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RECENT STUDIES OF LEAD POLONIDE (PbPo)

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ABSTRACT

Lead polonide (PbPo) is the fourth member of the lead salt group of semiconductors, and has the same NaCl crystal structure as do PbS, PbSe, and PbTe. The empirical relation stating that the energy gap $E_0$ of a semiconductor is directly proportional to $(1/a_0^2)$, where $a_0$ is the lattice constant, has been found to be valid for a number of semiconductors with the NaCl crystal structure. Using this empirical relation, a plot of $E_0$ as a function of $(1/a_0^2)$ for PbS, PbSe, PbTe, and PbPo has been used to calculate a value of $E_0 \equiv E(L_6^-) - E(L_6^+) \approx -0.1$ eV for PbPo. Based on this result, it has been suggested that the band structure of PbPo may be inverted from that of PbS, PbSe, and PbTe. This inversion would result in PbPo having an $L_6^+$ conduction-band edge and an $L_6^-$ valence-band edge. It would therefore imply a negative value of the temperature coefficient $(dE_0/dT)$ of the energy gap in PbPo. The f-sum rule has been applied to this proposed inverted band structure and used to calculate values of the longitudinal and transverse effective masses as follows: for electrons, $(m_L^x/m) = 0.040$, $(m_T^x/m) = 0.024$; for holes, $(m_L^x/m) = 0.045$, $(m_T^x/m) = 0.028$. All of these results predicted for PbPo await the test of experimental study. It is suggested that experimental measurements on lead polonide of the energy gap, of the sign of its temperature coefficient, and of carrier effective masses would provide an interesting test of the correctness of the hypotheses on which the conclusions above are based.
ÉTUDES RÉCENTES DE POLONIDE DE PLOMB (PbPo)

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ABSTRAIT

Le polonide de plomb est le quatrième membre du groupe "PbS" des semiconducteurs, et a le même structure crystallographique "NaCl" comme PbS, PbSe, et PbTe. La relation empirique énonçant que la zone interdite $E_0$ d'un semi-conducteur est directement proportionnelle à $(1/a_0^2)$, où $a_0$ est la constante du treillis, a été trouvée d'être valide pour un nombre des semiconducteurs avec le structure de NaCl. Faisant usage de cette relation empirique, un graphique d'$E_0$ comme fonction de $(1/a_0^2)$ pour PbS, PbSe, PbTe, et PbPo a été employé pour calculer un valeur d'$E_0$ = $E(L_0^-) - E(L_0^+) \approx 0.1$ eV pour PbPo. Fondé sur ce résultat, on a suggéré que le structure des bandes de PbPo est peut-être renversé de ceux de PbS, PbSe, et PbTe. Ce renversement résulterait en le PbPo ayant un bord $L_0^-$ du bande de conduction, et un bord $L_0^+$ du bande de valence. Cela impliquerait un valeur négatif du coefficient de la température $(dE_0/dT)$ de la zone interdite de PbPo. Le règle "f-sum" a été appliqué à ce structure renversé des bandes et a été employé de calculer des valeurs des masses effectives longitudinales et transversales comme suivant: pour les électrons, $(m^* _e/m) = 0.040$, $(m^* _h/m) = 0.024$; pour les trous, $(m^* _e/m) = 0.045$, $(m^* _h/m) = 0.028$. Tous ces résultats prédit pour le PbPo attend l'épreuve d'étude expérimentale. C'est suggéré que des mesurages expérimentals, sur le PbPo, du valeur de la zone interdite, du signe du coefficient de la température, et des valeurs des masses effectives des porteurs, fourniraient des épreuves intéressantes du correction des hypothèses sur lesquels les conclusions en haut sont fondés.
I. Introduction

The compound semiconductors PbS, PbSe, and PbTe, collectively known as the lead salts, have been the subject of intensive research for many years. However, PbPo (lead polonide), the fourth member of this group, has been the object of only one experimental study\(^1\), and the only data available are its crystal structure and lattice constant at room temperature. The work in this paper, published earlier in preliminary form\(^2,3\), proposes a possible band structure for lead polonide. Using this band structure, values of the energy gap and of effective masses are calculated. While these proposals regarding PbPo are based on empirical evidence, the proposed band structure is amenable to an unequivocal experimental test.

