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Authors
Aubert, B
Bona, M
Karyotakis, Y
et al.

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Search for $b \to u$ transitions in $B^0 \to D^0 K^{*0}$ decays

B. Aubert,1 M. Bona,1 Y. Karyotakis,1 J. P. Lees,1 V. Poireau,1 E. Prencipe,1 X. Prudent,1 V. Tisserand,1 J. Garra Tico,2 E. Grauges,2 L. Lopez,3a,b A. Palano,3a,b M. Pappalardo,3a,b G. Eigen,4 B. Stugu,4 L. Sun,4 G. S. Abrams,5 M. Battaglia,5 D. N. Brown,5 R. N. Cahn,5 R. G. Jacobsen,5 L. T. Kerth,5 Yu. G. Kolomensky,5 G. Lynch,5 I. L. Osipenkov,5 M. T. Ronan,5,6 K. Tackmann,5 T. Tanabe,5 C. M. Hawkess,6 N. Soni,6 A. T. Watson,6 H. Koch,7 T. Schroeder,7 D. Walker,8 D. J. Asgeirsson,9 B. G. Fulsom,9 L. Lopez,3a,b A. Palano,3a,b M. Pappalardo,3a,b G. Eigen,4 B. Stugu,4 L. Sun,4 G. S. Abrams,5 M. Battaglia,5 D. N. Brown,5 R. N. Cahn,5 R. G. Jacobsen,5 L. T. Kerth,5 Yu. G. Kolomensky,5 G. Lynch,5 I. L. Osipenkov,5 M. T. Ronan,5,6 K. Tackmann,5 T. Tanabe,5 C. M. Hawkess,6 N. Soni,6 A. T. Watson,6 H. Koch,7 T. Schroeder,7 D. Walker,8 D. J. Asgeirsson,9 B. G. Fulsom,9 L. Lopez,3a,b A. Palano,3a,b M. Pappalardo,3a,b G. Eigen,4 B. Stugu,4 L. Sun,4 G. S. Abrams,5 M. Battaglia,5 D. N. Brown,5 R. N. Cahn,5 R. G. Jacobsen,5 L. T. Kerth,5 Yu. G. Kolomensky,5 G. Lynch,5 I. L. Osipenkov,5 M. T. Ronan,5,6 K. Tackmann,5 T. Tanabe,5 C. M. Hawkess,6 N. Soni,6 A. T. Watson,6 H. Koch,7 T. Schroeder,7 D. Walker,8 D. J. Asgeirsson,9 B. G. Fulsom,9 L. Lopez,3a,b A. Palano,3a,b M. Pappalardo,3a,b G. Eigen,4 B. Stugu,4 L. Sun,4 G. S. Abrams,5 M. Battaglia,5 D. N. Brown,5 R. N. Cahn,5 R. G. Jacobsen,5 L. T. Kerth,5 Yu. G. Kolomensky,5 G. Lynch,5 I. L. Osipenkov,5 M. T. Ronan,5,6 K. Tackmann,5 T. Tanabe,5 C. M. Hawkess,6 N. Soni,6 A. T. Watson,6 H. Koch,7 T. Schroeder,7 D. Walker,8 D. J. Asgeirsson,9 B. G. Fulsom,9 L. Lopez,3a,b A. Palano,3a,b M. Pappalardo,3a,b G. Eigen,4 B. Stugu,4 L. Sun,4 G. S. Abrams,5 M. Battaglia,5 D. N. Brown,5 R. N. Cahn,5 R. G. Jacobsen,5 L. T. Kerth,5 Yu. G. Kolomensky,5 G. Lynch,5 I. L. Osipenkov,5 M. T. Ronan,5,6 K. Tackmann,5 T. Tanabe,5 C. M. Hawkess,6 N. Soni,6 A. T. Watson,6 H. Koch,7 T. Schroeder,7 D. Walker,8

