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Authors
Ye, X
Zhu, C
Ercius, P
et al.

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Structural diversity in binary superlattices self-assembled from polymer-grafted nanocrystals

Xingchen Ye\textsuperscript{1}, Chenhui Zhu\textsuperscript{2}, Peter Ercius\textsuperscript{3}, Shilpa N. Raja\textsuperscript{4,5}, Bo He\textsuperscript{6}, Matthew R. Jones\textsuperscript{1}, Matthew R. Hauwiller\textsuperscript{1}, Yi Liu\textsuperscript{6}, Ting Xu\textsuperscript{4,5} & A. Paul Alivisatos\textsuperscript{1,5,7}

Multicomponent nanocrystal superlattices represent an interesting class of material that derives emergent properties from mesoscale structure, yet their programmability can be limited by the alkyl-chain-based ligands decorating the surfaces of the constituent nanocrystals. Polymeric ligands offer distinct advantages, as they allow for more precise tuning of the effective size and ‘interaction softness’ through changes to the polymer’s molecular weight, chemical nature, architecture, persistence length and surrounding solvent. Here we show the formation of 10 different binary nanocrystal superlattices (BNSLs) with both two- and three-dimensional order through independent adjustment of the core size of spherical nanocrystals and the molecular weight of densely grafted polystyrene ligands. These polymer-brush-based ligands introduce new energetic contributions to the interparticle potential that stabilizes various BNSL phases across a range of length scales and interparticle spacings. Our study opens the door for nanocrystals to become modular elements in the design of functional particle brush solids with controlled nanoscale interfaces and mesostructures.

\textsuperscript{1}Department of Chemistry, University of California, Berkeley, California 94720, USA. \textsuperscript{2}Advanced Light Source, Lawrence Berkeley National Laboratory, Berkeley, California 94720, USA. \textsuperscript{3}National Center for Electron Microscopy, The Molecular Foundry, Lawrence Berkeley National Laboratory, Berkeley, California 94720, USA. \textsuperscript{4}Department of Materials Science and Engineering, University of California, Berkeley, California 94720, USA. \textsuperscript{5}Materials Sciences Division, Lawrence Berkeley National Laboratory, Berkeley, California 94720, USA. \textsuperscript{6}The Molecular Foundry, Lawrence Berkeley National Laboratory, Berkeley, California 94720, USA. \textsuperscript{7}Kavli Energy NanoScience Institute, Berkeley, California 94720, USA. Correspondence and requests for materials should be addressed to T.X. (email: tingxu@berkeley.edu) or to A.P.A. (email: apalivisatos@lbl.gov).
O
dered arrays of colloidal nanocrystals (NCs) represent
an important class of metamaterials with tunable
structures and properties1–9. Progress in NC synthesis
and self-assembly has enabled co-crystallization of two types of
NCs into binary nanocrystal superlattices (BNSLs) exhibiting a
wide range of stoichiometries and lattice symmetries4,8,10–14. The vast majority of studies on BNSLs thus far involve
the self-assembly of colloidal NCs that are capped with pristine
alkyl ligands4,10–12,14. As a consequence, the structural tunability
in BNSLs is often intimately connected to one’s ability to
synthetically adjust the inorganic core size of the NCs4. However,
it is not always feasible to tune the NC size across a broad range
for a given material. More importantly, the physical properties of
NCs exhibit a strong dependence on their dimensionality1. To
harness the full potential of self-assembly as a route to rational-
design metamaterials and functional devices, it is necessary to
develop a modular building block in which the inorganic core and
the organic ligand shell play complementary and equally
important roles in dictating the structure and function of the
final assembled phase.

Polymer brushes, or polymer chains end-tethered to a surface
through covalent or coordinative interactions, represent an
interesting class of soft materials15–24. The conformational
flexibility and functional versatility inherent to these systems
make polymer brushes an attractive platform for many
applications in nanotechnology and biotechnology20,24–27. More
importantly, grafting polymers onto NCs introduces new energetic
contributions arising from polymer chain conformational entropy
and interaction enthalpy. These energetic contributions can be
readily tailored by the control of the polymer’s molecular weight,
chemical nature, architecture, persistence length and surrounding
solvent. Therefore, the incorporation of polymeric ligands would
greatly expand the parameter space for the design of ordered
particle brush solids. Over the past several decades, extensive
experimental and theoretical efforts have been devoted to studies of
various particle-polymer brush hybrid materials. Several recent
examples of self-organization of polymer-grafted NCs into ordered
assemblies have demonstrated the formation of single-component
two-dimensional (2D) hexagonal lattices18,19,25,28–34. In contrast,
limited success has been achieved in creating more complex, binary
arrays of polymer-grafted NCs with both two- and three-
dimensional (3D) order. In one notable example, the Bockstaller
group has studied binary mixtures of polystyrene-coated Au NCs
and silica nanoparticles, and observed that the small Au NCs
segregate preferentially to interstitial sites within a regular array
formed by the larger silica nanoparticles35.

