Title
A HIGH CURRENT HEAVY ION BEAM TRANSPORT EXPERIMENT AT LBL

Permalink
https://escholarship.org/uc/item/6z66n8zv

Author
Chupp, W.

Publication Date
1984
A HIGH CURRENT HEAVY ION BEAM TRANSPORT EXPERIMENT AT LBL


January 1984
DISCLAIMER

This document was prepared as an account of work sponsored by the United States Government. While this document is believed to contain correct information, neither the United States Government nor any agency thereof, nor the Regents of the University of California, nor any of their employees, makes any warranty, express or implied, or assumes any legal responsibility for the accuracy, completeness, or usefulness of any information, apparatus, product, or process disclosed, or represents that its use would not infringe privately owned rights. Reference herein to any specific commercial product, process, or service by its trade name, trademark, manufacturer, or otherwise, does not necessarily constitute or imply its endorsement, recommendation, or favoring by the United States Government or any agency thereof, or the Regents of the University of California. The views and opinions of authors expressed herein do not necessarily state or reflect those of the United States Government or any agency thereof or the Regents of the University of California.
A HIGH CURRENT HEAVY ION BEAM TRANSPORT EXPERIMENT AT LBL*


Lawrence Berkeley Laboratory
University of California
Berkeley, California 94720

January 1984

* This work was supported by the Office of Energy Research, Office of Basic Energy Sciences, Department of Energy under Contract No. DE-AC03-76SF00098.
A HIGH CURRENT HEAVY ION BEAM TRANSPORT EXPERIMENT AT LBL*

W. Chupp, A. Faltens, E. C. Hartwig, D. Keefe, C. H. Kim, C. Pike,
S. S. Rosenblum, M. Tiefenback, D. Vanecek, and A.I. Warwick

Lawrence Berkeley Laboratory
University of California
Berkeley, California

Introduction

Information on the current limit in a long quadrupole transport channel is required in designing an accelerator driver for an inertial confinement fusion system.\(^1\) Although a current transport limit was proposed by Maschke,\(^2\) quantitative estimates require a detailed knowledge of the stability of the beam. Analytic calculations based on the Kapchinskij-Vladimirskij (K-V) distribution function have identified transversely unstable modes, but particle simulations\(^3\) have shown that some of the K-V instabilities are benign, i.e., particles redistribute themselves in the 4-D transverse phase space, but the rms emittances do not grow. Some preliminary results of beam transport experiments were reported in the 1983 Particle Accelerator Conference in Santa Fe.\(^4,5,6,7\)

In the "smooth approximation", particles in a quadrupole focusing channel execute simple harmonic motions whose frequency (\(\omega_B\)) is given by

\[
\omega_B^2 = \omega_B^2 - \frac{1}{2} \omega_p^2
\]

where symbols from left denote the betatron frequencies with and without the space charge and the beam plasma frequency, \((4\pi ne^2/M)^{1/2}\). Eq. (1) can be rewritten in terms of the beam current density \(j\) and the phase advances of the betatron oscillation per lattice period \((2L)\) with and without the space charge \(\sigma_0\) and \(\sigma_0^*\) respectively;

\[
j = 3.75 \times 10^{-11} A^{-1/2} L^{-2} (\sigma_0^2 - \sigma_0^*^2) T^{3/2}
\]

* This work was supported by the Office of Energy Research, Office of Basic Energy Sciences, Department of Energy under Contract No. DE-AC03-76SF00098.
where $A$ is the atomic mass number, $T$ the kinetic energy in eV, $\sigma$'s in degrees and $j$ and $L$ are in mks units. Eq. (2) agrees very well with the K-V calculation for $\sigma_0 = 60^\circ$ (see fig. 4). The K-V envelope equation shows that the beam cross-section scales as $\epsilon/\sigma$ for $\sigma/\sigma_0 \ll 1$ where $\epsilon$ is the un-normalized beam emittance. The benefits of operating the transport channel at small $\sigma$ values are obvious. Maschke's original assumption was $(\sigma/\sigma_0)^2 > 0.5$, and the value used in the earlier driver designs based on the K-V stability calculation was $\sigma/\sigma_0 \geq 0.4$.