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31Humboldt-Universität zu Berlin, Institut für Physik, Newtonstr. 15, D-12489 Berlin, Germany
32Imperial College London, London, SW7 2AZ, United Kingdom
33University of Iowa, Iowa City, Iowa 52242, USA
34Iowa State University, Ames, Iowa 50011-3160, USA
35Johns Hopkins University, Baltimore, Maryland 21218, USA
36Laboratoire de l’Accélérateur Linéaire, IN2P3/CNRS et Université Paris-Sud 11, Centre Scientifique d’Orsay, B. P. 34, F-91898 Orsay Cedex, France
37Lawrence Livermore National Laboratory, Livermore, California 94550, USA
38University of Liverpool, Liverpool L69 7ZE, United Kingdom
39Queen Mary, University of London, London, E1 4NS, United Kingdom
40University of London, Royal Holloway and Bedford New College, Egham, Surrey TW20 0EX, United Kingdom
41University of Louisville, Louisville, Kentucky 40292, USA
42Johannes Gutenberg-Universität Mainz, Institut für Kernphysik, D-55099 Mainz, Germany
43University of Manchester, Manchester M13 9PL, United Kingdom
44University of Maryland, College Park, Maryland 20742, USA
45University of Massachusetts, Amherst, Massachusetts 01003, USA
46Massachusetts Institute of Technology, Laboratory for Nuclear Science, Cambridge, Massachusetts 02139, USA
47McGill University, Montréal, Québec, Canada H3A 2T8
48aINFN Sezione di Milano, I-20133 Milano, Italy
48bDipartimento di Fisica, Università di Milano, I-20133 Milano, Italy
49University of Mississippi, University, Mississippi 38677, USA
50Université de Montréal, Physique des Particules, Montréal, Québec, Canada H3C 3J7
51Mount Holyoke College, South Hadley, Massachusetts 01075, USA
52aINFN Sezione di Napoli, I-80126 Napoli, Italy
52bDipartimento di Scienze Fisiche, Università di Napoli Federico II, I-80126 Napoli, Italy
53NIKHEF, National Institute for Nuclear Physics and High Energy Physics, NL-1009 DB Amsterdam, The Netherlands
54University of Notre Dame, Notre Dame, Indiana 46556, USA
55Ohio State University, Columbus, Ohio 43210, USA
56University of Oregon, Eugene, Oregon 97403, USA
57aINFN Sezione di Padova, I-35131 Padova, Italy
57bDipartimento di Fisica, Università di Padova, I-35131 Padova, Italy
58Laboratoire de Physique Nucléaire et de Hautes Énergies, IN2P3/CNRS, Université Pierre et Marie Curie-Paris6, Université Denis Diderot-Paris7, F-75252 Paris, France
59University of Pennsylvania, Philadelphia, Pennsylvania 19104, USA
60aINFN Sezione di Perugia, I-06100 Perugia, Italy
60bDipartimento di Fisica, Università di Perugia, I-06100 Perugia, Italy
61aINFN Sezione di Pisa, I-56127 Pisa, Italy
61bDipartimento di Fisica, Università di Pisa, I-56127 Pisa, Italy
61cScuola Normale Superiore di Pisa, I-56127 Pisa, Italy
62Princeton University, Princeton, New Jersey 08544, USA
63aINFN Sezione di Roma, I-00185 Roma, Italy
63bDipartimento di Fisica, Università di Roma La Sapienza, I-00185 Roma, Italy
64Universität Rostock, D-18051 Rostock, Germany
65Rutherford Appleton Laboratory, Chilton, Didcot, Oxon, OX11 0QX, United Kingdom
66CEA, Irfi, SPP, Centre de Saclay, F-91191 Gif-sur-Yvette, France
67University of South Carolina, Columbia, South Carolina 29208, USA
68Stanford Linear Accelerator Center, Stanford, California 94309, USA
69Stanford University, Stanford, California 94305-4060, USA
70State University of New York, Albany, New York 12222, USA
71University of Tennessee, Knoxville, Tennessee 37996, USA
72University of Texas at Austin, Austin, Texas 78712, USA
73University of Texas at Dallas, Richardson, Texas 75083, USA
74INFN Sezione di Torino, I-10125 Torino, Italy

*Deceased.
†Now at Temple University, Philadelphia, PA 19122, USA.
‡Now at Tel Aviv University, Tel Aviv, 69978, Israel.
§Also with Università di Perugia, Dipartimento di Fisica, Perugia, Italy.
¶Also with Università di Roma La Sapienza, I-00185 Roma, Italy.
‖Now at University of South Alabama, Mobile, AL 36688, USA
*Also with Università di Sassari, Sassari, Italy.
We present a study of the decays $B^0 \to D^0 K^{*0}$ and $B^0 \to \bar{D}^0 K^{*0}$ with $K^{*0} \to K^+ \pi^-$. The $D^0$ and the $\bar{D}^0$ mesons are reconstructed in the final states $f = K^+ \pi^-$, $K^+ \pi^- \pi^0$, $K^+ \pi^- \pi^+ \pi^-$, and their charge conjugates. Using a sample of $465 \times 10^6 B\bar{B}$ pairs collected with the BABAR detector at the PEP-II asymmetric-energy $e^+e^-$ collider at SLAC, we measure the ratio $R_{\text{ADS}} = [\Gamma(B^0 \to [f]_D K^{*0}) + \Gamma(B^0 \to [\bar{f}]_D K^{*0})]/[\Gamma(B^0 \to [f]_D K^{*0}) + \Gamma(B^0 \to [\bar{f}]_D K^{*0})]$ for the three final states. We do not find significant evidence for a signal and set the following limits at 95\% probability: $R_{\text{ADS}}(K\pi\pi) < 0.244$, $R_{\text{ADS}}(K\pi\pi\pi) < 0.181$, and $R_{\text{ADS}}(K\pi\pi\pi) < 0.391$. From the combination of these three results, we find that the ratio $r_S$ between the $b \to u$ and the $b \to c$ amplitudes lies in the range $[0.07, 0.41]$ at 95\% probability.

