Title
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Permalink
https://escholarship.org/uc/item/3q1199kz

Journal
Modern Physics Letters A, 29(11)

ISSN
0217-7323

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Publication Date
2014-04-10

DOI
10.1142/S0217732314300109

Peer reviewed
Nuclear theory and science of the facility for rare isotope beams

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The Facility for Rare Isotope Beams (FRIB) will be a world-leading laboratory for the study of nuclear structure, reactions and astrophysics. Experiments with intense beams of rare isotopes produced at FRIB will guide us toward a comprehensive description of nuclei, elucidate the origin of the elements in the cosmos, help provide an understanding of matter in neutron stars and establish the scientific foundation for innovative applications of nuclear science to society. FRIB will be essential for gaining access to key regions of the nuclear chart, where the measured nuclear properties will challenge established concepts, and highlight shortcomings and needed modifications to current theory. Conversely, nuclear theory will play a critical role in providing the intellectual framework for the science at FRIB, and will provide invaluable guidance to FRIB’s experimental programs. This review overviews the broad scope of the FRIB theory effort, which reaches beyond the traditional fields of nuclear structure and reactions, and nuclear astrophysics, to explore exciting interdisciplinary boundaries with other areas.

Keywords: Nuclear structure and reactions; nuclear astrophysics; fundamental interactions; high performance computing; rare isotopes; radioactive beams.

PACS Nos.: 21.60.-n, 21.30.-x, 21.65.-f, 24.10.-i, 24.80.+y, 25.60.-t, 26.30.-k, 26.50.+x, 26.60.-c

1. Introduction: New Opportunities with FRIB

Nuclear physics plays a key role in our quest to understand the Universe. In recent years, researchers have made remarkable progress in our fundamental understanding of the complex and fascinating system, that is the nucleus. This progress has been driven by new theoretical insights and increased computational power, as well as by experimental access to new isotopes with a large excess of neutrons or protons. However, while much has been learned so far about nuclear systems and associated phenomena, much remains to be understood.

The Facility for Rare Isotope Beams (FRIB), which is a sponsored project of the US Department of Energy, Office of Science, will push the frontiers of nuclear science by providing access to the widest range of isotopes possible. For example, to explore changes in shell structure, useful yields of nickel isotopes will be available from $^{48}$Ni to $^{84}$Ni, thereby spanning the full range of neutrons in the pfg-shells. The key is for the facility to deliver very high power heavy-ion primary beams, 400 kW
Fig. 1. (color online) Number of isotopes of elements up to $Z = 92$ estimated to be produced in sufficient quantities at FRIB (green bars) to allow study of their structure and determine at least one other property other than simple observation. The number of isotopes estimated to exist (blue bars) is taken from the recent theoretical survey of Ref. 11. FRIB is predicted to produce nearly 80% of all possible isotopes in this range.

minimum, at energies of at least 200 MeV/u to be used in the production of rare isotopes. These high-power beams will be generated by a superconducting linear accelerator coupled with a production area designed to operate at high current. The broad scientific program requires rare-isotope beams at energies ranging from stopped ions in traps to ions at relativistic energies of hundreds of MeV/u. FRIB will have these capabilities by using full-energy beams following in-flight separation, stopped ions thermalized using a variety of ion catcher schemes, and reaccelerated ions delivered by the reaccelerator (ReA) superconducting linear post-accelerator. The goal is to reach reaccelerated beam energies of 12–20 MeV/u. As a result, the full complement of direct reactions (including high-$\ell$ transfer and deep-inelastic reactions) will be accessible for experimentation. An advantage of the in-flight production and reacceleration approach is that isotopes of all elements will normally be available with very short development times and high efficiency (approaching 10% to 20%). The technique will also provide beams of most isotopes, even those with short (tens of ms) half-lives. This offers the possibility to perform experiments, for example, with beams of highly refractory elements along the $N = 126$ line of isotones below $^{208}$Pb, as required to improve $r$-process nucleosynthesis models.

The anticipated range of isotopes to be available at FRIB, as estimated using the LISE++ program, is shown in Fig. 1. It is compared to the predicted number of possible isotopes from the average of Density Functional Theory (DFT) predictions. With the 400 kW beams of FRIB, nearly 80% of all isotopes of elements up to uranium may become available for the study. This includes many new isotopes estimated to lie along the drip lines (perhaps even up to element $Z = 61$ as shown in the figure) and many nuclei with skins predicted to be greater than 0.5 fm (cf. Ref. 13). In addition, the facility will have provisions to collect unused isotopes and make them available for experiments and applications in other fields, such as medicine. One option being considered is to collect isotopes produced in the beam dump by uranium stopping in water. This approach would, for example, make...
nearly continuous supplies of $^{223}\text{Rn}$ or $^{225}\text{Ra}$ available for fundamental interaction studies searching for an atomic electric dipole moment (EDM).\textsuperscript{15} Other options are to provide a source of isotopes such as $^{67}\text{Cu}$ or $^{149}\text{Tb}$ for medical studies.\textsuperscript{14}