In this work, we explore the self-assembly of binary mixtures of
polymer-grafted NCs into long-range-ordered particle brush
solids. We carry out detailed studies of the polymer brush
characteristics on a wide variety of NCs, in both solvated and
dried states. These results allow us to access a set of modular
building blocks from which a desired BNSL phase can be created
via rational choice of NC component. Distinct from alkyl-chain-
based ligands, one unique advantage of using polymeric ligands is
that the interparticle spacing can be predicted and experimentally
accessed with high precision ranging from one to several tens
of nanometres, which can be important for tailoring magnetic
dipolar coupling36, plasmonic coupling37,38 and energy transfer
mediated by dipole–dipole interactions within NC assemblies39.

Results
Synthesis and characterization of polymer-grafted NCs. To
introduce polymeric ligands onto the surfaces of NCs, we used the ‘grafting-to’ method, as it allows for independent optimization of
the synthesis of inorganic NCs and polymers. Monodisperse Au
and Fe₃O₄ NCs were first synthesized according to established
protocols (Supplementary Fig. 1)40–42. We then carried out a
simple ligand-exchange process to graft a dense layer of low-
polydispersity polymers to the NCs (Supplementary Table 1). We
chose atactic polystyrene, an amorphous polymer that is often
regarded as a model polymer system21,27,30,34,35,43–46. For Au NCs,
thiol-terminated polystyrene was used to replace the pristine
oleylamine ligand, given the strong affinity between thiol groups
and gold surfaces. On the other hand, carboxyl-terminated
polystyrene was employed to displace the native oleic acid ligands
of Fe₃O₄ NCs, driven largely by the law of mass action. Following
ligand exchange, it was found that both Au and Fe₃O₄ NCs
became insoluble in hexane but were readily soluble in toluene,
chloroform and tetrahydrofuran, all of which are known to be
good solvents for polystyrene. The ligand exchange was also
monitored using Fourier transform infrared (FTIR) spectroscopy.
Distinct vibrational fingerprints of the aromatic moiety were
evident for all polystyrene-exchanged NCs, but were noticeably
absent for the as-synthesized NCs (Supplementary Fig. 2)47.
Altogether, these results indicate the presence of an appreciable
amount of polystyrene on the surfaces of the NCs.

To probe more quantitatively the ligand-exchange reaction,
thermal gravimetric analysis (TGA) was used to evaluate the
ligand grafting density. For polymer-grafted NCs, weight loss
events were observed at elevated temperatures (above 250 °C),
originating predominantly from thermal degradation of poly-
styrene chains into volatile products composed mostly of styrene
monomer and oligomers (Supplementary Fig. 2)47. As summarized in Table 1, there appears to be a clear trend of
decreasing grafting densities with increasing polystyrene chain
lengths for Au NCs of various core sizes. This may be
qualitatively understood using de Gennes’s scaling model for a
polymer chain confined inside a small cylindrical tube: the loss in
conformational entropy for constrained polystyrene chains can be
more than compensated for by the enthalpy gain associated with
bond formation between the polymer anchoring groups (thiols or
carboxylic acids) and the NC surfaces49. As the enthalpic
contribution remains unchanged regardless of the polystyrene
chain length, grafting a longer chain will become energetically
more costly unless the chain can be confined within a tube of
greater diameter. In addition, the dynamic, self-limiting nature of
the ligand-exchange process may also play a role. The
already-grafted polymer chains can introduce a steric barrier
for subsequent chains to reach the binding sites on the NC
surface. This effect can be more pronounced for longer chains.
From the TGA-derived grafting densities, we estimated the
average distance between adjacent ligand anchoring sites by
assuming that the effective footprint of individual ligand
molecules is a circular area with a diameter equal to the
distance between adjacent chains. As shown in Supplementary
Table 2, the average spacings between polystyrene ligands on Au
NCs are considerably smaller than the Flory radius R_F, defined as
the root-mean-squared end-to-end distance for a free polymer

| Table 1 | Grafting densities (chains nm⁻²) of polystyrene ligands on Au NCs estimated from TGA. |
| Core diameter | OLAM | PS-SH (1.1k) | PS-SH (1.5k) | PS-SH (3.0k) | PS-SH (5.0k) | PS-SH (11.5k) | PS-SH (20.0k) |
| 3.8 nm Au | 5.60 | 2.62 | 2.25 | 1.71 | 1.08 | — | — |
| 4.5 nm Au | 5.75 | 2.16 | 2.28 | 1.89 | — | — | — |
| 7.6 nm Au | 4.92 | 2.39 | 1.72 | 1.27 | 0.95 | 0.83 | — |

OLAM, oleylamine; PS-SH, thiol-terminated polystyrene; TGA, thermal gravimetric analysis. The estimated error is less than 10% based on multiple runs with the same sample.
chain\(^5\). Therefore, the polystyrene chains are expected to extend from the NC surface much farther than their natural dimensions to avoid steric overcrowding, thus forming a polymer ‘brush’. Moreover, the grafting densities on 3.8 nm (core diameter) Au NCs are consistently larger than those on 7.6 nm Au NCs for the same polystyrene chain length, which may be attributed to the fact that the smaller radius of curvature of larger NCs can create a more crowded local environment for the polymer chains.

