. Combined with the path length (\(L\)) measured in the

\[\text{FIG. 1. (Color Online). Raw } \Delta N_K \text{ distributions in Au+Au collisions from } \sqrt{s_{NN}} = 7.7 \text{ to } 200 \text{ GeV for 0-5%, 30-40%, and 70-80% collision centralities at midrapidity. The distributions are not corrected for the finite centrality bin width effect nor the reconstruction efficiency.}\]
See that at the lower $p_T$ range (0.2 < $p_T$ < 0.4 GeV/c), kaons have a lower efficiency compared with the higher $p_T$ range (0.4 < $p_T$ < 1.6 GeV/c). The efficiencies increase monotonically with the centrality changing from most central (0 ∼ 5%) to peripheral (70 ∼ 80%). $K^+$ and $K^-$ have similar efficiencies.

By calculating the covariance between the various order factorial moments, one can obtain the statistical uncertainties for the efficiency corrected moments based on the error propagation derived from the Delta theorem [41, 45, 46]. The statistical uncertainties of various order cumulants and cumulant ratios strongly depend on the width ($\sigma$) of the measured multiplicity distributions as well as the efficiencies ($\varepsilon$). One can roughly estimate the statistical uncertainties of $S\sigma$ and $K\sigma^2$ as error($S\sigma$) $\propto \frac{1}{\sqrt{2\pi}}$ and error($K\sigma^2$) $\propto \frac{1}{\sigma^2}$. That explains why we observe larger statistical uncertainties for central than peripheral collisions, as on the width of the net-kaon distributions grows from peripheral to central. Furthermore, due to the smaller detection efficiency of kaons than the protons, we observe larger statistical uncertainties of cumulants and cumulant ratios than those of the net-proton fluctuations [29]. Systematic uncertainties are estimated by varying the following track quality cuts: distance of closest approach, the number of fit points used in track reconstruction, the $dE/dx$ selection criteria for identification, and additional 5% uncertainties in the reconstruction efficiency. The typical systematic

FIG. 2. (Color Online). Collision centrality dependence of the $p_T$-averaged efficiencies in Au+Au collisions. For the lower $p_T$ range (0.2 < $p_T$ < 0.4 GeV/c), only the TPC is used. For the higher $p_T$ range (0.4 < $p_T$ < 1.6 GeV/c), both the TPC and TOF are used for particle identification (PID).
FIG. 3. (Color Online). Collision centrality dependence of cumulants ($C_1$, $C_2$, $C_3$, and $C_4$) of $\Delta N_K$ distributions for Au+Au collisions at $\sqrt{s_{NN}} = 7.7 - 200$ GeV. The error bars are statistical uncertainties and the caps represent systematic uncertainties. The Poisson and NBD expectations are shown as dashed and blue solid lines, respectively.

FIG. 4. (Color Online). Collision centrality dependence of $M/\sigma^2$ for $\Delta N_K$ distributions in Au+Au collisions at $\sqrt{s_{NN}} = 7.7 - 200$ GeV. The Poisson expectations are shown as dashed lines.
FIG. 5. (Color Online). Collision centrality dependence of the $S\sigma$ for $\Delta N_K$ distributions from Au+Au collisions at $\sqrt{s_{NN}} = 7.7$ - 200 GeV. The error bars are statistical uncertainties and the caps represent systematic uncertainties. The Poisson (dashed line) and NBD (blue solid line) expectations are also shown.

FIG. 6. (Color Online). Collision centrality dependence of the $\kappa\sigma^2$ for $\Delta N_K$ distributions from Au+Au collisions at $\sqrt{s_{NN}} = 7.7$ - 200 GeV. The error bars are statistical uncertainties and the caps represent systematic uncertainties. The Poisson (dashed line) and NBD (blue solid line) expectations are also shown.
the volume of the system. This reflects the fact that the additivity property of the cumulants by increasing ear variation with general, the various order cumulants show a nearly linear relations centralities are represented by the average number of participating nucleons ($N_{\text{part}}$) = 7.7, 11.5, 14.5, 19.6, 27, 39, 62.4 and 200 GeV. The error bars are statistical uncertainties and the caps represent systematic uncertainties. The expectations from Poisson and NBD and the results of the UrQMD model calculations are all from the 0-5% centrality.

![Net Kaon Au+Au](image)

**FIG. 7.** (Color Online). Collision energy dependence of the values of $M/\sigma^2$, $S\sigma$, $\kappa\sigma^2$ for $\Delta N_K$ multiplicity distributions from 0-5% most central and 70-80% peripheral collisions in Au+Au collisions at $\sqrt{s_{\text{NN}}} = 7.7, 11.5, 14.5, 19.6, 27, 39, 62.4$ and 200 GeV. The error bars are statistical uncertainties and the caps represent systematic uncertainties. The expectations from Poisson and NBD and the results of the UrQMD model calculations are all from the 0-5% centrality.

uncertainties are of the order of 15% for $C_1$ and $C_2$, 21% for $C_3$, and 65% for $C_4$. The statistical and systematic (caps) errors are presented separately in the figures.