In this broad overview of FRIB theory, we concentrate on major themes pertaining to science, organization and education aspects of the effort. The references and links cited are not meant to be inclusive; they should rather be used as sources to further in-depth information. This paper is organized as follows. Section 2 summaries the science case for FRIB, in the context of the overarching science questions. The interdisciplinary aspects of the FRIB program are presented in Sec. 3. Section 4 discusses various ways of enhancing the coupling between experiment and theory. High-performance computing will play a key role in FRIB science program; this is discussed in Sec. 5. Sections 6 and 7 talk about organization of the FRIB theory community and educational aspects, respectively. Finally, Sec. 8 offers a broad perspective on FRIB theory.

\section{FRIB Science Overview}

The science case for FRIB has been formulated over many years and is well-documented.\textsuperscript{1,2,4} In short, the facility will address — on many levels — the overarching science questions identified by the US National Academy of Science in the fourth decadal survey of nuclear physics entitled \textit{Exploring the Heart of Matter}:\textsuperscript{1} (1) \textit{How did matter come into being and how does it evolve?} (2) \textit{How does subatomic matter organize itself and what phenomena emerge?} (3) \textit{Are the fundamental interactions that are basic to the structure of matter fully understood?}, and (4) \textit{How can the knowledge and technological progress provided by nuclear physics best be used to benefit society?} Together with experiment, future developments in low-energy nuclear theory and computational science will be critical in answering these questions.

\subsection{The origin of the elements}

Our radioactive galaxy demonstrates continuing formation of new short-lived elements by nuclear reaction sequences (see Fig. 2 and Refs. 16 and 19). Nuclear structure helps dictate galactic chemical evolution. One example is the neutron driven $s$- and $r$-processes, responsible for building heavy elements. The resulting final abundances of these processes reflect nuclear shell structure, which gives rise to the respective nucleosynthesis paths. Another example concerns the $rp$-process, which provides a sensitive probe for neutron star surfaces and crusts. To this day, we do not know exactly where the heavy elements were made. Possible $r$-process sites include supernovae and neutron star mergers. Differences in reaction paths, which depend on the masses and lifetimes of the nuclei involved, could affect abundance signatures for each site. Theory is a key component to resolve this mystery. Indeed, nuclear models provide a structural input for key nuclei that participate in reaction networks but are not accessible to experiment, and large scale computational
simulations — such as those shown in Fig. 2, bottom — tell us about astrophysical conditions at possible sites.

The theory roadmap includes deriving nuclear interactions from quantum chromodynamics (QCD) and connecting those to the structure of the lightest elements and Big Bang nucleosynthesis (BBN). The combined effort of new experiments and theoretical/computational approaches will enable us to accurately determine all relevant properties and reactions of light nuclei, in particular neutron-rich nuclei formed during stellar evolution. Interactions obtained from effective theories of QCD, DFTs, experiments and astrophysical observations will describe the properties of nucleonic matter found in nature: the nuclear landscape, neutron stars and supernovae.

While great progress has been made in the last decade in the theoretical description of nuclear structure by \textit{ab initio} methods, CI approaches, and nuclear DFT, the exploration of neutron-rich systems is still in its infancy. Figure 3 provides theory predictions for the neutron-rich calcium isotopes, which are a frontier for probing nuclear forces and shell structure. Predictions for masses (by way of two-neutron separation energies) show good agreement for measured nuclei, but diverge where not yet constrained by experiment.\cite{14,15} This divergence is especially evident for the $2^+_1$ excitation energies.\cite{22} The interplay between theory and experiment at FRIB will lead to a robust phenomenology with controlled and quantitative uncertainties for the theory predictions of unmeasured nuclei, see Sec. 4 for more discussion.

\subsection*{2.2. Organization of sub-atomic matter}

The nature of nuclear forces and the mechanism of nuclear binding produce amazingly regular patterns in nuclei. Theory provides the framework to understand the emergence of these collective phenomena.
Finite nuclei exhibit phase-transitional behavior, critical points as a function of particle number, spin and temperature. To understand what causes the emergent phenomena in atomic nuclei, we need predictive models of small- and large-amplitude collective motion, such as those involved in fission and heavy-ion fusion. The atomic nucleus is an open quantum system; hence, phenomena of nuclear structure are intimately connected to reactions, and both should be described in a unified way. There are challenges in achieving this unified description: the inclusion of the particle(s) continuum and its impact on properties of weakly bound states (such as halos) and unbound nuclear states, and understanding the role of reaction thresholds on the appearance of collective cluster states.