Various methods have been proposed to determine the unitarity triangle angle $\gamma$ [1–3] of the Cabibbo-Kobayashi-Maskawa (CKM) quark mixing matrix [4] using $B^- \to D^{(*)0} K^{(*)-}$ decays, where the symbol $D^{(*)0}$ indicates either a $D^0$ or a $\bar{D}^0$ meson. A $B^-$ meson can decay into a $D^{(*)0} K^{(*)-}$ final state via a $b \to c$ or a $b \to u$ process. CP violation may occur due to interference between the amplitudes when the $D^{(*)0}$ and $\bar{D}^{(*)0}$ decay to the same final state. These processes are thus sensitive to $\gamma = \arg\{-V_{ub}^* V_{cd}/V_{cb}^* V_{cd}\}$. The sensitivity to $\gamma$ is proportional to the ratio between the $b \to u$ and $b \to c$ transition amplitudes ($r_B$), which depends on the $B$ decay channel and needs to be determined experimentally.

In this paper we consider an alternative approach, based on neutral $B$ mesons, which is similar to the Atwood-Dunietz-Soni (ADS) method [2] originally proposed for charged $B^- \to D^{(*)0} K^{(*)-}$ decays. We consider the decay channel $B^0 \to \bar{D}^0 K^{*0}$ with $K^{*0} \to K^+ \pi^-$ [charge conjugate processes are assumed throughout the paper and $K^{*0}$ refers to the $K'(892)$]. This final state can be reached through $b \to c$ and $b \to u$ processes as shown in Fig. 1. The flavor of the $B$ meson is identified by the charge of the kaon produced in the $K^{*0}$ decay. The neutral $D$ mesons are reconstructed in three final states, $f = K^+ \pi^-$, $K^+ \pi^- \pi^0$, $K^+ \pi^- \pi^+ \pi^-$. We search for $B^0 \to [\bar{f}]_D [K^+ \pi^-]_{K^{*0}}$ events, where the CKM-favored $B^0 \to \bar{D}^0 K^{*0}$ decay, followed by the doubly Cabibbo-suppressed $\bar{D}^0 \to \bar{f}$ decay, interferes with the CKM-suppressed $B^0 \to D^0 K^{*0}$ decay, followed by the Cabibbo-favored $D^0 \to f$ decay. These are called “opposite-sign” events because the two kaons in the final state have opposite charges. We also reconstruct a larger sample of “same-sign” events, which mainly arise from CKM-favored $B^0 \to \bar{D}^0 K^{*0}$ decays followed by Cabibbo-favored $\bar{D}^0 \to f$ decays.

In order to reduce the systematic uncertainties, we measure ratios of decay rates

$$R_{\text{ADS}} = \frac{\Gamma(B^0 \to [f]_D K^{*0}) + \Gamma(B^0 \to [\bar{f}]_D K^{*0})}{\Gamma(B^0 \to [f]_D K^{*0}) + \Gamma(B^0 \to [\bar{f}]_D K^{*0})},$$

(1)

$$A_{\text{ADS}} = \frac{\Gamma(B^0 \to [f]_D K^{*0}) - \Gamma(B^0 \to [\bar{f}]_D K^{*0})}{\Gamma(B^0 \to [f]_D K^{*0}) + \Gamma(B^0 \to [\bar{f}]_D K^{*0})},$$

(2)

where $R_{\text{ADS}}$ is the ratio between opposite- and same-sign events.

The $K^{*0}$ resonance has a natural width (50 MeV/c$^2$) that is larger than the experimental resolution. This introduces a phase difference between the various amplitudes. We therefore introduce effective variables $r_S$, $k$, and $\delta_S$ [5], obtained by integrating over the region of the $B^0 \to \bar{D}^0 K^+ \pi^-$ Dalitz plot dominated by the $K^{*0}$ resonance, defined as follows:

$$r_S^2 = \frac{\Gamma(B^0 \to D^0 K^+ \pi^-)}{\Gamma(B^0 \to \bar{D}^0 K^+ \pi^-)} = \frac{\int dp A_S^2(p)}{\int dp A_S^2(p)},$$

