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JKR Theory for the Stick—Slip Peeling and Adhesion Hysteresis of Gecko Mimetic Patterned Surfaces with a Smooth Glass Surface

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3 Supporting Information

ABSTRACT: Geckos are highly efficient climbers and can run over any kind of surface with impecable dexterity due to the typical design of their hierarchical foot structure. We have fabricated tilted, i.e., asymmetric, poly(dimethylsiloxane) (PDMS) microflaps of two different densities that mimic the function of the micrometer sized setae on the gecko foot pad. The adhesive properties of these microflaps were investigated in a modified surface forces apparatus; both for normal pure loading and unloading (detachment), as well as unloading after the surfaces were sheared, both along and against the tilt direction. The tilted microflaps showed directional, i.e., anisotropic adhesive behavior when sheared against an optically smooth (RMS roughness ≈ 10 ± 8 nm) SiO2 surface. Enhanced adhesion was measured after shearing the flaps along the tilted (gripping) direction and low adhesion when sheared against the tilted (releasing) direction. A Johnson–Kendall–Roberts (JKR) theory using an effective surface energy and modulus of rigidity (stiffness) quantitatively described the contact mechanics of the tilted microflaps against the SiO2 surface. We also find an increasing adhesion and stick—slip of the surfaces during detachment which we explain qualitatively in terms of the density of flaps, considering it to increase from 0% (no flaps, smooth surface) to 100% (close-packed flaps, effectively smooth surface). Large energy dissipation at the PDMS—silica interface caused by the viscoelastic behavior of the polymer results in stick—slip peeling and hence an enhanced adhesion energy is observed during the separation of the microflaps surface from the smooth SiO2 surface after shearing of the surfaces. For structured multiple contact surfaces, hysteresis as manifested by different loading and unloading paths can be due entirely to the elastic JKR micro-contacts. These results have important implications in the design of biomimetic adhesives.

INTRODUCTION

The supreme ability of geckos to attach and detach quickly to any surface has been fascinating man for over two millennia. They can attach and detach their toes in matters of millisecond1 on surfaces, be they vertical or inverted. This exceptional feature of quick attachment and equally quick detachment to any surface is attributed to the typical hierarchical structure of their foot-pad2 and is still a challenge that no conventional adhesive is capable of meeting. A considerable number of studies have been performed to understand the mechanism of the gecko adhesive system3—8 and mimic the same for functional surfaces and articulated robotic devices.9—12

It has been shown that the geckos employ the universal van der Waals force of adhesion6,13 and possibly capillary forces14—18 to attach to surfaces and a peeling mechanism for quick detachment.4 It has been demonstrated that the hierarchical structure of the gecko foot hair not only allows it to conform to micro and nano scale asperities maintaining high adhesion force on surfaces, but also has anisotropic/directional frictional-adhesion properties.13,19,20 Various types of patterned hierarchical structures mimicking the gecko foot pad have been fabricated for enhanced adhesion to smooth and rough surfaces.10,11,21—30 Previous works have shown that tilted micro structures perform most closely to the gecko adhesive system.11,12,21,22,31,32 However, little effort has been made to understand the effect of the geometry and the areal density of the flaps at the micro level, which is crucial in determining the contact mechanics of the arrays of the flaps to a surface.

Here, we report the mechanism of adhesion of the tilted poly(dimethylsiloxane) PDMS micro flaps to a smooth silica surface with and without prior shearing of the surfaces. Shearing significantly changes the effective adhesion energy (twice that of the theoretical value) of the flaps to the silica surface, and its magnitude is dependent on the sliding direction. The unloading of the (asymmetric and structured) flaps from the silica surface with multiple micro contacts is well described by the classic Johnson–Kendall–Roberts (JKR) theory, unlike the peeling of two smooth PDMS surfaces and, the observed hysteresis and stick—slip has a different origin to that seen between two smooth (unstructured) single contact geo-
We demonstrate that the effective stiffness of the arrays of the flaps play minor role in determining the adhesion energy. Stick−slip peeling instabilities during separation after prior sliding of the flaps along the direction of the tilt could rationalize the measured high adhesion energies of the PDMS flaps on the silica surface.

**MATERIALS AND METHODS**

**Fabricated Patterned Surfaces.** Large arrays of tilted PDMS flaps of two different densities (Figure 1), were fabricated using microfabrication techniques described elsewhere. The low (1X) and the high (3.5X) areal density flaps have 1850 flaps/mm² and 6410 flaps/mm², respectively. The flaps are tilted at an angle of 20° from the vertical. Schematic top-view orthographic diagrams showing the positions of the flaps relative to each other for both the (b) 1X flaps and (d) 3.5X flaps.