Extended nucleonic matter is another avenue to understand emergent phenomena. Only with theory can we explore the connection between neutron-rich matter in the Cosmos and in the laboratory. Figure 4 illustrates the multi-disciplinary nature of this quest. Answers to many challenging scientific questions ranging from the dynamics of supernova and HIC to the structure of neutron stars and rare isotopes, all depend critically on the Equation of State (EOS) of neutron-rich nucleonic matter. Figure 4 demonstrates that the isospin-asymmetric part of the EOS, namely the density dependence of nuclear symmetry energy, is still not fully understood. As seen in Fig. 4(a), while significant effort has been devoted to constraining the symmetry energy parameters around the saturation density from the data obtained in terrestrial laboratories, astrophysical observations and nuclear theory, large uncertainties still remain. Of particular importance is the determination of the symmetry energy at supra-saturation densities.

Figure 4(b) (from Ref. 25) displays the mass–radius relation for a neutron star as predicted by various theoretical models. The typical mass of a neutron star is about 1.4 solar masses, and the typical radius is thought to be about 12 km. One of the main science drivers of FRIB is the study of nuclei with neutron skins three or four times thicker than is currently possible. Studies of neutron skins in heavy nuclei
Fig. 4. (color online) Left: Summary of constraints on symmetry energy parameters. The experimental constraints from nuclear data (masses, neutron skin thicknesses, dipole polarizability of $^{208}$Pb, giant dipole resonances (GDR) and isotope diffusion in heavy-ion collisions (HIC) are marked. The hatched rectangle shows constraints from fitting astrophysical observations. The two closed regions show neutron matter constraints. The enclosed white area is the experimentally allowed overlap region. Right: Predicted relation between mass and radius of a neutron star modeled with forces involving two nucleons (NN) and forces also involving three nucleons (NN + NNN). The three-nucleon forces are both essential and poorly known, as indicated by a dark blue uncertainty band. The orange lines roughly indicate the predicted central density of the neutron star. The black dots mark the predicted values of the neutron skin in $^{208}$Pb. The accurate measurement of a large neutron star mass $M = 1.97(4) M_{\text{solar}}$ provides a strong constraint on theoretical models.

and investigations of high-frequency nuclear oscillations and intermediate energy nuclear reactions with a range of proton and neutron-rich nuclei will help pin down the behavior of nuclear matter at densities below twice the typical nuclear density $\rho_0$. At higher densities, relativity and the observations of a nearly two-solar-mass neutron stars place severe constraints on the relationship between the pressure and density of nuclear matter.

2.3. Fundamental symmetries

Experimental tests of the Standard Model using the nucleus as a laboratory include: searches of atomic EDMs in rare isotopes; parity violation tests in Fr; Cabibbo-Kobayashi-Maskawa (CKM) matrix unitarity tests by superallowed $\beta$ decay measurements in $N \approx Z$ nuclei; and searches of exotic scalar and tensor couplings in $\beta$ decay.

Here, again, theory and experiment go hand in hand. A variety of nuclear-structure calculations are critical to tests of the Standard Model. These include the isospin-mixing corrections in superallowed $\beta$ decays; nuclear anapole moments in parity violation; Schiff moments for atomic EDM searches; ordinary and neutrinoless double-$\beta$ decay matrix elements. These theoretical predictions are typically needed with high accuracy and quantified uncertainties. In addition, new weak interaction signatures need to be explored to probe astrophysical environments. For example, neutrino signatures probe the burning conditions and chemistry of...
the solar core and define the physics of core-collapse supernovae. Electron capture in neutron star crusts affects neutron star cooling. These studies rely strongly on theoretical predictions.

2.4. Nuclear theory and society

Last but not least, nuclear physics can and should be used for the benefit of society. The theory roadmap includes theoretical advancements relevant for medical applications and for stockpile stewardship. Examples are an ab initio theory for light-ion fusion, a microscopic theory of spontaneous and neutron-induced fission and reaction theory for medium and heavy nuclei.

Similar to astrophysics, an important stockpile stewardship application involves a complex network of neutron-induced reactions on unstable nuclei that cannot be accessed directly in the laboratory, due to the short lifetime of the targets. On the other hand, an indirect approach leading to the same compound nucleus as the desired reaction, such as $(d, p)$, which may be performed in inverse kinematics with radioactive beams at FRIB, can provide important guidance to infer the reaction of interest. However, since this “surrogate” reaction may populate slightly different angular momenta and parities in the entrance channel, a robust theory for nuclear reactions is needed in order to properly infer the results for the desired reaction.