Scaling behaviour of polymer brushes on spherical NCs. The development of polymer brush theories dates back to the 1970s. In their pioneering work, Alexander\(^51\) and de Gennes\(^52\) theoretically predicted that the thickness of a planar polymer brush in a good solvent scales as \(h \sim N^{1/3}\), where \(N\) is the degree of polymerization for the grafted polymer and \(\sigma\) is the grafting density. Distinct from planar brushes, a spherical interface implies that the effective ligand areal density is not invariant but decreases with increasing radial distance from the surface. Therefore, one would expect drastically different scaling behaviour between spherical and planar polymer brushes.

Daoud and Cotton adopted the Alexander and de Gennes’s free energy scaling approach and developed scaling models for star-shaped polymers\(^53\). The widely used Daoud–Cotton model set up a theoretical framework for the understanding of spherical polymer brushes and polymers tethered to curved surfaces. Later, Birshtein and Zhulina determined that the thickness of a polymer brush layer grafted to a spherical surface in the melt state (that is, in the absence of solvent) scales as \(h_0 \sim N^{1/5} \sigma^{1/4}\), and that in a good solvent scales as \(h \sim N^{3/5} \sigma^{1/5}\) (refs 54–56). These different scaling laws highlight the dissimilarity of the mechanisms underlying polymer chain conformations between the solvated and the dried state. In the presence of solvent, polymer chains stretch away from the grafting surface by virtue of the effective repulsions between chain segments. In the dried state, however, the chains stretch away from the interface to alleviate steric constraints or overfilling of space.

Spherical polymer brushes represent a model system that is intermediate between flat brushes and star-shaped polymers. A linear polymer chain attached by one end to a spherical NC at relatively high coverage is expected to take on more stretched conformations in the vicinity of NC surface and assume progressively more relaxed configurations with increasing radial distance from the NC surface, as pictured schematically in Fig. 1a. Polymer brushes grafted onto spherical NCs dispersed in a good solvent can be categorized into three different regimes depending on the grafting density and the polymer chain length\(^54,55\). At low grafting densities, polymer chains adopt an approximately random coil conformation, the so-called ‘mushroom’ regime. As the grafting density exceeds the chain overlap threshold, a transition to the semidilute polymer brush regime takes place, resulting in the stretching of polymer chains normal to the grafting surface. In the limit of high grafting densities, the concentrated polymer brush (CPB) regime is accessed, which is characterized by non-Gaussian chain characteristics and more extended chain conformations due to excluded volume interactions. Dukes et al.\(^57\) concluded that for a spherically symmetric grafting surface the hydrodynamic thickness of polymer brushes scale as \(h \sim N^{3/5}\) for the CPB regime but...
unperturbed polymer chains in the melt, the polystyrene chains greatly expanded by using polymeric ligands. It is worth pointing (Fig. 1f, blue curve). Compared with commonly employed alkyl least 70% of the total volume within these hybrid building blocks experimental findings on polymer brushes bound to spherical above-mentioned theoretical predictions as well as recent molecular weight of the polymer chains, which is almost homogeneously dense polymer brushes on the NC surfaces. It is Fig. 6), providing compelling evidence for the presence of the interparticle separation in 2D NC superlattices, independent of the core size of Au NCs (Fig. 1f, red curve and Supplementary Fig. 7). These scaling relations with exponents between 0.7 and 0.8 were obtained for 3.8 and 4.5 nm Au NCs (Supplementary Fig. 4). These scaling results indicate that it is appropriate to consider the polystyrene chains on Au NCs to be in the CPB regime26,31–33,57. It is also instructive to assess the scaling relation between the polymer-brush thickness and the molecular weight of polystyrene $M_n$ in the melt. The interparticle spacing in a ‘dried’ NC array is largely determined by the ligand chain configuration as well as degree of chain interdigitation between adjacent NCs. The ligand layer thickness $l$, estimated as half of the nearest-neighbour surface-to-surface interparticle separation in 2D NC superlattices, serves as a good measure of the size of the tethered polymer chains (Fig. 1d). The average thickness of the ligand layer, determined from statistical analysis of a large set of nearest-neighbour NC pairs from TEM images (Fig. 1e and Supplementary Figs 5 and 6), was found to increase systematically with increasing molecular weight of the polystyrene ligand (Supplementary Tables 5 and 6). Well-defined interparticle spacings with a narrow distribution (coefficient of variation $<8\%$) are observed for all 2D NC superlattices (Supplementary Fig. 6), providing compelling evidence for the presence of homogeneously dense polymer brushes on the NC surfaces. It is found that the brush thickness scales roughly as the square root of the molecular weight of the polymer chains, which is almost independent of the core size of Au NCs (Fig. 1f, red curve and Supplementary Fig. 7). These results are in line with the above-mentioned theoretical predictions as well as recent experimental findings on polymer brushes bound to spherical surfaces25,34–57. Remarkably, the polystyrene ligands take up at least 70% of the total volume within these hybrid building blocks (Fig. 1f, blue curve). Compared with commonly employed alkyl ligands, the range of accessible ligand shell thickness can be greatly expanded by using polymeric ligands. It is worth pointing out that even though the observed scaling behaviour is similar to unperturbed polymer chains in the melt, the polystyrene chains on NCs are indeed stretched. The average ligand layer thickness is found to be about twice the radius of gyration $R_g$ of free polystyrene chains (Supplementary Table 6), which seems somewhat contradictory with the conclusions drawn from TGA or DLS measurements that the polystyrene chains are stretched and can be treated as polymer brushes. These results can be reconciled by considering that the areal ligand density on the outer NC surface can be reduced appreciably by a factor of $(\frac{R_g}{l})^2$ compared with the grafting density, providing room for polystyrene chains from approaching NCs to interpenetrate. We note that the polymer chains can also deform and fill the interstitial space in NC superlattices. Interpenetration between spherical polymer brushes and polymer chain deformation help reduce the energetically unfavourable polymer-air interfacial area and act to densify NC packing14,35.