Experimentally, we define stable propagation of the beam if the beam current, size, and emittance measured at the end of the transport channel (41 lattice periods) are the same as the values measured at the beginning. We find that:

1. Stable beam transport is observed for $\sigma_0 = 60^\circ$ and $\sigma > 12^\circ$

2. Strong instabilities are observed for $\sigma_0 = 120^\circ$ and $\sigma \leq 90^\circ$

3. The semi-gaussian nature of the particle distribution (i.e., uniform in configuration space, gaussian in transverse velocity space) is approximately preserved for $\sigma_0 = 60^\circ$ and $\sigma/\sigma_0 = 0.2$.

Apparatus

The apparatus (Fig. 1) consists of the ion source, injector (gun), matching section (5 quadrupoles M1-M5), transport section (82 electrostatic quadrupoles Q1-Q82), and the diagnostic tank. The fact that a beam is stable in a channel of 82 quadrupoles does not insure that the beam will be stable in a longer channel such as in the ICF driver which may have a few hundred periods and includes acceleration. However, we believe that the present experiment can provide necessary conditions for the beam stability and can serve as an incentive to develop more accurate computational techniques. A more complete description of the apparatus can be found in our earlier publication. Because of the high voltages on the electrostatic quadrupoles, the placement of diagnostics is restricted to the mid-plane between any pair of quadrupoles. At such a location - the antisymmetrical
point of the lattice— the phase ellipses in the \( xx' \) and \( yy' \) planes for a matched beam are similar in shape but tilted with equal and opposite angles (astigmatic). The ranges of the \( Cs^+ \) beam parameters and the ways they are varied are listed below.

- Kinetic energy (T): 80 - 160 keV (Marx Generator)
- Beam Current (I): 0.7 - 23 mA (Current Attenuators)
- Beam Emittance (\( \epsilon_N \)): 0.8 - 5 \( \times \) \( 10^{-7} \) rad m (Biased Grids)

The current is measured with a gridless deep Faraday cup (with an uncertainty of \( \pm 2\% \)) at the end of the transport section and with a shallow gridded Faraday cup (0 to \(-10\%\)) in between quadrupoles at the end of the matching section. The kinetic energy is measured by the time of flight method (\( \pm 2\% \)). The beam emittance is measured by a two slit scan method (\( \pm 10\% \)), using two 0.25 mm slits separated by one lattice half-period (15.24 mm) followed by a shallow Faraday cup. The beam current profile is measured with a single slit and a shallow Faraday Cup, or with a "harp" which consists of a 32 isolated parallel wires spaced 1.25 mm apart. The beam radii \((a \text{ and } b \text{ for horizontal and vertical, respectively})\) are deduced from the measured profiles by the rms analysis, and the tilts \((a' \text{ and } b')\) from the emittance plots. For a perfectly matched beam, \(a = b\), and \(a' = -b'\) at the antisymmetry points.

The particle distribution function at the end of the injector is semi-Gaussian. The semi-Gaussian distribution gives an elliptical current profile just as a K-V distribution would. The measured beam emittance is approximately five times higher than expected from the thermal temperature of the zeolite ion source (0.1 eV). We believe that the non-uniformity of the ion emission from the source and the presence of the grid(s) between the injector and the matching section are responsible for the observed higher temperature.

Experimental Procedure

Beam matching and data analysis are guided by the rms envelope equation derived by Sacherer.\(^8\) The rms emittance is defined as

\[
\epsilon_{\text{rms}} = (\beta y) \sqrt{\langle x^2 \rangle \langle y^2 \rangle - \langle xx' \rangle^2}
\]
SINGLE BEAM TRANSPORT EXPERIMENT