Progress made in the understanding of nuclear reactions within an ab initio framework can provide important information to understand fusion reactions in both astrophysical and terrestrial environments. A recent example concerns uncertainties in the differential cross-section for elastic $n$-$^3$H scattering, which need to be of the order 5% to reliably infer a fuel density for inertially confined fusion experiments. Theoretical calculations based on a reaction theory using the ab initio, no-core shell model and the resonating group method were able to achieve this accuracy and compare well with data extracted from later experiments. Similar calculations have recently yielded first-principles results for the $d(^3$H, $n$)$^4$He fusion reaction.

3. Interdisciplinary Aspects of the FRIB Scientific Program

Physics with exotic nuclei has intimate connections to many research areas outside nuclear structure, reactions and nuclear astrophysics, see Ref. 35 and Sec. 5 of Ref. 3. Figure 5 illustrates some of these intersections and the shared fundamental questions that tie them together.

A particularly profound synergy exists between research in FRIB physics and research in astrophysics and cosmology. This synergy also ties into neutrino physics. The near future will see 30-m class optical telescopes and a myriad of new observational probes of the cosmos, from measurements of polarization in the cosmic microwave background (CMB), to 21-cm probes of high redshift ($z \sim 10–100$), to new X-ray (e.g. NuStar) and Gamma-ray (e.g. Fermi) observatories. Nuclear
How do collective phenomena emerge from simple constituents?

How can complex systems display astonishing simplicities?

What are unique properties of open systems?

How do nuclei shape the physical universe?

What is the origin of the elements?

Fig. 5. There are diverse intersections of FRIB science with research in other sub-fields of physics, with shared fundamental questions.

physics, nuclear astrophysics and neutrino physics will be a key in unraveling what the new data may mean.

As already emphasized, understanding the origin of the elements around us is one of the quests of modern science. The answer lies in understanding the synthesis history of the elements in the universe, and how this evolution gives us insight into the origin and evolution of the structures we see, and the nature of dark matter and dark energy. New data on the history of nucleosynthesis from a quite high redshift to the present epoch will present nuclear astrophysicists with exciting opportunities. At issue is whether the history of nucleosynthesis and star formation is consistent with the picture we have for the mass assembly history of galaxies. Insight into this issue may be a key to understanding, for example, the origin and evolution of the dwarf spheroidal galaxies which, in turn, may give insights into the nature of dark matter.\textsuperscript{36}

CMB observations have given us, or will give us, precise determinations of the baryon density of the universe and the ratio of relativistic to non-relativistic energy density at the epoch of photon decoupling. These, combined with increasingly precise determinations of the primordial deuterium and helium abundances, are creating a nearly over-determined situation for BBN. This turns BBN into an even more powerful probe of the physics of the early universe, particularly of new physics in the neutrino sector, and potentially the QCD epoch. However, there are many open questions involving the synthesis of $^7\text{Be}$ and $^7\text{Li}$ in BBN (with new physics) and the subsequent fate of these species in stars. These are central problems in nuclear astrophysics.\textsuperscript{37}

A quantitative understanding of stellar evolution, stellar explosions and the compact objects they produce, relies on nuclear physics. In the past decade, advances in theory, computation and simulation have helped to interpret diverse astrophysical
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phenomena, unravelling how nuclear physics input shapes observable outcomes. Input from experimental nuclear and neutrino physics has played an important role, but theory is essential to access the enormous range of ambient conditions realized in astrophysics. The nuclear and weak reactions, the EOS and transport properties of hot and dense matter, which play a central role in the most extreme conditions, are seldom within reach of direct experiments. A quantitative theory of nuclei and nuclear matter with quantifiable errors and well-understood model systematics can unravel mechanisms that power supernova, gamma-ray bursts, X-ray bursts and neutron star mergers and provide fundamental tests of nuclear physics under extreme conditions. For example, the density dependence of the nuclear symmetry energy influences the spectrum and the time structure of the supernova neutrino signal\cite{38}–\cite{40} and the gravitational wave signal from binary neutron star mergers.\cite{41}

The properties of the neutron star crust, where neutron-rich nuclei and matter at subnuclear density both play a role, are helping to interpret a host of X-ray phenomena associated with accreting neutron stars, and in some cases, permitting us to develop a quantitative theory to predict thermal evolution on timescales of years\cite{42} and motivating a slew of new observations.

There are also numerous profound connections between FRIB science and many-body physics. Despite the fact that the number of nucleons in heavy nuclei is small compared to the number of electrons in solids or atoms in gases, nuclei exhibit emergent phenomena that are present in other complex systems studied by quantum chemists, atomic, molecular and condensed-matter physicists, and materials scientists. Atomic nuclei exhibit both fundamental and emergent behavior; hence, they provide important clues to our understanding of the transition from microscopic to mesoscopic, and to macroscopic.