**Normal and Lateral Force Measurements.** A modified surface forces apparatus (SFA) was used to measure the normal $F_L$ (adhesion and loads) and the lateral forces $F_P$ between the arrays of the fabricated microflaps and a spherical silica disc of radius of curvature, $R = 2$ cm, and RMS roughness $\sim 10 \pm 8$ nm. The full details of the force measurements have been described in previous work. As a summary, the spherical glass disc was mounted to the top friction device, which can slide laterally over a distance of 100−500 μm at different sliding speeds (1−10 μm/s). The PDMS flaps were glued to a flat glass disc, which sits on a double cantilever spring with strain gauges that can measure the normal forces. A CCD camera was mounted on a microscope to visualize the contact area during loading, unloading, and sliding of the spherical silica disc against the arrays of the fabricated PDMS microflaps (Figure 2).

In the SFA experiment, the top spherical silica disc was pressed against the PDMS microflaps at a constant speed of $\sim 10 \mu m/s$ until the desired preload, $F_L$ was reached. Adhesion tests were performed by separating the two surfaces, without them being sheared against each other (no prior shearing). Adhesion was also measured after the surfaces were sheared against each other at a velocity of $10 \mu m/s$ along the $+y$ direction (along the direction of the tilt) and $-y$ direction (against the direction of the tilt). Shearing was stopped after sliding for $\sim 300 \mu m$ while the surfaces were still under a shear stress (Figure 3). The flaps did not get damaged even after many sliding cycles (50−100) at a given contact point and the adhesion tests were reproducible at different contact points. Measurements and surface preparations were performed in a clean dust free environment (sealed SFA or in Laminar flow hood).

**Theoretical Background.** A brief description of the contact mechanics between two bodies in adhesive contact will be helpful in interpreting the experimental data, since this work investigates the effect of shear on the change in the adhesion properties of a patterned surface against a smooth silica disc.
Deformation of the tilted PDMS flaps under pure loading, shear against tilt, stop shearing and unload

Shear along tilt, +y direction

Shear against tilt, −y direction

Figure 3. Schematics of a single flap deformation showing the separation of the flap with the upper silica surface after the flaps are sheared (a) along the direction of the tilt (+y direction) (b) against the direction of the tilt (−y direction). The adhesion forces, −F⊥, measured after sliding the top surface in the +y direction are significantly higher than the values measured after sliding in the −y direction.

Classical mechanics deals solely with bulk materials, whereas contact mechanics takes into account the bulk properties along with the surface and geometry of contact. Geometric effects of local elastic deformation were first considered by Hertz,35 and the effect of adhesive interactions were neglected. An improvement over the Hertzian theory is the Johnson–Kendall–Roberts (JKR) theory,36 in which the contact surfaces are considered to be adhesive. The adhesion force (Fad) between a sphere of radius r and a plane in the JKR model is given by the following:

\[ F_{ad} = \frac{3}{2} \pi r W_{12} \]  

(1)

where \( W_{12} = \gamma_1 + \gamma_2 - \gamma_{12} \) is the thermodynamic work of adhesion, and \( \gamma_1, \gamma_2, \) and \( \gamma_{12} \) are the surface and interfacial energies of two interacting surfaces.

A JKR experiment involves bringing two surfaces (a sphere and a plane) into contact by applying an external load followed by retraction until the contact is broken. The deformation of the surfaces at a specified load \( F_i \) is described by the contact area of radius \( a \) as a result of compression (and adhesion). The expression for \( a \) is given by the following:36

\[ a = \pi \left\{ \frac{r}{K_{eff}} \left[ F_i + 6\pi W_{12} + \left( 12\pi W_{12} F_i + (6\pi W_{12})^{1/2} \right)^{2/3} \right] \right\}^{2/3} \]  

(2)

\[ \frac{1}{K_{eff}} = \frac{3}{4} \left( \frac{1 - \nu_1^2}{E_1} + \frac{1 - \nu_2^2}{E_2} \right) \]  

(3)

where \( K_{eff} \) is the effective stiffness, \( \nu \) and \( E \) are the Young’s modulus and the Poisson’s ratio of the samples 1 and 2, respectively.

Results and Discussion

Adhesion Force Measurement with No Prior Shearing. The adhesion behavior of the low (1X) and the high (3.5X) areal density PDMS microflaps were tested against a smooth spherical silica disc at different preloads of \( F_{ad} = 1 - 40 \) mN. The 1X flaps showed no measurable adhesion (\( F_{ad} < 0.1 \) mN) to the silica surface which is consistent with our previous work (Figure 4).11 The graph of apparent area, \( A_{app} \) vs the normal actual load, \( F_{fl} \) for the 1X flaps showed no hysteresis between the loading and unloading curves (Figure 4), which is a characteristic signature of non-adhesive contact. This observation is attributed to the high surface roughness (RMS roughness \( \approx 250 \) nm) of the top edge of the 1X flaps (as visualized in the SEM) that reduces the real area of contact between the flaps and the spherical silica surface. The effective stiffness, \( K_{eff} \) of the 1X (low density) PDMS microflaps was calculated to be 1 MPa by JKR sphere on flat geometry fit (eqs 1–3) to the experimental data (Figure 4). The calculated value for \( K_{eff} \) is significantly higher than the expected value for bulk PDMS (~300 kPa) and is attributed to the nonlinear strain response to the applied stress for the PDMS material (see Supporting Information, SI, Figure S1).