Three-dimensional binary superlattices. Using these monodisperse polystyrene-capped Au and Fe3O4 NCs as spherical building blocks, we explore the possibility of order formation in a binary mixture of NC polymer brushes. BNSLs were formed by slow drying of a toluene solution of mixed NCs on top of an immiscible liquid subphase, namely, diethylene glycol (DEG)12. Fe3O4 NCs (13.4 nm) functionalized with polystyrene having a number-average molecular weight $M_n=5.3\, k$, denoted as 13.4 nm (5.3 k) Fe3O4 NCs, were chosen throughout this work as the large NC building blocks for BNSLs. The experimentally derived polymer brush scaling relations or ‘master curves’ for different-sized Au NCs allow for modular design of smaller NC building blocks targeting a specific NC size ratio (Fig. 1f, red curve and Supplementary Fig. 7).

Figure 2a shows a representative TEM image of NaZn13-type BNSLs self-assembled from 3.8 nm (3.0 k) Au and 13.4 nm (5.3 k) Fe3O4 NCs. Both the cubic symmetry and the long-range positional ordering are clearly manifested by the sharp diffraction spots in the selected-area electron diffraction (SAED) pattern recorded from the same BNSL domain (Fig. 2b). High-magnification TEM imaging (Fig. 2d) and high-angle annular dark field scanning TEM (HAADF-STEM) imaging (Fig. 2e) match the [001] projection of the NaZn13 structure in which (Au)$_{13}$icosahedral clusters are separated by simple cubic arrangements of Fe3O4 NCs (Fig. 2c and Supplementary Figs 8 and 9)58. Importantly, a greater portion of electron-transparent regions within these assemblies are observed in comparison to those BNSLs formed by NCs capped with short alkyl chains8,61, highlighting the presence of dense polystyrene brushes on the NC surfaces. Low-magnification TEM image reveals a mosaic texture of predominantly [001]-oriented BNSL grains separated by narrow, glassy regions (Supplementary Fig. 10). The 3.8 nm (3.0 k) Au NC has an average ligand shell thickness $l=3.0\, nm$ (Supplementary Table 6), exceeding its core radius (1.9 nm), whereas $l=3.3\, nm$ for the 13.4 nm (5.3 k) Fe3O4 NC. The effective NC radius is computed as the sum of NC core radius and the ligand shell thickness, allowing the size ratio $\gamma$ (ratio of effective radius between small and large NCs) to be readily calculated to be $\gamma=0.49$.

To study the formation of other BNSL structures using the same combination of 3.8 nm (3.0 k) Au and 13.4 nm (5.3 k) Fe3O4 NCs, we systematically varied the concentration ratio of the two NC building blocks. When the NC concentration ratio is reduced from $\sim 15:1$ used for NaZn13 to $\sim 7:1$, bcc-AB$_{13}$-type BNSLs were obtained. The bcc-AB$_{13}$ structure was initially identified in several alkali-metal intercalation compounds of fullerene C$_{60}$ such as C$_{60}$K and C$_{60}$Cs$_6$ (ref. 59). The unit cell is composed of a body-centred cubic (BCC) lattice formed by the large spheres, with four small spheres arranged into a square on each of the six facets of the cube (Supplementary Fig. 8). Recently, it has been observed in assemblies of oppositely charged micron-sized colloids80, BNSLs14,41 and binary layers of DNA-coated particles6,61. Figure 2f shows representative TEM images of a [001]-oriented domain of the bcc-AB$_{13}$-type BNSLs. Scanning electron microscopy (SEM) was exploited to probe the surface structure of the bcc-AB$_{13}$-type BNSLs. As shown in Fig. 2g and Supplementary Fig. 11, the arrangements of NCs on the top layers match the structural model of the (001) plane, confirming the
structural assignment as bcc-AB6. Further decreases in NC concentration ratio result in the formation of phase-pure BNSLs of lower stoichiometries, including AuCu3 (Fig. 2k–m and Supplementary Fig. 12a), AlB2 (Fig. 2n–p and Supplementary Fig. 12b) and NaCl (Fig. 2q–s). It is worth emphasizing that although these structures have been observed in earlier works, this is the first demonstration of the ability to access all five BNSL structures using NCs with a single size ratio (g ≈ 0.49)4,14. In other words, these polystyrene-grafted NCs appear to be more ‘responsive’ to changes in the NC mixing ratio during BNSL self-assembly.