One example of fruitful interdisciplinary research that bridges between nano- and femto-scales is the physics of strongly coupled superfluid systems, such as neutron droplets and cold atoms close to the unitary regime: both have been successfully treated by many-body nuclear techniques.\cite{43}–\cite{45} Another example is Cooper pairing. Nucleonic superfluidity lies at the heart of nuclear physics: it is present in finite nuclei and in the nuclear matter of neutron stars, where spatially anisotropic pairing fields, also discussed in the context of high-temperature superconductivity in novel materials, are expected. Theoretical concepts and tools are shared between the fields. For example techniques developed in nuclear structure physics, such as the random matrix theory\cite{47}–\cite{48} and semiclassical methods\cite{49} have been carried over to the study of mesoscopic systems such as quantum dots and clusters of atoms.

One of the main goals of many-body physics that is shared with nuclear physics is to understand how collective phenomena emerge from simple constituents. We know that complex systems can display astonishing simplicities associated with dynamical many-body symmetries, symmetry breaking effects, and quantum phase transitions, and the atomic nucleus shows many examples of collective behavior. The many-body behavior of neutrinos in a core-collapse supernova, the only many-
body system driven by weak interactions, reveals an intriguing connection between neutrinos, emergent properties in many-body physics and nucleosynthesis.

Open quantum systems, whose properties are affected by the environment of decay, scattering and reaction channels, are also great interdisciplinary unifiers. Many aspects of open quantum systems that are independent of the system dimensionality are now explored in atomic nuclei, hadrons, molecules, quantum dots and wires and other solid-state microdevices, crystals in laser fields and microwave cavities. As radioactive nuclear beam experimentation extends the known nuclear landscape towards the particle drip lines, the coupling to the continuum space becomes increasingly more important. The novel nuclear approaches developed in this context, such as the continuum shell model, are now being applied to studies of other open quantum systems, such as coupled quantum dots or dipole-bound anions.

4. Enhancing the Feedback Between Experiment and Theory

The scientific method uses experimentation to assess theoretical predictions. Based on experimental data, the theory is modified and subsequently can be used to guide future measurements. The process is then repeated, until the theory is able to explain observations, and experiment is consistent with theoretical predictions. This positive feedback in the “experiment-theory-experiment-” loop can be enhanced, if statistical methods and scientific computing are applied to determine the couplings between model parameters, parameter uncertainties and the errors of calculated observables.

Nuclei communicate with us through observables revealed by experiment. Some observables are easy to measure; some take considerable effort and experimental ingenuity. Often, the observable, such as the cross-section for a certain nuclear reaction channel, can be used to deduce a quantity of interest, like the distribution of neutron matter in the nucleus or the resonance width. A challenge for FRIB science is that in most cases the extraction of structural data will be model dependent. The reliability of the extracted information will depend critically on the ability of theory to accurately describe those reaction processes. Microscopic approaches to reaction theory consistent with the state-of-the-art structure models are necessary to reduce the ambiguity of current highly phenomenological models. Statistical tools will be useful in providing uncertainty quantification. A number of new approaches are being developed for this purpose, but many challenges remain.

With nearly 7000 possible isotopes and thousands of pieces of information for each one, not every observable has the potential to impact our understanding in the same way: some measurements will be more important than others. Identification of the key measurements is one way in which theory can provide the foundation for an optimized experimental program at FRIB. By studying the theoretical relevance of the anticipated experimental outcomes, a theoretical assessment of the scientific impact of experiments will help identify critical measurements. However, we also
Fig. 6. Calculated and experimental two-neutron separation energies of even–even zirconium isotopes. Calculations performed in Ref. 11 using SLy4, SV-min, UNEDF0 and UNEDF1 energy density functionals are compared to experiment FRDM53 and HFB-2154 mass models. The differences between model predictions are small in the region, where data (marked by squares) exist and grow steadily when extrapolating towards the two-neutron drip line ($S_{2n} = 0$). The bars on the SV-min results indicate statistical errors due to uncertainty in the coupling constants of the functional. Detailed predictions around $S_{2n} = 0$ are illustrated in the inset.

recognize that as with any new facility, surprises not anticipated by current theory are likely to arise. Theory working hand-in-hand with experiment will be a key to unravel the puzzles. Past examples of this interplay are the unexpected evolution of shell structure with $N$ and $Z$, and the existence of nuclei with large neutron halos and skins. Often these surprises have provided crucial clues for new physics that was missing from our models.

Theory can also evaluate whether the anticipated experimental errors are adequate to provide meaningful guidance for further model developments. Theory should provide input for planning future experiments by isolating those experimental data crucial to better constrain nuclear models and validating and verifying model-based extrapolations.13,52 An FRIB theory effort, working closely with the experimentalists associated with FRIB, will serve as a focal point for facilitating interactions aimed at enhancing the experiment-theory cycle in the scientific method.