The band edge structure of PbS, PbSe, and PbTe is comprised of a direct minimum energy gap \(E_0\) at the L point. The conduction band edge is an \(L_6^-\) state and the valence band edge is an \(L_6^+\) state. Lead sulfide, selenide, and telluride all have the rock-salt crystal structure. Lead polonide also has the NaCl crystal structure, with a lattice constant\(^1\) \(a_o = 6.590\ \text{Å}\) at room temperature. This fact suggests that PbPo very likely has the same band structure as do PbS, PbSe, and PbTe, including a direct energy gap at the L point. Given this assumption, it is of considerable interest to calculate the energy gap \(E_0 = E(L_6^-) - E(L_6^+)\) of PbPo. As discussed in detail below, knowledge of \(E_0\) for lead polonide would also be most useful in the study\(^4\) of the anomaly in the energy gap values \([E_0(PbTe) > E_0(PbSe)]\) in the lead salt group.

II. The Empirical Relation between Energy Gap and Lattice Constant

In order to calculate \(E_0\) for PbPo, the well-known\(^5\) empirical relation between the energy gap \(E_0\) of a semiconductor and its lattice constant \(a_o\) was
considered. This relation states that \( E_o \) is directly proportional to \( (1/a_o^2) \). It is known to hold quite well for the Group IV elemental semiconductors diamond, silicon, germanium, and \( \alpha \)-tin, thus covering a wide range of energy gap values.

In order to apply this relation to the lead salts, its validity for semiconductors with the rock-salt crystal structure was investigated. The following groups of semiconductors were considered, and values of \( E_o \) were plotted as a function of \( (1/a_o^2) \) for: (1) solid solutions of SnSe in PbSe; (2) solid solutions of SnTe in PbTe; (3) BaS, BaSe, BaTe; (4) CaS, CaSe, CaTe; (5) SrS, SrSe, SrTe.

The values of \( E_o \) (at 12 K) for solid solutions \( \text{Pb}_{(1-x)}\text{Sn}_x\text{Te} \), where \( 0.15 \leq x \leq 0.27 \), were determined by laser emission studies. The energy gap range corresponding to these values of \( x \) is \( 0.106 \text{ eV} \leq E_o \leq 0.044 \text{ eV} \). All solid solutions of SnTe in PbTe have the rock-salt crystal structure, and the linear experimental relation between \( a_o \) and \( x \) was used to determine values of \( a_o \) (at \( \sim 300 \text{ K} \)) corresponding to the values of \( x \) for which \( E_o \) had been measured. These values of \( E_o \) are plotted as a function of \( (1/a_o^2) \) in Figure 1. The horizontal error bars shown were calculated by the author using an estimated uncertainty in \( x \) of \( \pm 3\% \), a value typical of the results of electron beam microprobe analysis. Also shown in Figure 1 are values of \( E_o \) for PbTe of \( 0.190 \text{ eV} \) (at 4 K) and \( 0.186 \text{ eV} \) (at 12 K); the horizontal error bars were also estimated by the author. It is clearly seen from Figure 1 that the empirical relation \( E_o \propto (1/a_o^2) \) holds very well for the cubic solid solutions \( \text{Pb}_{(1-x)}\text{Sn}_x\text{Te} \) in the range \( 0 \leq x \leq 0.27 \).

A similar plot is shown in Figure 2 for solid solutions \( \text{Pb}_{(1-y)}\text{Sn}_y\text{Se} \), which have the cubic rock-salt crystal structure for \( y \leq 0.4 \). Values of \( E_o \)
at 12 K for Pb_{(1-y)}S_{ny}Se, with 0 \leq y \leq 0.276, were also determined by laser emission\textsuperscript{11,12}. The range of values of E\textsubscript{o} corresponding to this range of composition is 0.149 eV \geq E\textsubscript{o} \geq -0.102 eV. The error bars shown correspond to uncertainties estimated by the author. It should be noted that these data cover both positive and negative values of the energy gap E\textsubscript{o} = E(L\textsubscript{6}^-) - E(L\textsubscript{6}^+), where negative values of E\textsubscript{o} correspond to a band structure\textsuperscript{10,11} in which the conduction band edge is an L\textsubscript{6}^+ state and the valence band edge is an L\textsubscript{6}^- state. This band structure is often referred to as inverted relative to the band structures of PbS, PbSe, and PbTe. The values of the lattice constant a\textsubscript{o} of solid solutions Pb_{(1-y)}S_{ny}Se (at \sim 300 K) were calculated using the linear relation between a\textsubscript{o} and y observed\textsuperscript{13} experimentally. From Figure 2 it is again seen that the relation E\textsubscript{o} \propto (1/a\textsubscript{o}^2) is followed very well by these solid solutions of SnSe in PbSe. It is especially interesting that this empirical relation is valid for both positive and negative values of the energy gap. (It should be noted that this relation, shown in Figure 3, holds also for CdTe\textsuperscript{14}, HgTe\textsuperscript{15}, and solid solutions\textsuperscript{16-19} Hg_{(1-x)}Cd\textsubscript{x}Te (0.86 \geq x \geq 0.63) with the zinc-blende structure\textsuperscript{20}, for both positive and negative values of the energy gap.)

