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Mesoscale electric fluctuations interacting with zonal flows, magnetic fluctuations, and turbulence

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Abstract: New mesoscale electric fluctuations (MSEFs) are identified in the edge plasmas of the HL-2A tokamak using multiple Langmuir probe arrays. The MSEFs, resulting from the synchronization and having components of dominant GAM and m/n=6/2 potential fluctuations, are found at the same frequency as that of the magnetic fluctuations of m/n=6/2 (m and n are poloidal and toroidal mode numbers, respectively). The temporal evolutions of the MSEFs and the magnetic fluctuations clearly show the frequency entrainment and the phase lock between the GAM and the m/n=6/2 magnetic fluctuations. The results indicate that GAMs and magnetic fluctuations can transfer energy through nonlinear synchronization. The nonlinear coupling analyses show that the MSEFs couple to turbulence and low frequency zonal flows (LFZF s). This suggests that the MSEFs may contribute to the LFZF formation, reduction of turbulence level, and thus confinement regime transitions. The analysis
of the envelope modulation demonstrates that both the MSEFs and the LFZFs modulate the turbulence while the MSEFs are modulated by the LFZFs.

1. Introduction

Interaction of magnetic field structures and flows in magnetohydrodynamics is a subject of general interest in physics. Typical examples include magnetic braking of stellar rotation [1], angular momentum transport in astrophysical disks [2, 3], and dynamics of the Earth’s core and geodynamo [4]. In fusion plasmas, the interactions between plasma flows and magnetic fluctuations have attracted attention, for understanding and control of plasma confinement and transport. For example, the neoclassical tearing modes, which need a seed magnetic island for onset [5, 6], can be, theoretically, triggered by a turbulence noise source [7]. At the same time, the magnetic island-induced sheared flows can suppress turbulence and contribute to the formation of an internal transport barrier [8]. The coupling of toroidal Alfven eigenmodes (TAEs) and Beta-induced Alfven eigenmodes (BAEs) to the zonal flows is predicted to reduce the saturation level of TAEs and BAEs so as to reduce fast ion loss [9]. For the mitigation or suppression of the large edge localized modes in the high confinement mode (H-mode) plasmas, which is considered to be an urgent task for fusion research, the resonant magnetic perturbations (RMPs) [10] are used worldwide. In applying RMPs, the interactions of magnetic perturbations, zonal flows [11], and microscopic turbulence take place.

Two types of zonal flows, (i.e., the low frequency zonal flows (LFZFs) [11, 12] and the geodesic acoustic modes (GAMs)[13, 14]), are known. The effects of magnetic perturbation on zonal flows were reported. For instance, the GAM is damped in the presence of RMPs [15]; the RMP-induced magnetic islands can enhance the LFZFs and turbulence, and accelerate the edge toroidal rotation [16,17]; the poloidal flows are reversed when the RMP-induced island width is large enough [18]; a quasi-coherent mode is detected near the low safety factor rational surface [19, 20]. However, the dynamical and mutual interaction between flows and magnetic perturbations has not been deeply studied experimentally.
To understand the complicated interaction of the flows with the magnetic structures, we have to know the ways of their interaction dynamically. Here, the observation of the synchronization, a universal nonlinear phenomenon in nature [21–24], of GAMs and magnetic fluctuations in the edge plasmas of the HL-2A tokamak is reported [25]. The frequency entrainment and phase lock, two essential elements in synchronization, are demonstrated. Because the magnetic field and velocity field are the two essential vector fields in plasmas, governing the turbulent structure formation in the Universe and laboratory, the discovery of synchronization reveals a new, essential and prototypical process in nonlinear dynamics of high temperature plasmas. The mesoscale electric field fluctuations (MSEFs), resulting from the synchronization, can interact with the LFZFs and turbulence through nonlinear three wave coupling. The mesoscale refers to the finite radial wavelength \( \sim L \) in the regime of \( r_c < L < a \). Here, \( r_c \) and \( a \) are the correlation length of turbulence and macro-scale of the system. On the HL-2A tokamak, the \( r_c \) and \( a \) are \( \sim 0.5 \) cm and \( \sim 40 \) cm, respectively.

The rest of this work is organized as follows. The experimental set-up is given in section 2. The experimental results, described in section 3, include the observation of the MSEFs, the mode structures of the MSEFs, the frequency entrainment and the phase lock between the GAMs and magnetic fluctuations, and the nonlinear interaction among magnetic fluctuations, MSEFs, LFZFs, and turbulence etc. Section 4 presents the discussion and conclusion.

2. Experiment setup

The experiments presented here were conducted in Ohmic and electron-cyclotron-resonance-heating (ECRH)
deuterium plasmas of a circular cross section on the HL-2A tokamak. The major and minor radii of the HL-2A tokamak are \( R = 1.65 \) m and \( a = 0.4 \) m, respectively. The ECRH power is \(~500\) kW. The parameters specially set for the experiments are the toroidal magnetic field \( B = 1.2\text{-}1.3 \) T, the plasma current \( I_p = 150\text{-}180 \) kA, the line averaged electron density \( N_e = 1\text{-}2\times10^{19}m^{-3} \), the safety factor \( q_a = 3.3 \). The sampling rate of the probe data is 1 MHz corresponding to Nyquist frequency of 500 kHz. The frequency resolution is 0.25 kHz in the following analysis unless otherwise stated. A combination of distributed Langmuir probe (LP) arrays was used to measure floating potential fluctuations, and density and temperature profiles, as shown in the figure 1.