(3)

$$k e^{i\delta_S} = \frac{\int dp A_S(p) A_{\bar{S}}(p) e^{i\delta(p)}}{\int dp A_S^2(p) \int dp A_{\bar{S}}^2(p)}.$$  (4)

From their definition, $0 \leq k \leq 1$ and $\delta_S \in [0, 2\pi]$. The amplitudes for the $b \to c$ and $b \to u$ transitions, $A_{\bar{S}}(p)$ and $A_S(p)$, are real and positive and $\delta(p)$ is the relative strong phase. The variable $p$ indicates the position in the

FIG. 1. Feynman diagrams for $B^0 \to D^0 K^{*0}$ (left, $b \to c$ transition) and $B^0 \to \bar{D}^0 K^{*0}$ (right, $b \to \bar{u}$ transition).
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$\bar{D}^0 K^+ \pi^-$ Dalitz plot. The parameter $k$ accounts for contributions, in the $K^{*0}$ mass region, of higher-mass resonances. In the case of a two-body $B$ decay, $r_S$ and $\delta_S$ become $r_B = A_u/A_D$ and $\delta_B$ (the strong phase difference between $A_u$ and $A_D$) with $k = 1$. As shown in [6], the distribution of $k$ can be obtained by simulation studies based on realistic models for the different resonance contributions to the decays of neutral $B$ mesons into $\bar{D}^0 K^+ \pi^-$ final states. When considering the region in the $B^0 \rightarrow \bar{D}^0 K^+ \pi^-$ Dalitz plane where the invariant mass of the kaon and the pion is within 48 MeV/$c^2$ of the nominal $K^{*0}$ mass [7], the distribution of $k$ is narrow, and is centered at 0.95 with a root-mean-square width of 0.03.

Because of CKM factors and the fact that both diagrams in Fig. 1 are color-suppressed, the average amplitude ratio $r_S$ in $B^0 \rightarrow \bar{D}^0 K^{*0}$ is expected to be of order 0.3, larger than the analogous ratio for the charged $B^- \rightarrow D^{(*)-} K^- \pi^-$ decays, which is of order 0.1 [8,9]. This implies better sensitivity to $\gamma$ for the same number of events, an expectation that applies to all $B^0 \rightarrow D^{(*)0} K^{(*)-}$ decays, and that motivates the use of neutral $B$ meson decays to determine $\gamma$. Currently, the experimental knowledge of $r_S$ [6,10] is $r_S < 0.54$ at 95% probability.

The ratios $R_{ADS}$ and $A_{ADS}$ are related to $r_S$, $\gamma$, $k$, and $\delta_S$ through the following relations:

$$R_{ADS} = r_S^2 + r_D^2 + 2kk_D r_S r_D \cos \gamma \cos(\delta_S + \delta_D),$$

$$A_{ADS} = 2kk_D r_S r_D \sin \gamma \sin(\delta_S + \delta_D)/R_{ADS},$$

where

$$r_D^2 = \frac{\Gamma(D^0 \rightarrow f)}{\Gamma(D^0 \rightarrow \bar{f})} = \frac{\int dm A_{DCS}^2(m)}{\int dm A_{CF}^2(m)},$$

$$k_D e^{i\delta_D} = \frac{\int dm A_{CF}(m) A_{ADS}(m) e^{i\delta(m)}}{\sqrt{\int dm A_{CS}^2(m) \int dm A_{CS}^2(m)}},$$

with $0 \leq k_D \leq 1$, $\delta_D \in [0, 2\pi]$, $A_{CF}(m)$ and $A_{ADS}(m)$ the magnitudes of the Cabibbo-favored and the doubly Cabibbo-suppressed amplitudes, $\delta$ the relative strong phase, and the variable $m$ the position in the $D$ Dalitz plot. In the case of a two-body $D$ decay, $k_D = 1$, $r_D$ is the ratio between the doubly Cabibbo-suppressed and the Cabibbo-favored decay amplitudes and $\delta_D$ is the relative strong phase.

Determining $r_S$, $\gamma$, and $\delta_S$ from the measurements of $R_{ADS}$ and $A_{ADS}$, with the factor $k$ fixed, requires knowledge of the parameters $(k_D, r_D, \delta_D)$, which depend on the specific neutral $D$ meson final states. The ratios $r_D$ for the three $D$ decay modes have been measured [7], as has the strong phase $\delta_D$ for the $K \pi$ mode [11]. In addition, experimental information is available on $k_D$ and $\delta_D$ for the $K \pi \pi^0$ and $K \pi \pi \pi$ modes [12]. The smallness of the $r_D$ ratios implies good sensitivity to $r_S$ from a measurement of $R_{ADS}$. For the same reason, and since, with the present statistics, the asymmetries $A_{ADS}$ cannot be extracted from data, the sensitivity to $\gamma$ is reduced. The aim of this analysis is therefore the measurement of $r_S$. In the future, good knowledge of all the $r_D$, $k_D$, and $\delta_D$ parameters, and a precise measurement of the $R_{ADS}$ ratios for the three channels, will allow $\gamma$ and $\delta_S$ to be determined from this method as well.