The II-VI semiconductors BaS, BaSe, BaTe; CaS, CaSe, CaTe; and SrS, SrSe, SrTe, all have the rock-salt crystal structure\textsuperscript{21}. They have large energy gaps\textsuperscript{22}, with E\textsubscript{o} > 3 eV at \sim 80 K for all nine compounds. These values\textsuperscript{22} of E\textsubscript{o}, however, appear to have been estimated from optical spectra\textsuperscript{23} at \sim 80 K. Since these spectra show strong exciton absorption, the energy gap values for these semiconductors must be regarded as approximate. Figure 4 shows E\textsubscript{o} plotted as a function of (1/a\textsubscript{o}^2), using values\textsuperscript{21} of a\textsubscript{o} at \sim 300 K for these nine semiconductors. While the fit of these points to straight lines is not as good as that of the data in Figures 1 and 2, it seems reasonable to conclude
that the relation $E_\circ \propto (1/a_\circ^2)$ is followed, at least approximately, by these semiconductors.

Based on the results presented in Figures 1, 2, and 4, it is concluded that this empirical relation holds at least as well for compound semiconductors with the NaCl crystal structure as it does for the Group IV elemental semiconductors with the diamond structure. Given this conclusion, it is of interest to apply the relation $E_\circ \propto (1/a_\circ^2)$ to the sequence PbS, PbSe, PbTe, PbPo in order to calculate a value of the energy gap of lead polonide.

III. Calculated Value of the Energy Gap of PbPo

To calculate $E_\circ$ for lead polonide using the known value of $a_\circ$ for PbPo, it is necessary to extrapolate a plot of $E_\circ$ as a function of $(1/a_\circ^2)$ for PbS, PbSe, and PbTe. Using values of $E_\circ$ at 77 K\textsuperscript{9} and at 300 K\textsuperscript{24}, and values\textsuperscript{25} of $a_\circ$ at 300 K, for PbS, PbSe, and PbTe, the plots of $E_\circ$ as a function of $(1/a_\circ^2)$ shown in Figure 5 were made. From the points in Figure 5, it is quite clear that the sequence PbS, PbSe, PbTe does not follow the $E_\circ \propto (1/a_\circ^2)$ relation. However, the straight lines connecting the points for PbS and PbSe have been extrapolated; the points for PbTe have not been used. This choice may be justified in the following manner. In recent papers\textsuperscript{4}, it has been proposed that PbTe is the irregular member of the sequence PbS, PbSe, PbTe, and this irregular nature of PbTe is the reason that $E_\circ (\text{PbTe}) > E_\circ (\text{PbSe})$. In making this proposal, it was pointed out that the outer s-electron energies\textsuperscript{26} of the S, Se, and Po atoms are a linear function of their atomic number, whereas the Te atom 5s electron energy does not lie on this S-Se-Po line. This observation suggests the existence of an empirical regularity in the series of semiconductors PbS-PbSe-PbPo, a regularity not shared by PbTe.
For this reason, and because of their common crystal structure, it is suggested that PbS, PbSe, and PbPo form a regular sequence of related semiconductors with common properties. Specifically, it is assumed that (1) PbS, PbSe, and PbPo have similar band structures, including a direct gap $E_o$ at L; (2) $E_o$ for PbPo is smaller than $E_o$ for PbSe; (3) the empirical relation $E_o \propto (1/a_o^2)$ holds for the sequence PbS, PbSe, PbPo; (4) $E_o$ for PbPo may be determined by an extrapolation of the PbS-PbSe lines on a plot of $E_o$ vs. $(1/a_o^2)$. Figure 5 shows this extrapolation of the PbS-PbSe lines for both 77 K and 300 K. It is seen that both lines intersect the value of $(1/a_o^2)$ for PbPo at negative values of $E_o$. Since the assumption has been explicitly made that the energy gap for PbPo is at the L point, this result implies that, for PbPo, $E_o \equiv [E(L_6^-) - E(L_6^+)] < 0$, leading to the conclusion that $E(L_6^+) > E(L_6^-)$ for PbPo. This result is interpreted as indicating that the band structure of PbPo may be inverted from those of PbS, PbSe, and PbTe, leading to an $L_6^+$ conduction band edge and an $L_6^-$ valence band edge in PbPo.

