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Large Dielectric Constants and Massive Carriers in La$_2$CuO$_4$

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We report measurements of the conductivity and dielectric constant as a function of frequency and temperature on samples of La$_2$CuO$_4$ from dc to 100 GHz. An analysis of the frequency dependence of the complex conductivity indicates that the high-frequency dielectric constant is large ($\approx$50) and weakly temperature dependent. The dc charge carriers are massive (1100$m_e$), weakly damped, and partially pinned.

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The discovery$^1$ of superconductivity in La$_{2-x}$Sr$_x$CuO$_4$ by Bednorz and Müller has led to extensive studies of these materials. They and others have proposed$^3$ that La$_{2-x}$Sr$_x$CuO$_4$ is similar to Pb$_{1-x}$Ba$_x$BiO, a perovskite with a superconducting transition temperature larger than expected from the carrier density, and that both are likely candidates for bipolaronic superconductivity. To test this we have made extensive measurements of the frequency-dependent conductivity and dielectric constant in single crystals of semiconducting La$_2$CuO$_4$. We find a high dielectric constant of 50–75 and extremely massive (m$^* \approx 1100$m$_e$) charge carriers. We show that these results are consistent with theories of bipolaronic transport.

All of the measurements reported here were performed on crystals of La$_2$CuO$_4$ grown from a CuO flux. The samples were annealed in N$_2$ at 650°C, slowly cooled, and then polished to eliminate all the flux and off-stoichiometric surface layers. In the a-b plane of one sample we made the 34-GHz measurements, applied four-probe contacts, measured the dc conductivity, polished off the contacts, and finally made the 60-GHz, 94-GHZ, and microwave bridge measurements. A second sample was used only for 10-kHz capacitance bridge measurements of the anisotropic dielectric constant.

The millimeter-wave conductivity measurements were performed with a bridge technique extensively discussed and tested in an earlier publication.$^3$ The bridges operate on an interferometer principle with precision attenuators and phase shifters used to null the output of an arm containing a sample against that of a reference arm. Here we only discuss the equivalent circuit for the termination admittance

$$Y = [Z_{\text{inf}} + Z_a]^{-1},$$

where $Z_{\text{inf}}$ is the impedance of an infinitely conducting object with dimensions and position identical to the sample and $Z_a$ is the part of the impedance that depends on the conductivity. Schwinger and Saxon$^4$ have calculated $Z_{\text{inf}}$ and $Z_a \propto 1/\sigma$ for a small sample aligned with the electric field of the TE$_{011}$ mode and extending between plates of a continuous section of waveguide. Here we use a section of waveguide with a hole for the sample a distance $3\delta/4$ from a terminating plate, where $\delta$ is the guided wavelength. Tests with quartz rods verified that the expression for $Z_\sigma$ is accurate with $\approx 20\%$ corrections. We find that $Z_{\text{inf}} = i\omega L$, where $L = (l/\mu_0/2\pi)\ln(r'/r) = 0.6$ nH with $l$ the sample length and $r'$ the radius of the hole. The effective radius $r = (A/\pi)^{1/2}$ = 0.1 mm is determined from the sample cross section $A$.

The measurements in the microwave regime were performed with a bridge operating in the range 3–15 GHz. The bridge operates on the same principle as the millimeter-wave bridges, except that it is implemented with coaxial transmission lines. The sample is placed between the center conductor, which is terminated as a flat surface perpendicular to the axis of the coaxial line, and the outer conductor, which extends on as a circular waveguide beyond cutoff. The admittance of this termination is

$$Y = \frac{i\omega C_c + \frac{1}{i\omega L - i/\omega C_c + Z_\sigma}}{1 - \frac{1}{i\omega L - i/\omega C_c + Z_\sigma}},$$

where $C_c$ is the capacitance from the end of the inner conductor to the outer conductor, $L$ is the inductance of the sample, $C_c$ is the contact capacitance, and $Z_\sigma = l/A\sigma$ is the sample impedance. We tested the validity of this description with separate experiments for each term. For the first term in Eq. (2) we machined a Teflon cylinder which precisely fit the interior dimension of the outer conductor and touched the end of the inner conductor. The frequency dependence of the phase shift was such that a capacitance $C_c = 25$ fF was an appropriate description. We estimated the inductance to be $(l'/\mu_0/2\pi)\ln(a'/A^{1/2})$, where $l'$ is the distance between outer and inner conductors and $a$ is a constant of order unity. We evaluated $a$ by measuring the frequency-dependent phase shift of a Pt wire silver painted on the surface of the coaxial line and estimated that $a = 1.33$ and that the termination was a nearly pure inductance, with a small end-capacitance correction and no apparent...
contact impedance. We used the same inductance formula to calculate an inductance of 0.75 nH for the La$_2$CuO$_4$ sample.