By taking advantage of high-performance computing, nuclear theory is developing tools to deliver uncertainty quantification and error analysis for theoretical studies. Statistical tools can also be used to assess the information content of an observable with respect to current theoretical models. Such technologies are essential for providing predictive capability, to estimate uncertainties, and to assess extrapolations — as theoretical models are often applied to entirely new nuclear systems and conditions that are not accessible to experiment. As already discussed in Fig. 3, current nuclear models do not give consistent answers when going outside “safe” regions explored experimentally. Figure 6 illustrates the difficulties encountered with theoretical extrapolations towards the drip lines. Shown are the two-neutron separation energies $S_{2n}$ for the isotopic chain of even–even zirconium isotopes pre-
dicted with different theoretical models. In the region for which experimental data are available, all models agree and reproduce the data equally well. However, the discrepancy between various predictions steadily grows when moving away from the region of known nuclei, because the dependence of the effective force on the neutron excess is poorly determined. In the example considered, the neutron drip line is predicted to be between $N = 84$ (FRDM and SLy4) and $N = 96$ (UNEDF0), i.e. the model (systematic) error is appreciable. In addition to systematic errors, calculated observables are also subject to statistical errors due to uncertainties in model parameters. Figure 6 indicates that the statistical error predicted with the SV-min energy density functional gradually grows with $N$. This is primarily caused by the isovector properties of the model that are not well-constrained by the current data. For other examples, see Refs. 13, 52, 58 and 59. Experimentally, FRIB with its extended reach has the possibility to produce $^{124}Zr$ and determine its two-neutron separation energy. The figure illustrates that, with the theoretical understanding of the origin of model uncertainties coupled with the new data, a significant improvement in the precision of nuclear models will be possible.

5. High Performance Computing Aspects of FRIB Science

As eloquently stated in the recent decadal survey,¹ "High-performance computing provides answers to questions that neither experiment nor analytic theory can address; hence, it becomes a third leg supporting the field of nuclear physics." Large-scale nuclear physics computations dramatically increase our understanding of nuclear structure and reactions and the properties of nucleonic matter. A series of workshops on computational physics and forefront areas of nuclear science,⁶⁰ including QCD, nuclear structure and reactions and nuclear astrophysics, established the importance and breadth of computational nuclear physics. A large fraction of the discussion revolved around topics critical to FRIB science. The importance of computational nuclear physics has been re-emphasized recently in influential reports.¹ ² Reaching the full potential of the FRIB research program requires comprehensive investigations of many questions that can only be addressed using world-leading computational facilities.

Computational nuclear structure and reactions in the US has advanced significantly through the UNEDF⁶¹–⁶³ SciDAC project and its successor NUCLEI.⁶⁴ Both projects joined forces of nuclear theorists, computer scientists and applied mathematicians to break analytic, algorithmic and computational barriers in low-energy nuclear theory. Integral to both projects has been the greatly enhanced degree of quality control: verification of methods and codes, the estimation of uncertainties and assessment. The UNEDF project helped to form a coherent nuclear theory community, opened up new capabilities, fostered transformative science resulting in high-visibility publications and advanced the careers of many junior scientists. The NUCLEI project encompasses significant components of computational physics relevant to FRIB science; it bridges the scales from hadronic interactions...
to the structure and dynamics of heavy nuclei to neutron stars within a coherent framework. Figure 7 shows the structure of this project and its ties to applied mathematics and computer science.

The mathematics and computer science components in NUCLEI are directly tied to relevant parts of the NUCLEI project. These groups do forefront research in applied math and computer science that will be both broadly applicable across different fields of science and immediately beneficial to the physics projects in NUCLEI. Examples of joint projects include: development of the Asynchronous Dynamic Load Balancing (ADLB) library, which provides scalable load balancing services for Quantum Monte Carlo calculations on the largest machines available; new schemes for sparse matrix-vector operations and development of efficient scalable iterative eigensolvers for distributed multi-core platforms and topology-aware mapping of computational tasks to reduce communication overhead employed in state-of-the-art CI calculations; applications of the wavelet-based Multiresolution Adaptive Numerical Environment for Scientific Simulations (MADNESS) to nuclear DFT; derivative-free multi-parameter optimizations of chiral interactions and energy density functionals with Practical Optimization Using No DERivatives (POUNDERS) framework; and uncertainty quantification using the Gaussian Process Models for Simulation Analysis tool, which is important in many applications from nuclear interaction input to the significance of predictions to upcoming experiments.

Many scientific advances in the field were made possible by a rapid increase in our ability to use the largest-scale computational resources. The usage of high-
FRIB nuclear theory

performance computers in nuclear structure and reactions in the US rose from 80 M core-hr/year in 2009 to 320 M core-hr/year in 2013. In the future, our ability to use the largest-scale computers will require additional investments in manpower, particularly as we transition to new architectures. These new positions are critical to enable the effort to scale to the most powerful computers heading toward exascale, and to support the FRIB-related experimental programs in a timely manner.