The results presented here are obtained with 423 fb$^{-1}$ of data collected at the $Y(4S)$ resonance with the BABAR detector at the PEP-II $e^+e^-$ collider at SLAC [13], corresponding to $465 \times 10^6 \bar{B}B$ events. An additional “off-resonance” data sample of 41.3 fb$^{-1}$, collected at a center-of-mass (CM) energy 40 MeV below the $Y(4S)$ resonance, is used to study backgrounds from continuum events, $e^+e^- \rightarrow q\bar{q}$ ($q = u, d, s$, or $c$). The BABAR detector is described elsewhere [14].

The event selection is based on studies of off-resonance data and Monte Carlo (MC) simulations of continuum and $e^+e^- \rightarrow Y(4S) \rightarrow BB$ events. All the selection criteria are optimized by maximizing the function $S/\sqrt{S+B}$ on opposite-sign events, where $S$ and $B$ are the expected numbers of opposite-sign signal and background events, respectively.

The neutral $D$ mesons are reconstructed from a charged kaon and one or three charged pions and, in the $K \pi \pi^0$ mode, a neutral pion. The $\pi^0$ candidates are reconstructed from pairs of photon candidates, each with energy greater than 70 MeV, total energy greater than 200 MeV, and invariant mass in the interval $[118, 145]$ MeV/$c^2$. The $\pi^0$ candidate’s mass is subsequently constrained to its nominal value [7].

The invariant mass of the particles used to reconstruct the $D$ is required to lie within $14$ MeV/$c^2$ ($\approx 1.9\sigma$), 20 MeV/$c^2$ ($\approx 1.5\sigma$), and 9 MeV/$c^2$ ($\approx 1.6\sigma$) of the nominal $D^0$ mass, for the $K \pi$, $K \pi \pi^0$, and $K \pi \pi \pi$ modes, respectively. For the $K \pi \pi \pi$ mode we also require that the tracks originate from a single vertex with a probability greater than 0.1%.

The tracks used to reconstruct the $K^{*0}$ are constrained to originate from a common vertex and their invariant mass is required to lie within 48 MeV/$c^2$ of the nominal $K^{*0}$ mass [7]. We define $\theta_H$ as the angle between the direction of flight of the $K$ and $B$ in the $K^{*0}$ rest frame. The distribution of $\cos \theta_H$ is proportional to $\cos^2 \theta_H$ for signal events and is expected to be flat for background events. We require $|\cos \theta_H| > 0.3$. The charged kaons used to reconstruct the $\bar{D}^0$ and $K^{*0}$ mesons are required to satisfy kaon identification criteria, based on Cherenkov angle and $dE/dx$ measurements and are typically 85% efficient, depending on momentum and polar angle. Misidentification rates are at the 2% level.

The $B^0$ candidates are reconstructed by combining a $\bar{D}^0$ and $K^{*0}$ candidate, constraining them to originate from a common vertex with a probability greater than 0.1%. In forming the $B$, the $D$ mass is constrained to its nominal value [7]. The distribution of the cosine of the $B$ polar
angle with respect to the beam axis in the $e^+e^-$ CM frame $\cos \theta_B$ is expected to be proportional to $1 - \cos^2 \theta_B$. We require $|\cos \theta_B| < 0.9$. We measure two almost independent kinematic variables: the beam-energy substituted mass $m_{ES} = \sqrt{(E_0^2/2 + p_0 \cdot p_B)^2/E_0 - p_B^2}$, and the energy difference $\Delta E = E_B - E_0/2$, where $E$ and $p$ are energy and momentum, the subscripts $B$ and $0$ refer to the candidate $B$ and $e^+e^-$ system, respectively, and the asterisk denotes the $e^+e^-$ CM frame. The distributions of $m_{ES}$ and $\Delta E$ peak at the $B$ mass and zero, respectively, for correctly reconstructed $B$ mesons. The $B$ candidates are required to have $\Delta E$ in the range $[-16, 16]$ MeV ($\approx 1.3\sigma$), $[-20, 20]$ MeV ($\approx 1.5\sigma$), and $[-19, 19]$ MeV ($\approx 1.4\sigma$) for the $K\pi$, $K\pi\pi^0$, and $K\pi\pi\pi$ modes, respectively. Finally we consider events with $m_{ES}$ in the range $[5.20, 5.29]$ GeV/$c^2$.