Further tests of the microwave bridge were made by studying the less pure La$_2$CuO$_4$ crystals grown from a PbO flux (by J. P. Remeika). The real part of their frequency-dependent conductivity displays a peak. These samples, however, had an impedance less than 50 Ω, the characteristic impedance of the coaxial line, and the conductivity resonance appeared in the loss measurements as a minimum. The samples prepared from a CuO flux, however, have an impedance greater than 50 Ω and the conductivity resonance appears as a maximum in the measured loss. This confirms that no systematic error in loss measurements could produce the resonance reported here.

The temperature-dependent conductivity measurements at dc, 34, 60, and 94 GHz are displayed in Fig. 1. The largest conductivities are at 34 GHz with lower conductivities at other frequencies. Thus a maximum exists between dc and 60 GHz.

The dielectric constants at 34, 60, and 94 GHz are shown in Fig. 2. At low temperatures the dielectric constants at the three frequencies are nearly equal and all the results extrapolate to a dielectric constant of 50 at zero temperature. At temperatures above 50 K the dielectric constants decrease and then plateau at lower or negative values. We also measured the dielectric constant at 0 kHz and 4.2 K and found $\epsilon = 45 \pm 5$ in the $a$-$b$ plane (displayed in Fig. 2) and $\epsilon = 23 \pm 3$ along the $c$ axis.

The conductivity and dielectric constants are plotted with the microwave bridge results in Fig. 3 at $T =$ 293 and 50 K. The real part of the dielectric constant is presented as the imaginary part of the complex conductivity. The curves in Fig. 3 are fits with a harmonic-oscillator model

$$\sigma(\omega) = \frac{ne^2 \tau}{m^*} \frac{i \omega}{i \omega + \tau(\omega^2 - \omega_0^2)} + \frac{i \omega \epsilon_{\infty}}{4\pi},$$

where the solid curve is Re$(\sigma)$, the dashed curve is Im$(\sigma)$, and the fit parameters are displayed in Table I. The high-frequency dielectric constant $\epsilon_{\infty}$ contains contributions from phonons, bound impurity states, and all other higher-frequency polarizabilities. For a typical semiconductor the first term in Eq. (3) is constant below 100 GHz and given by $ne^2 \tau/m^*$, where $n$ is the carrier density, $m^*$ is the effective mass, and $\tau$ is the carrier lifetime. Here, however, the peak in Re$(\sigma)$ and the negative values of Im$(\sigma)$ imply a long lifetime $\tau$ and a pinning frequency $\omega_0$ for the carriers. Equation (3) is then the simplest model which can qualitatively fit our data. Models which include a dc conductivity and have several additional parameters provide better fits than seen in Fig. 3, particularly at low frequencies, but do not provide additional insight.

Figure 2 displays the values of $\epsilon_{\infty}$ deduced from the fits by Eq. (3). If we assign all the spectral weight of $10^{22}$ electrons/cm$^2$ to the $\hbar \omega_0 = 1.7$ eV gap$^5$ then the contribution to the dielectric constant at low frequencies is $\epsilon = 4ne^2/l(m_e\omega_0)^2 \approx 5$. Optical reflectance measurements$^7$ indicate a dielectric constant of 6 at frequencies between the gap and optical-phonon modes, in excellent
agreement with this estimate. Other studies\(^6\) of reflectance at 40 cm\(^{-1}\) (below many of the phonon lines) imply \(\varepsilon_{\infty} = 51\) in the \(a-b\) plane and \(\varepsilon = 23\) perpendicular to the \(a-b\) plane, in excellent agreement with our results. Samples of La\(_2\)CuO\(_4\) prepared with our techniques typically have a carrier density \(n \approx 10^{19}\) cm\(^{-3}\) at room temperature and a dc conductivity activation energy \(\hbar \omega_0/k_B \approx 100\) K. If these carriers are bound to impurity sites at low temperature then their contribution to \(\varepsilon_{\infty}\) could be significant. This would decrease at \(T > 100\) K when the carriers are thermally ionized, an effect we do not observe. The most likely source of the dielectric constant is the low-lying phonon modes,\(^3,6\) suggesting that the material is near a ferroelectric instability. This large dielectric constant will screen electron-electron interactions, an important effect in the superconducting material.

The parameters associated with the low-frequency charge transport are \(\omega_0\), \(1/\tau\), and \(n e^2 \tau/m^*\). This transport disappears at low temperature, along with the dc conductivity. The microwave resonance must then be associated with the presence of the dc carriers and the resonant behavior indicates that the carriers are partially pinned and weakly damped. Using a mobility \(\eta/r/m^* = 3\) cm\(^2\)/V sec, the order of magnitude deduced\(^7\) for La\(_2\)Sr\(_2\)CuO\(_4\), and the fit parameter \(1/\tau\), we calculate an effective mass \(m^* = 1100 m_e\) at \(T = 293\) K. Given the uncertainties in this analysis these results are in complete agreement with our earlier result\(^8\) of \(m^* = 500 m_e\) in Eu\(_2\)CuO\(_4\). The effective mass is not dependent on the model; we obtain the same value from the carrier density, \(n = 10^{19}\) cm\(^{-3}\), and the integral of measured \(\text{Re}(\sigma)\).