A second conclusion drawn from Figure 5 concerns the temperature coefficient of the energy gap of PbPo. Since PbS, PbSe, and PbTe all have unusual positive values of $(dE_o/dT)$, it is of particular interest that an inverted band structure implies a negative value of the temperature coefficient of the energy gap of PbPo between 300 K and 77 K. If we let $E'_o \equiv E(L_6^+) - E(L_6^-)$ be the energy gap of PbPo, then from Figure 5, the values of $E'_o$ for PbPo are approximately 0.03 eV and 0.10 eV at 300 K and 77 K, respectively. The temperature coefficient $(dE'_o/dT)$ for PbPo would then have (assuming the usual linear variation of energy gap with temperature) a value of approximately $-3 \times 10^{-4}$ eV/K. This value is typical of the magnitude and sign of the temperature coefficient of the energy gap for most semiconductors. It may also be noted
that this change in the sign of the temperature coefficient from positive to negative, as the energy gap changes sign from positive to negative, has been observed experimentally for solid solutions of SnSe in PbSe.

IV. Calculated Carrier Effective Masses in PbPo

It has been shown that experimental values of longitudinal and transverse effective masses and of the energy gap for PbTe do not follow the same f-sum rule as do the corresponding data for PbS and PbSe. This result implies that the f-sum matrix element (considering for simplicity a two-band f-sum with only one term) is the same for PbS and PbSe. If the assumption (equivalent to assumption (1) in Section III) is now made that PbPo follows the same f-sum rule as do PbS and PbSe, effective mass values for PbPo may be calculated using values of the f-sum matrix elements previously determined for PbS and PbSe. For a band model involving only the \( L^+ \) conduction band and \( L^- \) valence band of PbPo, the effective mass \( m^* \) of electrons in the \( L^- \) band is given by

\[
m^*/(m - m^*) = \frac{m}{2} |M_j|^2 E',
\]

where \( E' = E(L^+) - E(L^-) \), \( M_j \) is the f-sum matrix element, \( j = \) longitudinal (L) or transverse (T), and \( m \) is the free electron mass. For holes in the \( L^- \) band, the negative sign on the left hand side of equation (1) is replaced by a plus sign. Using values of \( |M_L^+| \) and \( |M_T^-| \) obtained for electrons and holes in PbS and PbSe, the longitudinal and transverse effective masses \( m^*_L \) and \( m^*_T \) were calculated using \( E' = 0.1 \text{ eV} \) and assuming the (inverted) band structure proposed for PbPo. For electrons (\( L^+ \) band), \( |M_L^+| = 3.32 \), \( |M_T^-| = 4.32 \); for holes (\( L^- \) band), \( |M_L^-| = 3.26 \), \( |M_T^-| = 4.08 \); all in units of \( 10^{-14} \text{ g}^{1/2} \cdot (\text{eV})^{1/2} \).

The calculated effective mass values are shown in Table I, and are
appropriate for 80 K.

Table I. Calculated Effective Masses in PbPo

<table>
<thead>
<tr>
<th>Carrier</th>
<th>(m_e^*/m)</th>
<th>(m_h^*/m)</th>
<th>(m_c^*/m)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Electrons</td>
<td>0.024</td>
<td>0.040</td>
<td>0.029</td>
</tr>
<tr>
<td>Holes</td>
<td>0.028</td>
<td>0.045</td>
<td>0.032</td>
</tr>
</tbody>
</table>

Since PbS and PbSe have ellipsoidal surfaces of constant energy it is reasonable to assume the same for PbPo, and the values of the conductivity effective mass \(m_e^* = (3m_h^*m_t^*)/(2m_h^* + m_t^*)\) for PbPo shown in Table I were so calculated. It should be noted that the calculated values of \(m_h^*\) and \(m_t^*\) for PbPo are smaller than the corresponding values for PbS and PbSe. This is a direct consequence of the assumed appropriateness of the f-sum rule, since the effective mass so calculated will vary directly with the energy gap of the semiconductor.