The crystallization mechanism of BNSLs has been largely attributed to entropic driving forces13,41,58, although complex interparticle effects, such as van der Waals, dipolar, electrostatic, and so on, have also been implicated4,11. Recently, many-body effects and deformability of the ligand shell have been invoked to explain the entropy-driven crystallization of soft nanoscale objects14. Despite these conceptual advances aimed at improved understanding of BNSL formation, phase stability analysis based upon a hard sphere approximation (that is, the space-filling principle) still provides a reasonable theoretical framework and useful experimental guideline. This is due primarily to the fact that this model helps to rationalize the relative stability of plausible BNSL phases for a given effective size ratio or the range of size ratios needed to form a particular BNSL structure. Theoretical packing densities as a function of particle size ratio can be derived by modelling BNSL structures as sphere packings (Fig. 3)11,14,41. It is clear that the majority of BNSLs (except the AuCu3 structure) obtained with polystyrene-grafted NCs at the size ratio γ = 0.49 feature a reasonably high packing density (≥ 0.67).

The structure of BNSL assemblies can also be adjusted by tuning the size ratio γ. As shown in Fig. 4a–c, NaCl-type BNSLs were predominantly observed when using the combination of 4.2 nm (1.1 k) Au and 13.4 nm (5.3 k) Fe3O4 NCs, for which

**Figure 2 | Structural diversity in 3D BNSLs self-assembled from 3.8 nm (3.0 k) Au and 13.4 nm (5.3 k) Fe3O4 NCs.** (a) Low-magnification TEM image and (b) corresponding SAED pattern, (c) high-magnification TEM image and (d) HAADF-STEM image of NaZn13-type BNSLs. (e) Structural model of the [001] projection of NaZn13-type BNSLs. (f) Low-magnification TEM image, (g) high-magnification TEM image and (h) SEM image of bcc-AB6-type (isostructural with the C60K6 phase) BNSLs. (i) Structural models of the [001] projection (j) and the (001) surface (h) of bcc-AB6-type BNSLs. (k, n, q) Low-magnification TEM images, (l, o, r) high-magnification TEM images and (m, p, s) structural models of AuCu3-type (k–m), AlB2-type (n–p) and NaCl-type (q–s) BNSLs. Scale bars, (a) 100 nm; (d) 20 nm; (e) 20 nm; (f) 100 nm; (g) 20 nm; (l) 20 nm; (k) 100 nm; (f) 20 nm; (m) 50 nm; (o) 20 nm; (q) 100 nm; (r) 20 nm.

**Figure 3 | Theoretical packing densities for different BNSL phases.** Plots of hard-sphere packing density versus size ratio for various BNSL phases reported in this work. The horizontal dashed line represents the packing density ρ = 0.7405 for single-component close-packed structures.
\( \gamma = 0.40 \). This can be accounted for by the fact that the NaCl structure features a theoretical packing density \( \rho = 0.793 \) that far exceeds other BNSL phases at this size ratio (Fig. 3). On the other hand, MgZn\(_2\)-type (Fig. 4d–f) and CaCu\(_5\)-type BNSLs (Fig. 4g–i) became the preferred structures at \( \gamma = 0.69 \) when 6.1 nm (5.3 k) Au was employed as the smaller NC component. Both structures show significantly increased packing densities when \( \gamma \) increases from 0.49 to 0.69 (Fig. 3). Remarkably, the same CaCu\(_5\)-type BNSLs was obtained by using Au NCs having a larger core size (7.6 nm) yet capped with shorter polystyrene chains (\( \gamma = 0.68 \)), highlighting the versatility of using spherical polymer-grafted NCs as modular building blocks for constructing multicomponent assemblies (Fig. 4j).

The presence of polymeric grafts in the CPB regime on NCs can have complex and intriguing implications on the interparticle interaction potential\(^{62,63} \). In good solvents, the highly extended polymer chains can effectively screen the van der Waals attractions between NC cores and exert steric interactions over a longer range than previously used short alkyl chain ligands. During the late stages of drying-mediated assembly, polymer brushes become compressed but can still penetrate into the outer layers of opposing brushes, allowing for a softening of the repulsive interactions between the NCs. The interplay between polymer chain stretching and chain interpenetration maximizes the overall entropy of the system during the formation of superlattices. Moreover, the softness of the interaction potential can be programmed by varying the thickness of the polymer brushes. For single-component NC assemblies, we indeed observed a structural transition from close-packed structures (fcc or hcp) to a BCC lattice as the size ratio between the polymer ligand and NC core increased (Supplementary Fig. 13). Similar trends have been observed in other soft colloidal systems such as block copolymer micelles\(^{64} \) and NCs\(^{65,66} \).