**IV. RESULTS**

Figure 3 shows the centrality dependence of cumulants ($C_1 - C_4$) of net-kaon ($\Delta N_K$) multiplicity distributions in Au+Au collisions at $\sqrt{s_{\text{NN}}}$=7.7-200 GeV. The collisions centralities are represented by the average number of participating nucleons ($\langle N_{\text{part}} \rangle$), which are obtained by Glauber model simulation. The efficiency corrections have been done using the values shown in Fig. 2. In general, the various order cumulants show a nearly linear variation with $\langle N_{\text{part}} \rangle$, which can be understood as the additivity property of the cumulants by increasing the volume of the system. This reflects the fact that the cumulants are extensive quantities that are proportional to the system volume. The decrease of the $C_1$ and $C_3$ values with increasing collision energy indicates that the ratio $K^+/K^-$ approaches unity for the higher collision energies. Figure 3 also shows the Poisson and negative binomial distribution (NBD) [47, 48] expectations. The Poisson baseline is constructed using the measured mean values of the multiplicity distributions of $K^+$ and $K^-$, while the NBD baseline is constructed using both means and variances. Assuming that the event-by-event multiplicities of $K^+$ and $K^-$ are independent random variables, the Poisson and NBD assumptions provide references for the moments of the net-kaon multiplicity distributions. Within uncertainties, the measured cumulants values of $C_3$ and $C_4$ are consistent with both the Poisson and NBD baselines for most centralities.

The collision energy dependence of the cumulant ratios for $\Delta N_K$ distributions in Au+Au collisions are presented in Fig. 7. The results are shown in two collision centrality bins, one corresponding to most central (0-5%) and the other to peripheral (70-80%) collisions. Expectations from the Poisson and NBD baselines are derived for central (0-5%) collisions. The values of $M/\sigma^2$ decrease as the collision energy increases, and are larger for central collisions compared with the peripheral collisions. For most central collisions, the Poisson baseline for $C_1/C_2$ slightly underestimates the data, indicating possible correlations between $K^+$ and $K^-$ production. For $C_3/C_2$ ($=S\sigma$) in Fig. 5, the Poisson and NBD expectations are observed to be lower than the measured $S\sigma$ values at low collision energies. The measured values for $C_4/C_2$ ($=\kappa\sigma^2$) in Fig. 6 are consistent with both the Poisson and NBD baselines within uncertainties.

The collision energy dependence of the cumulant ratios for $\Delta N_K$ distributions in Au+Au collisions are presented in Fig. 7. The results are shown in two collision centrality bins, one corresponding to most central (0-5%) and the other to peripheral (70-80%) collisions. Expectations from the Poisson and NBD baselines are derived for central (0-5%) collisions. The values of $M/\sigma^2$ decrease as the collision energy increases, and are larger for central collisions compared with the peripheral collisions. For most central collisions, the Poisson baseline for $C_1/C_2$ slightly underestimates the data. Within uncertainties, the values of $S\sigma$ and $\kappa\sigma^2$ are consistent with both the Poisson and NBD baselines in central collisions. The blue bands give the results from the UrQMD model calculations for central (0-5%) Au+Au collisions. The width of the bands represents the statistical uncertainties. The UrQMD calculations for $S\sigma$, and $\kappa\sigma^2$ are consistent with the measured values within uncertainties [49]. A QCD based model calculation suggests that, due to heavy mass of the strange-quark, the sensitivity of the net-kaon ($\Delta N_K$) fluctuations is less than that of the net-proton ($\Delta N_p$) [50]. A much high statistics dataset is needed for the search of the QCD critical point with strangeness.
V. SUMMARY

In heavy-ion collisions, fluctuations of conserved quantities, such as net-baryon, net-charge and net-strangeness numbers, are sensitive observables to search for the QCD critical point. Near the QCD critical point, those fluctuations are expected to have similar energy dependence behavior. Experimentally, the STAR experiment has published the energy dependence of the net-proton (proxy for net-baryon) [29] and net-charge [30] fluctuations in Au+Au collisions from the first phase of the beam energy scan at RHIC. In this paper, we present the first measurements of the moments of net-kaon (proxy for net-strangeness) multiplicity distributions in Au+Au collisions from $\sqrt{s_{NN}} = 7.7$ to 200 GeV. The measured $M/\sigma^2$ values decrease monotonically with increasing collision energy. The Poisson baseline for $C_1/C_2$ slightly underestimates the data. No significant collision centrality dependence is observed for both $S\sigma$ and $\kappa\sigma^2$ at all energies. For $C_3/C_2 (=S\sigma)$, the Poisson and NBD expectations are lower than the measured $S\sigma$ values at low collision energies. The measured values for $C_4/C_2 (=\kappa\sigma^2)$ are consistent with both the Poisson and NBD baselines within uncertainties. UrQMD calculations for $S\sigma$ and $\kappa\sigma^2$ are consistent with data for the most central 0-5% Au+Au collisions. Within current uncertainties, the net-kaon cumulant ratios appear to be monotonic as a function of collision energy. The moments of net-kaon multiplicity distributions presented here can be used to extract freeze-out conditions in heavy-ion collisions by comparing to Lattice QCD calculations. Future high precision measurements will be made for the net-kaon fluctuations in the second phase of the RHIC Beam Energy Scan during 2019-2020.

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[34] STAR Internal Note - SN0493, 2009.