V. Relation to the Energy Gap Anomaly in the PbS Group

As mentioned earlier, the fact that \(E_o(PbTe)\) is larger than \(E_o(PbSe)\) is an anomaly in that \(E_o\) does not exhibit the usual monotonic decrease with anion atomic number. The proposal that PbTe is the irregular member of the sequence was based on an examination of the f-sum rule at the conduction and valence band edges in PbS, PbSe, and PbTe. The fact that PbTe does not follow the same f-sum rule as do PbS and PbSe is interpreted as indicating that the f-sum matrix element for PbTe is different from that for PbS and PbSe. This effect is ascribed to a qualitative difference in the \(L^6\) conduction band edge state for PbTe, reflecting the irregular value of the Te atom.
5s electron energy, which is responsible also for the anomalously large value of $E_o^{\prime}(\text{PbTe})$.

An experimental study of $E_o^{\prime}$ and $(dE_o^{\prime}/dT)$ for PbPo would provide interesting evidence concerning the validity of the premises and conclusions mentioned above. The properties herein proposed for the band structure of PbPo $[E(L_6^+) > E(L_6^-), (dE_o^{\prime}/dT) < 0]$ stem directly from the proposal above concerning the irregular nature of PbTe. This proposal was the justification for deriving the properties of PbPo by extrapolation of the properties of PbS and PbSe alone. Should experiment confirm the properties suggested for PbPo, it would provide corroborative evidence regarding the irregular nature of PbTe. Further, an experimental determination of carrier effective masses in PbPo in agreement with the values calculated in this paper would provide indirect confirmation of the proposed value of the energy gap of PbPo. Such agreement would then also confirm the applicability of the PbS-PbSe f-sum rule to PbPo and thus would also confirm the appropriateness of the extrapolation shown in Figure 5. If observed, then, experimental values of effective masses in PbPo in agreement with the calculations of this paper would provide further information concerning the interesting energy gap anomaly in the lead salt group. For these reasons, it is suggested that experimental determinations of the energy gap, its temperature coefficient, and effective masses in PbPo would be very worthwhile studies.

Acknowledgement

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References


5. T.S. Moss, "Optical Properties of Semiconductors", (Academic, New York, 1959), p. 49, is one of the few authors explicitly mentioning this empirical relation.


12. It may be noted that the value of $E_0$ at 12 K determined in this way for
PbSe is \( E_0 = 0.149 \) eV, differing from the value \( E_0 = 0.145 \) eV) determined by interband magneto-absorption studies.  

Figure Captions

Figure 1. $E_o$ plotted as a function of $(1/a_0^2)$ for solid solutions of SnTe in PbTe.

Figure 2. $E_o$ plotted as a function of $(1/a_0^2)$ for solid solutions of SnSe in PbSe.

Figure 3. $E_G = E(\Gamma_6) - E(\Gamma_8)$ plotted as a function of $(1/a_0^2)$ for solid solutions of HgTe in CdTe.

Figure 4. Energy gap plotted as a function of $(1/a_0^2)$ for CaS, CaSe, CaTe; SrS, SrSe, SrTe; BaS, BaSe, BaTe.

Figure 5. $E_o$ plotted as a function of $(1/a_0^2)$ for PbS, PbSe, PbTe, and PbPo.

Tables

Table I. Calculated Effective Masses in PbPo.
\( \text{Pb}_{(1-x)} \text{Sn}_x \text{Te} \)

\[ 0 \leq x \leq 0.27 \]

\text{NaCl Crystal Structure}
$E_0 = E(L_6^+) - E(L_6^-)$, 12 K (eV)

$Pb_{(1-y)}Sn_ySe$

$0 \leq y \leq 0.28$

NaCl Crystal Structure

$\frac{1}{a_0^2}$, $10^{14}$ cm$^{-2}$, 300K
$E_6 = E(T_6) - E(T_8)$, eV

$E = E(T_6) - E(T_8)$, eV

$E_0 = E(T_0) - E(T_8)$, eV

$E_0 = E(T_0) - E(T_8)$, eV

Hg$_x$Cd$_{(1-x)}$Te Solid Solutions

$0 \leq x \leq 1$

Zinc Blende Crystal Structure

- $T = 4$ K
- $T = 12$ K
- $T = 30$ K
- $T = 77$ K

CdTe

HgTe

$(l/a_0^2), 10^{14}$ cm$^{-2}$, 300 K
\[ E_0 = E(L_6^0) - E(L_6^+), \text{ eV} \]

- 300°K
- 77°K

\( \frac{1}{a_0^2} \) for PbPb

\[ \left( \frac{1}{a_0^2} \right) \text{, } 10^{14} \text{ cm}^{-2}, \text{ 300 K} \]
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