We examine background $B$ decays that have the same final state reconstructed particles as the signal decay to identify modes with peaking structure in $m_{ES}$ or $\Delta E$ that can potentially mimic signal events. We identify three such “peaking background” modes in the opposite-sign sample: $B^0 \rightarrow D^+ [K^{*0}K^-] \pi^+$ (for $K\pi$), $B^0 \rightarrow D^+ [K^{*0}K^-] \pi^+ \pi^0$ (for $K\pi\pi^0$), and $B^0 \rightarrow D^+ [K^{*0}K^-] \pi^+ a_1^+ (\pi^+ \pi^-)$ (for $K\pi\pi\pi$). To reduce their contribution we veto all candidates for which the invariant mass of the $K^{*0}$ and the $K^-$ from the $D^0$ lies within 6 MeV/$c^2$ of the nominal $D^*$ mass.

After imposing the vetoes, the contributions of the peaking backgrounds to the $K\pi$, $K\pi\pi^0$, and $K\pi\pi\pi$ samples are predicted to be less than 0.07, 0.05, and 0.12 events, respectively, at 95% probability. Other possible sources of peaking background are $B^0 \rightarrow D^0 \rho^0$ and $B^0 \rightarrow D^{+ -} [D^0 \pi^-] \pi^+$, which contribute to the three decay modes in both the same- and opposite-sign samples. These events could be reconstructed as signal, due to misidentification of a $\pi$ as a $K$. We impose additional restrictions on the identification criteria of charged kaons from $K^0$ decays to reduce the contribution of these backgrounds to a negligible level. Charmless $B$ decays, like $B^0 \rightarrow K^{*0}K\pi$, can also contribute. The number of expected charmless background events, evaluated with data from the $D^0$ mass sidebands, is $N_{peak} = 0.5 \pm 0.5$ (0.1 $\pm$ 1.2) in the same (opposite) sign samples.

In case of multiple $D$ candidates (less than 1% of events), we choose the one with reconstructed $D^0$ mass closest to the nominal mass [7]. In the case of two $B$ candidates reconstructed from the same $D^0$, we choose the candidate with the largest value of $|\cos \theta_B|$.

The overall reconstruction efficiencies for signal events are (13.2 $\pm$ 0.1)% for the $K\pi$, $K\pi\pi^0$, and $K\pi\pi\pi$ modes, respectively.

After applying the selection criteria described above, the remaining background is composed of continuum events and combinatorial $BB$ events. To discriminate against the continuum background events (the dominant background component), which, in contrast to $BB$ events, have a jetlike shape, we use a Fisher discriminant $F$ [15]. The discriminant $F$ is a linear combination of four variables calculated in the CM frame. The first discriminant variable is the cosine of the angle between the $B$ thrust axis and the thrust axis of the rest of the event. The second and third variables are $L_0 = \sum p_i$, and $L_2 = \sum |p_i| \cos \theta_i |^2$, where the index $i$ runs over all the reconstructed tracks and energy deposits in the calorimeter not associated with a track, the tracks and energy deposits used to reconstruct the $B$ are excluded, $p_i$ is the momentum, and $\theta_i$ is the angle with respect to the thrust axis of the $B$ candidate. The fourth variable is $|\Delta t|$, the absolute value of the measured proper time interval between the $B$ and $B$ decays, calculated from the measured separation between the decay points of the $B$ and $\bar{B}$ along the beam direction.

The coefficients of $F$, chosen to maximize the separation between signal and continuum background, are determined using samples of simulated signal and continuum events and validated using off-resonance data.

The signal and background yields are extracted, separately for each channel, by maximizing the extended likelihood $L = (e^{-N})/(N!) \cdot N^{N} \cdot \prod_{j=1}^{N} f(x_j | \theta, N')$. Here $x_j = \{m_{ES}, F\}$, $\theta$ is a set of parameters, $N$ is the number of events in the selected sample, and $N'$ is the expectation value for the total number of events. The term $f(x | \theta, N')$ is defined as

$$f(x | \theta, N') = \frac{N_{DK} \cdot f_{OS}(x | \theta_{SIG}) + N_{DK'} \cdot f_{SIG}(x | \theta_{SIG})}{1 + N_{ADS} \cdot f_{SIG}(x | \theta_{SIG}) + N_{SS} \cdot f_{SS}(x | \theta_{SS}) + N_{cont} \cdot f_{cont}(x | \theta_{cont})} + \frac{N_{OS} \cdot f_{OS}(x | \theta_{OS}) + N_{SS} \cdot f_{SS}(x | \theta_{SS})}{1 + N_{OS} \cdot f_{OS}(x | \theta_{os}) + N_{SS} \cdot f_{SS}(x | \theta_{ss})},$$