There are several possible mechanisms which could enhance the dynamical mass of the carriers in La\(_2\)CuO\(_4\). Those most commonly discussed in the literature are (i) magnetic interactions and (ii) phonon interactions.

(i) Large enhancements of the effective mass have been obtained\(^9\) for holes in a Mott-Hubbard model. The results depend strongly on whether one considers one hole or two holes but the mass enhancements are typically \(\approx 10\) for \(U/t \approx 10\). Two-band Mott-Hubbard calculations have also been performed\(^10\) for relevant values of the parameters and lead to mass enhancements of approximately 10.

(ii) Phonon interactions are commonly found to enhance the mass of electronic carriers. These enhancements are usually modest, except when the atoms undergo a static distortion in the response to a conduction charge. A displacement of the conduction charge then causes atomic motions which store large amounts of kinetic energy and create large mass enhancements. A typical example is the charge-density wave where mass enhancements\(^11\) \(\approx 10^2\) occur with atomic displacements \(\approx 0.1\) Å. Similar atomic displacements are observed\(^12,13\) in Tl\(_2\)Ba\(_2\)CaCuO\(_4\) and La\(_2\)CuO\(_4\). For a polaron with a drift velocity \(v_d\) we calculate the kinetic energy \(E\) stored in the atomic motions and define an effective mass from \(E = m^* v_d^2/2\). For a drifting 2D bipolaron with maximum distortion amplitude \(\delta r\) at a distance \(R\) from the bipolaron center the distortion must relax in a time \(R/v_d\). The atomic velocity is then \(v_d \delta r/R\) and the number of atoms moving is roughly \(\pi R^2/a^2\), where \(a\) is

<table>
<thead>
<tr>
<th>(T) (K)</th>
<th>(\omega_0/2\pi) (GHz)</th>
<th>(1/2\pi\tau) (GHz)</th>
<th>(n e^2 \tau/m^*) (mho/cm)</th>
<th>(\varepsilon_{\infty})</th>
</tr>
</thead>
<tbody>
<tr>
<td>293</td>
<td>4.9</td>
<td>41</td>
<td>9.1</td>
<td>75</td>
</tr>
<tr>
<td>156</td>
<td>7.0</td>
<td>56</td>
<td>5.4</td>
<td>66</td>
</tr>
<tr>
<td>50</td>
<td>52</td>
<td>71</td>
<td>0.59</td>
<td>52</td>
</tr>
</tbody>
</table>
the atomic spacing. The kinetic energy sum then leads to $m^* = \pi a \delta r^2$, where $a$ is the 2D mass density. If we assume that the displacements at the O(2) sites\textsuperscript{13} of La$_2$CuO$_4$ are caused by and follow the dopant holes, then $a = 2 \times 16 \times 1800 m_r / (15 \text{ Å}^2) = 3840 m_r / \text{Å}^2$ [for O(2) only] and $\delta r = 2.4 - 2.16 \text{ Å} = 0.24 \text{ Å}$. This implies $m^* = 695 m_r$, in excellent agreement with our results.

From our measurements alone we are unable to distinguish whether the carriers are polarons or bipolarons. Recent theoretical studies,\textsuperscript{14} however, indicate that polarons are stable with respect to polarons if the intrinsic $\epsilon_\infty$ is large. The dielectric constant here, $\epsilon_\infty$, is well within the stability criteria, implying that all the measurements reported here are consistent with a bipolaron interpretation.

In conclusion, we have studied the dielectric response of La$_2$CuO$_4$, and have found that the material is not describable as a normal semiconductor. The frequency-independent portion of the dielectric constant $\epsilon_\infty$ is much larger than electronic transitions could account for, suggesting that low-energy optically active phonons are dominating the dielectric behavior of this perovskitelike structure. The surprising aspect of these measurements is the large dynamical mass, $\approx 1100 m_r$, obtained from the analysis of the frequency-dependent conductivity. This is consistent with our earlier measurements\textsuperscript{8} on Eu$_2$CuO$_4$, indicating that the carriers in these planar compounds are massive and self-localized. The CuO compounds which superconduct contain high densities of holes and apparently have smaller masses,\textsuperscript{15} indicating that the mass may decrease with decreasing separation. All of these results are consistent with a bipolaronic interpretation but further investigations are required to confirm such a model.

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10. S. A. Trugman (private communication).
14. Emin, Ref. 2.