There are also deep connections between NUCLEI and computational efforts in neighboring areas. At the shortest scales, lattice gauge theory plays an important role, particularly for aspects such as the three-neutron force that are difficult to isolate, and often access, experimentally. These can play a very important role in neutron-rich nuclei and matter. Simulations of neutron star structure and explosive events on neutron stars and neutron star mergers will yield critical information about dense matter, as described in Sec. 2. Supernovae simulations encompass important studies of radiation hydrodynamics that illuminate the explosion mechanism and nucleosynthesis, the associated studies of neutrino propagation can tell us more about the astrophysics of supernovae, as well as neutrino properties. Examples of such simulations are displayed in Fig. 2. Each of the research areas displayed in Figs. 1–4 and 6 require state-of-the-art computational facilities and teams of physicists, computer scientists and applied mathematicians working together to advance our understanding and to fully exploit the capabilities of FRIB.

6. FRIB Theoretical Science Organization

The current nuclear theory effort in the US related to FRIB is quite broad and dispersed, with large groups at National Laboratories and some universities, but also many small university groups. There are theorists studying astrophysical phenomena, nuclear reactions, nuclear equations of state, nuclear structure and nuclear applications in national security and isotope R&D. Some function largely independently, while others collaborate in large research projects such as the NUCLEI effort discussed in Sec. 5 or topical collaborations in nuclear theory on neutrinos and nucleosynthesis in hot and dense matter and reactions for unstable isotopes.

The theory community interested in FRIB physics formed, over a decade ago, the “Rare Isotope Accelerator” (RIA) and FRIB theory users groups, whose primary purpose is to identify and prioritize the most important theory developments in relation to RIA and FRIB projects, to advocate for the science of radioactive beams, and to be a voice for the low-energy nuclear theory and astrophysics community. The members of the FRIB Theory Users Group regularly join the annual low-energy nuclear physics community meetings. During the last ten years, the theory community has produced two important documents: the RIA Theory Bluebook (2005) and an FRIB Theory Users Group Report (2011). The former report outlined various scientific directions necessary for an impactful theory effort, while the latter focused on issues surrounding education and training of the next generation of theorists, and included results from a survey on the needs of the field. While
To address the concerns discussed in the 2011 report, the pipeline of young theorists must be maintained. In particular, post-doctoral appointments are crucial for R&D career development. A national FRIB Theory Fellow program would address the problem, creating opportunities for young post-doctoral fellows to mature and fostering continuous interactions among theorists and experimentalists. The need for faculty or laboratory positions in nuclear theory has also been noted in the past, and was the second concern documented in Ref. 68. To overcome this problem, a bridging program for young faculty could be developed enabling needed growth into areas of critical need.

The nuclear theory community in the US has also extended beyond its boundaries. The report from a recent comparative research review of nuclear physics for the US Department of Energy\cite{new设施正在建设} states: “New RIB facilities are under construction in Canada, France and Asia. With the wider spread of world-leading experimental facilities, international networking will become more important in the future. As a first step, DOE has created exchange programs for nuclear theorists with selected countries. These programs should be expanded and include joint graduate education with international partners.” There are a number of initiatives already in place that foment collaborations between countries, namely JUSTIPEN,\cite{ JUSTIPEN} FUSTIPEN,\cite{ FUSTIPEN} and CUSTIPEN,\cite{ CUSTIPEN} which are theory exchange programs. In addition, International Collaborations in Nuclear Theory\cite{ 国际合作协调} coordinates theory topical programs between NSCL/FRIB, GSI and RIKEN, to address theoretical issues relevant to those laboratories. Finally, the Training in Advanced Low-Energy Nuclear Theory (TALENT)\cite{ TALENT} initiative in graduate education, discussed in Sec. 7 below, has also spurted from an international framework.

7. Education Challenges

The theory effort around FRIB will also play an important role in the development of a broad, modern and attractive educational curriculum addressing the nuclear many-body problem and related areas. A thorough knowledge of up-to-date theoretical methods and phenomenology will be required to tackle the theoretical and experimental challenges that will be faced by the next generation of nuclear physicists working in FRIB science. However, most university low-energy nuclear theory groups are small and, therefore, unable to offer a broad spectrum of advanced research-based nuclear physics courses. Fortunately, with advances in modern educational and computational tools, we are in a situation where globally coordinated efforts can make a significant qualitative difference in the way nuclear physics students are educated.