where $N_{DK}$ is the total number of signal events, $R_{ADS}$ is the ratio between opposite- and same-sign signal events, and $N_{cont}$, $N_{cont}^{SS}$, $N_{cont}^{OS}$, and $N_{cont}^{OS}$ are the number of same- and opposite-sign events for continuum and $BB$ backgrounds. The probability density functions (PDFs) $f$ are derived from MC and are defined as the product of one-dimensional distributions of $m_{ES}$ and $F$. The $m_{ES}$ distributions are modeled with a Gaussian for signal, and threshold functions with different parameters for the continuum and $BB$ backgrounds. The threshold function is expressed as follows:

$$A(x) = x_0 \sqrt{1 - \left(\frac{x}{x_0}\right)^2} \cdot e^{(1-(x/x_0)^2)^2},$$

where $x_0$ represents the maximum allowed value for the variable $x$ described by $A(x)$ and $c$ accounts for the shape of the distribution. The $F$ distributions are modeled with Gaussians.

From the fit to data we extract $N_{DK}$, $R_{ADS}$, and the background yields ($N_{SS}$, $N_{cont}^{SS}$, $N_{cont}^{OS}$, and $N_{cont}^{OS}$). We allow
the mean of the signal $m_{ES}$ PDF and parameters of the continuum $m_{ES}$ PDFs to float.

The fitting procedure is validated using ensembles of simulated events. A large number of pseudoeperiments is generated with probability density functions and parameters as obtained from the fit to the data. The fitting procedure is then performed on these samples. We find no bias on the number of fitted events for any of the components.

The results for $N_{DK^*}$, $R_{ADS}$, and the background yields are summarized in Table I. The total number of oppositesign signal events in the three channels is $N_{SS} = 24.4^{+10.9}_{-10.0}$ (statistical uncertainty only). Projections of the fit onto the variable $m_{ES}$ are shown in Fig. 2 for the opposite- and same-sign samples. To enhance the visibility of the signal, events are required to satisfy $\mathcal{F} > 0.5$ for $K\pi$, $\mathcal{F} > 0.7$ for $K\pi\pi^0$, and $\mathcal{F} > 1$ for $K\pi\pi\pi$. These requirements have an efficiency of about 67%, 67%, and 50% for signal and 9%, 5%, and 3% for continuum background.

The systematic uncertainties on $R_{ADS}$ are summarized in Table II. To evaluate the contributions related to the $m_{ES}$ and $\mathcal{F}$ PDFs, we repeat the fit by varying all the PDF parameters that are fixed in the final fit within their statistical errors, as obtained from the parametrization on simulated events. To evaluate the uncertainty arising from the assumption of negligible peaking background contributions, we repeat the fit by varying the number of these events within their statistical errors. In this evaluation, we consider all the possible sources of such backgrounds, coming from charmless $B$ decays and from $B$ decays with a $D$ meson in the final state, as discussed above. For the multibody $D$ decays, the selection efficiency on same- and opposite-sign events has been confirmed to be the same, regardless of the difference in the Dalitz structure, within a relative error of 3%. Finally, a systematic uncertainty associated with cross feed between same- and opposite-sign events is evaluated from MC studies to be $(3.5 \pm 0.5)\%$, $(4.6 \pm 0.6)\%$, and $(1.9 \pm 0.4)\%$ for the $K\pi$, $K\pi\pi^0$, and $K\pi\pi\pi$ modes, respectively. The total systematic uncertainties are defined by adding the individual terms in quadrature.

The final likelihood $\mathcal{L}(R_{ADS})$ for each decay mode is obtained by convolving the likelihood returned by the fit with a Gaussian whose width equals the systematic uncertainty. Figure 3 shows $\mathcal{L}(R_{ADS})$ for all three channels, where we exclude the unphysical region $R_{ADS} \lesssim 0$. The

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**Table I.** Fit results for $N_{DK^*}$, $R_{ADS}$, and the number of background events, for the three channels. The uncertainties are statistical only.

<table>
<thead>
<tr>
<th>channel</th>
<th>$K\pi$</th>
<th>$K\pi\pi^0$</th>
<th>$K\pi\pi\pi$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$N_{DK^*}$</td>
<td>$74 \pm 12$</td>
<td>$146 \pm 17$</td>
<td>$101 \pm 17$</td>
</tr>
<tr>
<td>$R_{ADS}$</td>
<td>$0.067^{+0.070}_{-0.054}$</td>
<td>$0.060^{+0.055}_{-0.037}$</td>
<td>$0.137^{+0.115}_{-0.055}$</td>
</tr>
<tr>
<td>$N_{SS}$</td>
<td>$75 \pm 16$</td>
<td>$265 \pm 33$</td>
<td>$345 \pm 35$</td>
</tr>
<tr>
<td>$N_{BG}$</td>
<td>$40 \pm 17$</td>
<td>$215 \pm 41$</td>
<td>$327 \pm 48$</td>
</tr>
<tr>
<td>$N_{Cont}$</td>
<td>$387 \pm 22$</td>
<td>$2497 \pm 56$</td>
<td>$2058 \pm 53$</td>
</tr>
<tr>
<td>$N_{OS}$</td>
<td>$1602 \pm 41$</td>
<td>$7793 \pm 96$</td>
<td>$6372 \pm 91$</td>
</tr>
</tbody>
</table>