Fig. 1. Schematic diagram of the apparatus showing (from right to left) the ion source, gun (injector), matching section (5 quadrupoles M1-M5), transport section (82 quadrupoles Q1-Q82) and the diagnostic section. Ranges of beam parameters are listed in the text. Lattice-half period = 15.24 cm, bore diameter = 5.08 cm.
where $\beta_\gamma$ are the usual relativistic parameters and the brackets denote averaging over the distribution function. Values of $\sigma_0$ and $\sigma$ are calculated from the equivalent K-V beam which has the same current, has $\epsilon_N = 4\epsilon_{\text{rms}}$, and has a beam radius $a = 2x_{\text{rms}}$. For the desired values of $\sigma_0$ and $\sigma$, we adjust the injector and lattice parameters ($I$, $T$, $\epsilon_N$, and $V_Q$) accordingly. These four parameters are fed into a computer program (EQENV) which integrates the envelope equations and searches for a matched beam (periodic) envelope in the transport section. The injected beam (axisymmetric) has to be transformed into the matched beam (astigmatic) as it passes through the matching section. Another computer code (PARAX) is used to search for the correct voltage settings of four of the five matching quadrupoles. The remaining quadrupole (usually the first or the last one) is set at a fixed voltage.

At the first trial of matching, the mismatch is usually large ($\pm 10\%$ variation of the radius as a function of $z$), but the median radius around which the envelope oscillates is observed to have the same value as the matched radius predicted by the rms envelope equation, within the experimental errors of measuring $V_Q$, $I$, $T$, $a$, and $b$. The envelope is insensitive to $\epsilon_N$ in the space charge dominated region. The envelope oscillation is measured by monitoring the horizontal and vertical beam profiles in between quadrupoles at various locations in the transport section. Satisfactory matching requires a number of iterations. It is possible to make small corrections by using the calculated $4 \times 4$ linear response matrix which relates changes of the four matching quadrupole voltages to changes in the envelope parameters ($a$, $a'$, $b$, $b'$) at the end of the matching section.

**Experimental Results**

We investigated to what accuracy we can control the beam radius. For each of the matched beams, we measured the beam radii (squared) at various locations along the focusing channel and compared them with the theoretically calculated value for the equivalent K-V beam. The results are summarized in Fig. 2 for $\sigma_0 = 60^\circ$. The errors indicated by the circles correspond to the amplitude of the envelope oscillation and the measurement errors of $\epsilon_N$. The measurement errors of the beam radii are much smaller than the amplitude of the envelope oscillation. The phase shifts ($\sigma$) are also calculated values for the equivalent K-V beams and range from $12^\circ$ to
55° as indicated in Fig. 2. We are in the process of modifying the injector to achieve even greater tune depression (down to approximately 6°). Values of $\sigma_0$ have been varied from 45° to 120°.

The effect of nonlinearities is studied by monitoring the distortions of the particle distribution (usually the figure-8 shape). The effects are undetectable for the largest beam radius we have studied so far. The largest matched beam radius was 15.5 mm between the quadrupoles and 19 mm (inferred) in the middle of the focusing lens. This corresponds to more than 80% of the bore radius (25.4 mm) when the mismatch oscillations (±5% of the radius) and the equilibrium orbit errors (±2 mm) are taken into account.

![Graph](Image)

**Fig. 2.** Experimental matched beam radii (squared) for various emittances and currents in a $\sigma_0 = 60°$ lattice. The values of $\sigma$ are calculated and the currents used experimentally are fitted for the equivalent K-V beam which has the same total current, but has $\epsilon_N = 4 \epsilon_{\text{rms}}$ and has a radius = $2 \chi_{\text{rms}}$. Approximate errors for $\epsilon_N$ and the amplitudes of the mismatch oscillation are indicated with an ellipse for each data points.
The particle distribution function at the injector is semi-Gaussian with an elliptical current profile projected in either the x or y directions as mentioned earlier. The distribution functions measured at the end of the transport section appear to be different qualitatively depending on the degree of tune depression as well as on the stability of the beam. These differences are illustrated in Fig. 3a, b, c for $\sigma/\sigma_0 = 12^\circ/60^\circ$ (stable), $50^\circ/60^\circ$ (stable), and $36^\circ/120^\circ$ (unstable). For $12^\circ/60^\circ$, the semi-Gaussian nature of the distribution is approximately preserved with the exception that there is a slight flattening tendency of the otherwise elliptical current profile (Fig. 3a). The flattening may mean hollowing of the current density distribution ($j$ vs. $x$ and $y$) on the beam axis by approximately 10%. For $50^\circ/60^\circ$, the observed distribution appears to be a full-Gaussian (Fig. 3b), i.e., Gaussian in both configuration and velocity space. A typical distribution after it has gone through an instability is shown in Fig. 3c. Dangerous instabilities such as this cause an irregular beam profile, a halo around the beam, and a significant current loss. The remaining beam has a much larger emittance than the injected beam.