The 3.5X (high density) PDMS microflaps showed an adhesion force of \( F_{ad} = 0.8 \) mN against the silica disc (Figure 5). SEM images show that these flaps have lower surface roughness (for the top edge of the flaps (RMS roughness \( \sim 170 \) nm). The
lower surface roughness and the high areal density result in better commensurability between the surfaces and hence superior adhesion of the 3.5X PDMS microflaps against the silica surface. The plot of $A_{app}$ vs $P^f_{app}$ for the 3.5X flaps was hysteretic with $K_{eff} = 6$ MPa and an effective value for the work of adhesion of $W = 8$ mJ/m$. This effective work of adhesion is an outcome of the decreasing energy due to the formation of bonds between the surfaces at the expense of the elastic deformation energy which reduces the binding energy.

The adhesion force per flap, $f_{app}$, was calculated to be 1 μN with a real area of contact per flap of $a_{real} = 5 \mu m^2$, and the local radius of curvature at pull-off was $r = 5 \mu m$ (Table 1) for the 3.5X flaps during pure loading and unloading (no shear). The Hamaker constant for PDMS and silica interacting across dry air is $5.3 \times 10^{-20}$ J. Hence, the adhesive pressure, $P_{ad}$ between PDMS and silica is, $P_{ad} = (A/6\pi D^3) = 6.3 \times 10^5$ N/m$, where $D = 0.165$ nm is the intermolecular distance. Thus, the theoretically calculated force of interaction between one flap and the silica surface due to van der Waals force is $f_{ad}^{theory} = a_{real}P_{ad} = 3$ mN. This is about 3 orders of magnitude bigger than the experimentally observed value for $f_{ad}$ and shows how roughness can significantly decrease the adhesive force of interaction between two surfaces.

The measured pull off force depends on the modulus of rigidity of the surfaces as well as the surface roughness, and the length scale, $λ = W/K_{eff}$ determines the range over which the attractive adhesive force dominates the repulsive elastic force. The higher the value for $λ$, the more compliant the surfaces are and the stronger the adhesive force of interaction is between the surfaces. The effective stiffness of the 3.5X (high density) PDMS microflaps is $≈ 3.5$ times larger than that of the 1X (low density) microflaps; however, the former flaps showed adhesion to the silica surface and the latter one does not. This is because $λ$ for the 1X and the 3.5X PDMS microflaps are $≈ 0$ and 1.3 nm respectively, i.e., the elastic strain energy between the 1X PDMS microflaps and the silica surface always dominates over the adhesive energy if the surfaces are separated without prior sliding.

### Adhesion Force Measurement with Prior Shearing
Shearing the arrays of the tilted PDMS microflaps against the silica surface significantly increased the adhesive force of interaction between the two surfaces. For the 1X (low density) microflaps, effective adhesion energies of $W = 28$ mJ/m$^2$ and 9 mJ/m$^2$ were obtained for prior shearing of the flaps against the silica surface along the $+y$ (along the tilted direction or grippintg direction) and the $-y$ directions (against the tilted direction or releasing direction), respectively (Figure 4). The high density 3.5X microflaps exhibited much larger $W$ of 122 mJ/m$^2$ and 45 mJ/m$^2$, respectively, for prior shearing the flaps against the silica surface along the $+y$ and $-y$ directions (Figure 5). The

![Image](https://example.com/image.png)

**Figure 5.** The apparent area, $A_{app}$ vs the normal actual load, $F_{a}$ for the 3.5X tilted PDMS microflaps as they are separated (unloaded) from the spherical silica surface of radius of curvature, $R = 2$ cm. The open squares represent the experimentally observed $A_{app}$ when unloading the flaps from the silica surface. The curves show the JKR fits to the experimental data. As a comparison, the area of the plot occupied by the curves for the 1X tilted PDMS microflaps is also shown by the shaded gray box.