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**Table II.** Systematic uncertainties $\Delta R_{ADS}$, in units of $10^{-2}$, for $R_{ADS}$, $R_{ADS}$, and $R_{ADS}$.

<table>
<thead>
<tr>
<th>Source</th>
<th>$K\pi$</th>
<th>$K\pi\pi^0$</th>
<th>$K\pi\pi\pi$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Sig. PDF</td>
<td>0.19</td>
<td>0.11</td>
<td>0.82</td>
</tr>
<tr>
<td>Cont. PDF</td>
<td>0.32</td>
<td>0.02</td>
<td>0.29</td>
</tr>
<tr>
<td>$BB$ PDF</td>
<td>0.57</td>
<td>0.16</td>
<td>1.48</td>
</tr>
<tr>
<td>Peaking background</td>
<td>1.70</td>
<td>0.87</td>
<td>1.40</td>
</tr>
<tr>
<td>$\epsilon_{CFS}$</td>
<td>---</td>
<td>0.17</td>
<td>0.39</td>
</tr>
<tr>
<td>Cross feed</td>
<td>0.04</td>
<td>0.05</td>
<td>0.02</td>
</tr>
<tr>
<td>TOTAL</td>
<td>1.8</td>
<td>0.91</td>
<td>2.2</td>
</tr>
</tbody>
</table>
The significance of observing a signal is evaluated in each channel using the ratio $\log(L_{\text{max}}/L_0)$, where $L_{\text{max}}$ and $L_0$ are the maximum likelihood values obtained from the nominal fit and from a fit in which the signal component is fixed to zero, respectively. We observe a ratio $R_{\text{ADS}}$ different from zero with a significance of 1.1, 1.7, and 1.4 standard deviations for the $K\pi$, $K\pi\pi^0$, and $K\pi\pi\pi$ modes, respectively. Since the measurements for the $R_{\text{ADS}}$ ratios are not statistically significant, we calculate 95\% probability limits by integrating the likelihoods, starting from $R_{\text{ADS}} = 0$. We obtain $R_{\text{ADS}}(K\pi) < 0.244$, $R_{\text{ADS}}(K\pi\pi^0) < 0.181$, and $R_{\text{ADS}}(K\pi\pi\pi) < 0.391$ at 95\% probability. The overall significance of observing an $R_{\text{ADS}}$ signal, evaluated from the combination of the three measurements, is 2.5 standard deviations.

Following a Bayesian approach, the measurements of the $R_{\text{ADS}}$ ratios are translated into a likelihood for $r_S$. A large number of simulated experiments for the parameters on which $R_{\text{ADS}}$ depends [see Eq. (5)] are performed. For each experiment, the values of $R_{\text{ADS}}(K\pi)$, $R_{\text{ADS}}(K\pi\pi^0)$, and $R_{\text{ADS}}(K\pi\pi\pi)$ are obtained and a weight $\mathcal{L}(R_{\text{ADS}}(K\pi))\mathcal{L}(R_{\text{ADS}}(K\pi\pi^0))\mathcal{L}(R_{\text{ADS}}(K\pi\pi\pi))$ is computed. In the extraction procedure to determine $r_S$, we use the experimental distributions for the $r_D$ ratios, $\delta_D(K\pi)$, $k_D(K\pi\pi^0)$, $\delta_D(K\pi\pi\pi)$, $k_D(K\pi\pi\pi)$, and $\delta_D(K\pi\pi\pi)$ [7,11,12]. All the remaining phases are extracted from a flat distribution in the range $[0, 2\pi]$. $r_S$ is extracted from a flat distribution in the range $[0, 1]$ and $k$ is extracted from a Gaussian distribution with mean 0.95 and standard deviation 0.03. We obtain the likelihood $\mathcal{L}(r_S)$ shown in Fig. 4. The most probable value is $r_S = 0.26$ and we obtain, by integrating the likelihood, the following 68\% and 95\% probability regions:

$$r_S \in [0.18, 0.34]@68\%\text{probability},$$
$$r_S \in [0.07, 0.41]@95\%\text{probability}.$$
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