The semi-Gaussian distribution is a self-consistent one for a focusing channel which has a cylindrical square-well potential, in the sense that the form of the distribution function does not change along the channel. In the present experiment, a focusing field somewhat similar to the square-well shape is formed for $(\sigma/\sigma_0)^2 \ll 1$ because the average focusing field inside the beam is reduced by the space charge of the beam by a factor $(\sigma/\sigma_0)^2$ while the reduction outside of the beam decreases as $1/x$. For each of the matched beams, we measured the emittance, size, and current at the beginning and at the end of the transport section: the beam is inferred to be stable if these values do not change within the experimental error. The results are summarized in Fig. 4 as the stable and unstable regions in the $j$ vs. $(\sigma/\sigma_0)$ parameter space. The dependence of $j$ on $\sigma/\sigma_0$ is calculated for the K-V distribution for the actual experimental geometry. For $\sigma_0 = 60^\circ$, the dependence agrees very well with the prediction of the smooth approximation.
Fig. 3. The particle distribution in the phase space \((x' - \alpha x, x)\) and the current profile \((\int \text{j}dy \text{ vs. } x)\) are shown for the three representative cases. The coordinate transformation \(x' = x' - \alpha x\) suppressed the tilt of the contours for the distribution in the middle of two adjacent quadrupoles. The contours plotted here correspond to 10, 30, 50, 70, and 90% of the peak of the distribution, respectively. (a) A high space charge stable beam case with \(\sigma_0 = 60^\circ\) and \(\sigma = 12^\circ\), measured at Q80. An elliptical profile is shown for comparison with a semi-Gaussian distribution. (b) A low space charge stable beam case with \(\sigma_0 = 60^\circ\) and \(\sigma = 50^\circ\), measured at Q80. A Gaussian profile is shown for a comparison with a full-Gaussian distribution. (c) An unstable beam case with an injected current corresponding to \(\sigma_0 = 120^\circ\) and \(\sigma = 36^\circ\), measured at Q44, where the current was only 60% of the injected value.
Fig. 4. Experimentally measured stable and unstable regions. Analytically predicted unstable modes for D-V distribution are shown for comparison.

The stability of the beam for $\sigma/\sigma_0 = 12^\circ/60^\circ$ implies that the earlier driver designs, which assumed $\sigma/\sigma_0 = 24^\circ/60^\circ$, are rather conservative. Since $\sigma \propto \epsilon_N / I$, for the same value of $\epsilon_N$ and $I$, twice the current can be transported, or for the same value of the beam size a beam with half the emittance can be transported. Computer simulations show that $\sigma/\sigma_0$ can be even smaller\textsuperscript{10}. We are now in the process of modifying the injector for $6^\circ/60^\circ$ operation. In contrast to the case of $\sigma_0 = 60^\circ$, strong envelope instabilities are observed for $\sigma_0 = 120^\circ$, with an emittance growth by a factor $\sim 2$ and current losses when $\sigma < 90^\circ$.

Since we did not institute any longitudinal focusing, the head and the tail of the beam are observed to spread out longitudinally, but the main body of the beam is not affected. This result agrees quantitatively with the 1-D computer simulation.\textsuperscript{11}
Acknowledgments

We gratefully acknowledge helpful discussions and suggestions by Drs. J. Bisognano, I. Haber, L. J. Laslett, L. Smith, and technical assistance of B. Balke, C. Chavis, E. Edwards, W. Ghiorsko, R. Hipple, and J. Stoker.

References

1. D. Keefe, in these proceedings, Session 4.


10. I. Haber, private communication, also in these proceedings, session 5.

This report was done with support from the Department of Energy. Any conclusions or opinions expressed in this report represent solely those of the author(s) and not necessarily those of The Regents of the University of California, the Lawrence Berkeley Laboratory or the Department of Energy.

Reference to a company or product name does not imply approval or recommendation of the product by the University of California or the U.S. Department of Energy to the exclusion of others that may be suitable.