**Two-dimensional binary superlattices.** When the total NC concentration was reduced by 10–15 times in the spreading solution, 2D BNSLs were formed over extend areas (centimeter scale). Figure 5a shows an example of AB-type 2D BNSLs self-assembled from 3.8 nm (3.0 k) Au and 13.4 nm (5.3 k) Fe\(_2\)O\(_4\) NCs. The SAED pattern (Fig. 5b), HAADF-STEM image (Fig. 5d) and SEM images (Supplementary Fig. 14) confirm that the superlattice is a monolayer in thickness. The large Fe\(_2\)O\(_4\) NCs arranged to form a square lattice, with the smaller Au NCs occupying the centre of individual squares, which is essentially the 2D analogue of the CsCl-type lattice\(^{67} \). The difference in electron density between the two NC cores is clearly visible from the HAADF-STEM image, where the dark background is mostly filled with polystyrene brushes (Fig. 5d). Importantly, the same mixture of Au and Fe\(_2\)O\(_4\) NCs would have become phase-separated or

\[ \text{NaCl} \{110\}, 4.2 \text{ nm (1.1 k)} \quad \text{MgZn}_2 \{001\}, 6.1 \text{ nm (5.3 k)} \]

\[ \text{CaCu}_5 \{001\}, 6.1 \text{ nm (5.3 k)} \]

\[ 7.6 \text{ nm (3.0 k)} \]

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**Figure 4 | Tuning BNSL structures through variations of NC core size and the chain length of polymer brushes.** (a) Low-magnification and (b) high-magnification TEM images of NaCl-type BNSLs self-assembled from 4.2 nm (1.1 k) Au and 13.4 nm (5.3 k) Fe\(_2\)O\(_4\) NCs. (c) Structural model of the [110] projection of NaCl-type BNSLs. (d) Low-magnification and (e) high-magnification TEM images of MgZn\(_2\)-type BNSLs self-assembled from 6.1 nm (5.3 k) Au and 13.4 nm (5.3 k) Fe\(_2\)O\(_4\) NCs. (f) Structural model of the [001] projection of MgZn\(_2\)-type BNSLs. (g) Low-magnification and (h) high-magnification TEM images of CaCu\(_5\)-type BNSLs self-assembled from 6.1 nm (5.3 k) Au and 13.4 nm (5.3 k) Fe\(_2\)O\(_4\) NCs. (i) Structural model of the [001] projection of CaCu\(_5\)-type BNSLs. (j) TEM image of CaCu\(_5\)-type BNSLs self-assembled from 7.6 nm (3.0 k) Au and 13.4 nm (5.3 k) Fe\(_2\)O\(_4\) NCs. Scale bars, (a) 100 nm; (b) 20 nm; (d) 100 nm; (e) 20 nm; (g) 100 nm; (h) 20 nm; (j) 20 nm.
formed disordered films without polystyrene ligands. To complement electron microscopy studies and to probe quantitatively the BNSL structure and the degree of ordering over statistically relevant areas (mm²), we carried out grazing incidence small-angle X-ray scattering (GISAXS) measurements on the AB-type 2D BNSLs. As shown in Fig. 5e, the rod-like shape of the intense scattering features (Bragg rods) in the 2D GISAXS image suggests the presence of an ordered NC monolayer. The scattering profile along the $q_x$ direction corresponding to in-plane ordering features three orders of diffraction peaks spaced as $q_1 : q_2 : q_3 = 1 : \sqrt{2} : \sqrt{5}$ (Fig. 5f). These three peaks can be indexed as the (11), (20) and (31) reflections of a 2D face-centred square lattice. The absence of the (22) reflection may be due to its coincidence with a form factor minimum. The spacing calculated from the first-order diffraction peak by using the formula $d_{11} = 2\pi / q_1$, is 17.8 nm, which is in good agreement with the average centre-to-centre distance between nearest-neighbour Fe₃O₄ NCs determined from TEM (18.3 ± 1.0 nm). Therefore, the GISAXS results confirm that AB-type 2D BNSLs are phase-pure over macroscopic length scales as they appear under electron microscopy surveys. To reveal whether the Au and Fe₃O₄ NCs of AB-type BNSLs are coplanar, we further performed HAADF-STEM electron tomography (Fig. 5g and Supplementary Movie 1). The cross-sectional slice of the 3D tomographic reconstruction of the AB-type BNSLs clearly shows coplanarity of the two NC building blocks (Fig. 5h). When the concentration ratio between 3.8 nm (3.0 k) Au and 13.4 nm (5.3 k) Fe₃O₄ NCs was increased, A₂B₃-type and AB₅-type 2D BNSLs were obtained (Supplementary Fig. 15). Notably, the AB₈ structure has not been reported in previous works on 2D BNSLs.