### Table 1. Sphere on Flat JKR Model for Individual Flap Deformation

<table>
<thead>
<tr>
<th></th>
<th>1X tilted PDMS flaps (±15%)</th>
<th>3.5X tilted PDMS flaps (±15%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>per flap JKR parameters</td>
<td>no shear</td>
<td>$γ$ shear</td>
</tr>
<tr>
<td>calculated number of flaps at pull off, $n^a$</td>
<td>–</td>
<td>530</td>
</tr>
<tr>
<td>calculated adhesion force, $f_{ad}$ (μN)$^b$</td>
<td>–</td>
<td>5</td>
</tr>
<tr>
<td>JKR radius of curvature, $r$ (μm)$^c$</td>
<td>–</td>
<td>20</td>
</tr>
<tr>
<td>calculated real area of contact, $a_{real}$ (μm)$^d$</td>
<td>–</td>
<td>31</td>
</tr>
</tbody>
</table>

$^a$Calculated from the measured apparent area of contact, $A_{app}$ using the equation, $n = A_{app}/σ$ where $σ = $ Flap density (1850 flaps/mm$^2$) for 1X tilted PDMS flaps and 6410 flaps/mm$^2$ for 3.5X tilted PDMS flaps
$^b$Calculated from the measured force at pull off (total adhesion force), $F_{ad}$, using the equation, $f_{ad} = F_{ad}/n$
$^c$Calculated from the JKR sphere on a flat model using equation 1.
$^d$Calculated from the JKR sphere on a flat model using equation 2, where, $1/K = 3/(4(k_{PDMS} + k_{glass})$). Now, $k_{PDMS} = (1−μ_{PDMS})/E_{PDMS}$, $k_{glass} = (1−μ_{glass})/E_{glass}$ since $E_{glass} (1.8$ MPa) $≈ E_{glass}(50$ GPa). Hence, $1/K ≈ 3/4$ $k_{PDMS} = 3/4(1−2ν_{PDMS})/E_{PDMS}$ $= 3/4(1−0.5^2)/1.8 \rightarrow K = 3.2$ MPa. Therefore, the fitted stiffness, K to the JKR sphere on flat model in equation 2 for the individual flaps is 3.2 MPa.
Slip instabilities were observed at the PDMS flaps–silica interface during unloading after prior shearing along the +y direction (along the direction of the tilt) for both the flap densities (Figure 6). The magnitudes of these instabilities were bigger for the 3.5X (high density) microflaps relative to the 1X (low density) microflaps (see SI Figure S2). This can be attributed to the larger number of flaps detaching from the PDMS–SiO\textsubscript{2} interface for the 3.5X microflaps compared to the 1X microflaps during the separation of the two surfaces, as illustrated in Figure 7. Theoretically, the stick–slip instability should reach a maximum value on increasing the flaps coverage, then decrease and eventually disappear for 100% coverage (close-packed flaps) which can be considered to be an effectively smooth surface, as in the case of zero coverage (Figure 7). No slip instabilities were recorded for unloading after prior shearing along the −y direction (against the direction of the tilt). Hence, another possible explanation for the high observed value of \( W \) for the 3.5X microflaps after prior shearing along the +y direction could be large energy dissipation at the PDMS–silica interface close to the crack tip caused by the viscoelastic behavior of the polymer. The latter possibility is more probable since the separation of the surfaces causes local elastic instabilities close to the crack tip, and this is evident from the graph of \( F_{ix} \) vs \( t \) (Figure 6).

Figure 7. The magnitude of stick–slip instabilities observed in the load and friction forces (See Figures 6a and) during the peeling of the spherical glass disc from the patterned surface increases with increase in the flap density and would disappear eventually resulting in smooth peeling. This observation can be attributed to the number of flaps undergoing detachment during slip instability in the system. The flaps undergoing slip during instability are shown in red.
This implies that the disparity in the adhesive strengths due to shearing of the surfaces along the two different directions is due to different real areas of contact between the PDMS flaps and silica surface during the sliding cycles and/or elastic instabilities, as explained above, and not due to the difference in the bending energies of the flaps as previously hypothesized.\textsuperscript{11}

**CONCLUSIONS**

Our experimental results demonstrate that the Johnson–Kendall–Roberts (JKR) theory, using an effective surface energy and stiffness at the macro scale, quantitatively describes the contact mechanics of the microflaps ensemble against a smooth silica surface. The effective stiffness and the surface energy depend on the ratio of real to apparent contact areas, which can be measured in the SFA experiments. Inserting these values in the JKR theory yielded normal load vs area curves close to those measured, thereby validating this model. We also find an increasing adhesion and stick–slip of the surfaces during detachment, which we explain qualitatively in terms of the density of flaps, considering it to increase from 0% (no flaps, smooth surface) to 100% (closed-packed flaps, effectively smooth surface). Our results and interpretations should be applicable to other rough and patterned surfaces and could serve as a model for designing and fabrication of gecko mimetic surfaces.

**ASSOCIATED CONTENT**

\section{Supporting Information}

The stress vs strain curve for bulk PDMS and the stick–slip peeling instabilities in the low density (1X) tilted PDMS flaps. This material is available free of charge via the Internet at http://pubs.acs.org.

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**Notes**

The authors declare no competing financial interest.

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**REFERENCES**