Recently, nuclear physicists in North America and Europe have teamed up to launch an educational initiative dubbed Nuclear TALENT (Training in Advanced Low-Energy Nuclear Theory).\cite{ TALENT} The long-term vision of TALENT is to develop a coherent graduate curriculum that will provide the foundations for a cross-cutting
low-energy nuclear theory research program, and will link modern theoretical approaches with on-going experimental efforts. To meet these objectives, educational modules are being commissioned from the best teachers and specialists in low-energy nuclear theory. The resulting unique material is being collected in the form of web-based courses, books and other educational resources. The development of such a knowledge base will allow highly specialized university groups to benefit greatly from a broad selection of topics taught by world-leading experts.

In its initial phase, TALENT has selected several topics in low-energy nuclear physics for teaching modules. The range of courses is broad, from nuclear forces and \textit{ab initio} approaches, to the theory of complex nuclei, to nuclear reactions and open quantum systems, to nuclear astrophysics, to computational tools for nuclear physics. Some of the topics have already been taught as intensive three-week courses hosted by the European Centre for Theoretical Studies in Nuclear Physics and Related Areas in Trento, the National Institute for Nuclear Theory in Seattle and GANIL in Caen. Other courses are in the pipeline, including one at the Joint Institute for Nuclear Astrophysics.

One of the major challenges facing TALENT is to develop a robust model for funding. To this point, all courses have been run on a voluntary basis, with financial support for students (lodging and local expenses) provided by the hosting institutions. Obviously, to put this educational initiative on solid ground, sustainable funding is needed. In addition, a proper model for transferring academic credit must be developed. There exist examples of educational collaborations between various universities in the US where bilateral agreements have been developed between various colleges of natural science, enabling an economically sustainable model for credit transfers. With such bilateral agreements, TALENT courses can be included in course curricula of participating institutions, and teaching duties could also be transferred. With an FRIB theory center on the horizon, there are good prospects for a better coordination of educational efforts in advanced theory of nuclei and nucleonic matter. While the current TALENT effort is built around theoretical and experimental activities in North America and Europe, its expansion into other regions is envisioned. In particular, considering the scale of experimental efforts in rare-isotope science in Japan and China, it is anticipated and hoped that Asia will soon join the initiative.

8. Summary

An understanding of the properties of atomic nuclei and their reactions is essential for a complete description of nuclei, an explanation of element formation and the properties of stars, and for present and future energy, defense and security applications. This requires a coherent picture across many energy scales, all the way from the interactions between nucleons to the superheavy nuclei and neutron stars.

The roadmap for low-energy nuclear theory is well-established. It involves the extension of \textit{ab initio} and CI approaches all the way to medium-heavy nuclei, and the quest for a universal nuclear density functional that will allow description
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of all nuclei up to the heaviest elements and neutron stars. It also includes developments in reaction theory required for a meaningful link to experiment. The direct coupling from nucleon–nucleon interaction scales (~100 MeV) to nuclear binding scales (~1–10 MeV) to collective excitation scales (< 1 MeV), facilitated by effective field theory, provides a coherent picture of the structure and dynamics of all nuclei and nucleonic matter found in astrophysical environments. To realize this vision, the properties of rare isotopes are an essential guide.

The development of a theoretical framework that connects the light and heavy nuclei, proton-rich and neutron-rich rare isotopes and dense neutron matter is within reach. In the next decade, these developments will have profound implications for nuclear physics, nuclear astrophysics and neighboring areas, such as high-energy astrophysics, fundamental interaction physics and hadron structure.

With FRIB, the field has a clear path to achieve its overall scientific goals and to answer the overarching questions. With FRIB, we will have the ability to produce the key isotopes now unavailable. FRIB will be the world’s most powerful facility to explore the rare-isotope frontier, making nearly 80% of the isotopes predicted to exist for elements up to uranium and providing access to beams of the most interesting isotopes. By taking advantage of the unique coupling of crucial data from FRIB and other radioactive beam facilities with advanced theoretical frameworks and high-performance computing, nuclear theory will be able to develop a predictive picture of nucleonic matter. This is an exciting perspective.

Acknowledgments
This work was supported by the US Department of Energy under Contract No. DE-FG02-96ER40963 (University of Tennessee), Nos. DE-SC0008499/DE-SC0008533 (NUCLEI SciDAC Collaboration), DE-AC02-06CH11357 (Argonne National Laboratory), DE-AC52-07NA27344 (Lawrence Livermore National Laboratory), DE-AC52-06NA25396 (Los Alamos National Laboratory), DE-SC0004087 and DE-FG52-08NA28552 (Michigan State Univ) and DE-AC05-00OR22725 (Oak Ridge National Laboratory); the National Science Foundation under Grant No. PHY-1306250 (Ohio State University), PHY-1068022 (Texas A&M University-Commerce), PHY-1068271 (Michigan State Univ), PHY-0970064 and PHY-1307372 (University of California, San Diego), PHY-1205024 (University of Wisconsin-Madison); and the National Aeronautics and Space Administration under grant NNX11AC41G issued through the Science Mission Directorate (Texas A&M University-Commerce).

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