**Discussion**

We have demonstrated the possibility of forming long-range-ordered binary superlattices using spherical polymer-grafted NCs. A rational choice of polymer-binding group and an optimized ligand-exchange protocol enable attachment of polymer
brushes onto NCs of several different sizes and compositions with high grafting densities (>0.5 nm⁻²). We determined that the brush thickness h scales roughly as the square root of the molecular weight Mₙ of the polymer chains in the melt, and as h ~ Mₙ¹/² when dispersed in good solvents. The scaling behaviour of the brush thickness with molecular weight is in excellent agreement with the existing theoretical predictions and establishes a practical ‘calibration curve’ for synthesising modular polymer-NC building blocks with controlled effective size and interaction potential. A rich variety of 2D and 3D BNSL structures can be accessed from these NCs, most of which agree reasonably well with predictions based on maximized packing densities. The use of polymeric ligands provides quantitative and precise control over nearest-neighbour interparticle distances ranging from several to several tens of nanometres within complex 3D NC assemblies. This is difficult, if not impossible, with the short alkylic-chain-based ligands that have been used in previous studies. Our results open up new and exciting opportunities for the modular design of multicomponent blends of polymer-NC composites for the creation of mechanically robust inorganic–organic materials with controlled nanoscale interfaces and microstructures.

Methods

NC synthesis. All NC syntheses were carried out under argon atmosphere using standard Schlenk line techniques. Au NCs (3.8 and 4.2 nm)⁵⁰, Au NCs (4.5 nm, 6.1 and 7.6 nm)⁵¹, and Fe₃O₄ NCs⁴² were synthesized according to literature methods.

NC ligand exchange. Polystyrene-based ligands (Polymer Source, Inc.) were attached to the NC surface by a simple ligand-exchange reaction. Thiou-decylated and carboxyl-terminated polystyrenes were used as the polymeric ligand for Au and Fe₃O₄ NCs, respectively. In a typical process, as-synthesized Au or Fe₃O₄ NCs were dissolved into 5 mL of tetrahydrofuran (THF) at a NC concentration of 5 mg/mL. Another 5 mL THF solution of end-functionalized polystyrene was prepared separately with a polymeric concentration of 40 mg mL⁻¹. The polystyrene solution was then added dropwise under sonication to the NC solution, and the resulting mixture was left to stir for 24 h at room temperature to promote surface saturation with polymeric ligands. The polymer-modified NCs were isolated by ethanol precipitation and centrifugation at 7 000 r.p.m. for 3 min. The supernatant was removed and the NCs were redispersed in THF. The above solvent–non-solvent cleaning procedure was repeated 4–6 times to remove excess unbound polymers. The NCs were finally dispersed in toluene to a concentration of about 3 mg mL⁻¹.

Self-assembly of NC superlattices. BNSLs were formed by co-crystallization of a binary mixture of NCs on top of an immiscible liquid subphase at room temperature. In a typical process, a toluene solution (~15 µL) containing two types of NCs was drop-cast onto the surface of DEG in a Teflon well (1.5 × 1.5 × 1.5 cm³). The well was then covered with a glass slide to slow down the evaporation rate of toluene. After 5 h, the BNSL film was transferred onto a carbon-coated Cu TEM grid (300-mesh) or a piece of Si wafer (100). The well was then covered with a glass slide to slow down the evaporation rate of toluene. After 5 h, the BNSL film was transferred onto a carbon-coated Cu TEM grid (300-mesh) or a piece of Si wafer (100). The beam size was about 300 µm vertically and 700 µm horizontally. A Philips 2011 microscope (pixel size: ~172 µm) from Dectris was positioned 3.8 m away from the sample. The reciprocal space calibration was performed by using the silver behenate standard. Samples for GISAXS measurements were deposited onto Si substrates. A series of incident angles ranging from 0.05° to 0.25° was used for each sample. GISAXS results presented here were obtained with an incident angle of 0.20°, which is greater than the critical angle of Si (0.18°) and thus ensures full penetration of X-rays into the film. Image processing was done using the Igor NIKA software package. The scattering intensities (I) are plotted with respect to wavevector q, where q = (4π/λ) sin θ, λ is the wavelength of the incident X-ray beam, and 2θ is the scattering angle.

Electron tomography. The projection images for 3D electron tomography were acquired using an FEI Titan 80–300 operated in HAAADF-STEM mode at 200 kV with a 10 nm probe semi-convergence angle. The pixel size was 2.27 nm. HAAADF-STEM images were taken from ~65° to 72° to create a tilt series of 78 images. The tilt series was aligned and reconstructed using the iTom software for the IMOD tomography package. Post-processing was performed in Matlab, and 3D visualization was performed using Tomviz 0.6.1.

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ments. The hydrodynamic diameter D_h was determined from the Stokes–Einstein equation, D_h = k_BT/(6πηD_MW), where D_MW is the diffusion coefficient of NCs, T is temperature, k_B is the Boltzmann constant and η is solvent viscosity. D_MW can be obtained from the intensity correlation function. Hydrodynamic diameters, reported as number averaged values, are averages of five measurements each composed of 15 scans.

Electron microscopies and GISAXS. Bright-field TEM images and SAED patterns were acquired on a 200-kV Tecnai G2 20 S-TWIN TEM equipped with a Gatan Orius SC200 CCD camera. SAED patterns were collected from areas of about 0.5 µm². HAAADF-STEM images were taken on a 200-kV FEI monochromated F20 UT Tecnai TEM. SEM imaging was carried out on a Zeiss Gemini Ultra-55 microscope operating at 5 kV. GISAXS experiments were conducted at beamline 7.3.3 at the Advanced Light Source at Lawrence Berkeley National Laboratory. X-rays (10 keV) with the energy bandwidth E/ΔE = 100 were used. The beam size was 0.5 µm vertically and 700 µm horizontally. A Philips 2011 microscope (pixel size: ~172 µm) from Dectris was positioned 3.8 m away from the sample. The reciprocal space calibration was performed by using the silver behenate standard. Samples for GISAXS measurements were deposited onto Si substrates. A series of incident angles ranging from 0.05° to 0.25° was used for each sample. GISAXS results presented here were obtained with an incident angle of 0.20°, which is greater than the critical angle of Si (0.18°) and thus ensures full penetration of X-rays into the film. Image processing was done using the Igor NIKA software package. The scattering intensities (I) are plotted with respect to wavevector q, where q = (4π/λ) sin θ, λ is the wavelength of the incident X-ray beam, and 2θ is the scattering angle.

Electron tomography. The projection images for 3D electron tomography were acquired using an FEI Titan 80–300 operated in HAAADF-STEM mode at 200 kV with a 10 nm probe semi-convergence angle. The pixel size was 2.27 nm. HAAADF-STEM images were taken from ~65° to 72° to create a tilt series of 78 images. The tilt series was aligned and reconstructed using the iTom software for the IMOD tomography package. Post-processing was performed in Matlab, and 3D visualization was performed using Tomviz 0.6.1.

TGA, DLS and FTIR. TGA was performed by using a Q5000 system (TA Instruments). The sample (5–10 mg) was loaded into an aluminum pan and was heated to 600°C at a constant heating rate of 20 °C/min under argon (for polystyrene alone or polystyrene-grafted NCs) or air (for as-synthesized NCs or oleylamine alone). Analysis was carried out using the TA Universal Analysis software package. The ligand grafting densities (σ) were estimated by using the formula σ = ([NₐP₂]/迫切的 neutron density factor of the bulk material and that no free polymer is present. Here, f is the weight fraction of the organic ligands determined by TGA, Nₐ is the Avogadro constant, ρ is the bulk density of NC's core material (19.32 g cm⁻³) for Au and 5.15 g cm⁻³ for Fe₃O₄, d is the diameter of NCs core and Mₙ is the number-average molecular weight of the polymeric ligands. FTIR spectra were taken in transmission mode on a Thermal Scientific Nicolo 6700 spectrometer equipped with a deuterated triglycine sulfate detector. Samples for FTIR measurements were prepared by drop-casting concentrated NC solutions onto a KBr substrate (International Crystal Laboratories) followed by drying under vacuum. DLS measurements were carried out on a Zetasizer Nano-ZS system (Malvern), equipped with a He–Ne 633 nm laser as the light source. The as-synthesized NCs were dispersed in hexane and polystyrene-capped NCs were dispersed in toluene. Samples were filtered through a 0.2 µm polytetrafluoroethylene syringe filter and were filled in a quartz cuvette for DLS measure-
ments. The hydrodynamic diameter D_h was determined from the Stokes–Einstein equation, D_h = k_BT/(6πηD_MW), where D_MW is the diffusion coefficient of NCs, T is temperature, k_B is the Boltzmann constant and η is solvent viscosity. D_MW can be obtained from the intensity correlation function. Hydrodynamic diameters, reported as number averaged values, are averages of five measurements each composed of 15 scans.

Statistical analysis of interparticle distances from TEM images. Using the ImageJ software, experimental TEM images of 2D single-component hexagonal superlattices were first converted to binary images and the centre of mass of individual particles were determined. Delaunay triangulation then generates a set of bonds connecting nearest-neighbour particle centres. A large number of bond counts (usually between 1,000 and 5,000) were obtained by analysing many TEM images acquired from different areas of the same sample (Supplementary Fig. 6). The distribution of bond length (that is, interparticle distance) was plotted using OriginPro 8.0.


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Author contributions
X.Y. designed the experiments. X.Y. performed the experiments. C.Z. performed GISAXS measurements. P.E. performed electron tomography reconstruction. R.H. and Y.L. carried out TGA studies. X.Y., C.Z., S.N.R., M.R.J. and M.R.H. performed data analysis. T.X. and A.P.A. supervised the project and wrote the manuscript with X.Y. All authors discussed the results and commented on the manuscript.

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