In the combination, a LP array of three tips and a four-tip LP array form a fast reciprocating probe set of seven tips with a 65 mm poloidal span. A radial rake probe array of 12 tips, in the toroidal direction, is located in the poloidal cross section 2100mm away from the set of seven tips. It was used to get radial profiles of floating potential fluctuations. The tip size and the mount of the LP sets are the same as was described in Ref. [26].

3. Experiment results

3.1 Observations of MSEF\text{s}

The new mesoscale electric fluctuations with components of the dominant GAMs and the \( n/n=6/2 \) potential fluctuations are detected inside the last closed flux surface (LCFS) in ECRH plasmas. The tip is located at the radial position of \( \Delta r = -4.6\text{cm} \), where the minus sign means inwards from the LCFS. Figures 2(a) and (b) give the auto power spectra of the floating potential fluctuations and the magnetic fluctuations from the Mirnov coils set up on the vacuum vessel wall, respectively. The small peak shown in
the figure 2(a) at the frequency of ~10.5 kHz is the MSEF. A large power fraction peak of the LFZF in the frequency range of ~0.25-3 kHz was also detected. The large peak at the frequency of ~ 6 kHz shown in figure 2 (b) is the tearing modes with mode numbers of m/n=2/1. The small peak presented in figure 2(b) at the same frequency as the MSEFs has components of the dominant m/n=6/2 magnetic fluctuations and the n=0 zonal field. Besides, the two small peaks at the frequency of 1.2 kHz and 12 kHz come from the power supply and the m/n=4/2 tearing mode, respectively.

3.2 Mode structures of the MSEFs

Figures 3 (a)-(d) show the toroidal coherency between potential fluctuations, their phase shifts, the coherency between floating potential and magnetic fluctuations, and the radial phase shifts between potential fluctuations, respectively. The toroidal coherency in the LFZF and MSEF frequency bands is all quite high. This indicates that the MSEF and LFZF have strong correlation in the toroidal direction with a span of 2100 mm. The corresponding phase shift in the MSEF frequency region is estimated as $\Delta \phi_t = 0.25 \pm 0.09 \text{ rad}$. The toroidal mode number is calculated as $n = 0 \pm 0.2$. The evaluated radial phase shift is $\Delta \phi_r = 1.4 \pm 0.2 \text{ rad}$ with a spans of 4 mm in radial direction, and the corresponding radial wave vector is estimated as $k_r = 3.5 \pm 0.2 \text{ cm}^{-1}$.

Thus, we conclude that the MSEF has the characteristics of the toroidal symmetry, and finite radial wave numbers, and thus the GAM component is dominant. In addition, the calculated coherency between the MSEFs and the magnetic fluctuations at the MSEF frequency is significantly above
the noise level, indicating that the MSEFs are well correlated with the magnetic fluctuations.

Fig. 4 (color online) The contour plots of coherency between potential and magnetic fluctuations (a), and between turbulence envelope and magnetic fluctuations in the frequency band of 9-11kHz (b).

The spatial structures of the MSEF at the frequency of ~10.5 kHz were identified further with correlation analysis. Figure 4 (a) shows the contour of $C(X(\Delta r), Y(\xi))$, where $X(\Delta r)$ is the potential perturbation at $r = a + \Delta r$ and $Y(\xi)$ is the magnetic fluctuation measured with the Mirnov coil at the toroidal angle $\xi$. Here, the coherency is described as $C_{xy} = \langle(X_i - X)(Y_i - Y)\rangle/[\sqrt{\langle(X_i - X)^2\rangle}\sqrt{\langle(Y_i - Y)^2\rangle}]$, where $X_i$ and $Y_i$ are two sets of variables, $i$ stands for time series, and $\langle ... \rangle$ denotes an ensemble average, though in this work this was estimated from the data using a time average, i.e. by applying the ergodic hypothesis. $X$ and $Y$ are the averages of $X_i$ and $Y_i$, respectively. The 12 probe tips are uniformly distributed in the radial direction from -4.8 to -0.4 cm inside the LCFS. The 10 Mirnov coils are located at different
toroidal angles. The toroidal mode number of n=2 is clearly demonstrated for the potential fluctuation at the frequency of ~10.5 kHz. The poloidal mode number of m=6 is also estimated with similar analysis. Figure 4 (b) also gives the contour plot of the coherency between turbulence envelopes [27] and magnetic fluctuations. The poloidal and toroidal mode numbers for the turbulence envelope are identified as m=6 and n=2, respectively. This analysis indicates that the MSEF also contains m/n=6/2 potential fluctuations. The phase shift between the turbulence envelope and the m/n=6/2 potential fluctuation is close to \( \pi /2 \). The radial wavelengths of the m/n = 6/2 potential fluctuation and turbulence envelope are all estimated as about ~2 cm. The m/n = 6/2 potential fluctuation propagates in the directions of toroidal magnetic field and ion diamagnetic drift.

The radial distributions of the potential fluctuation power at the MSEF frequency are measured and shown in figure 5 (a). The power as a function of the radial position shows two peaks. The amplitude of the MSEF first increases from the LCFS inwards, but reduces at the position of \( \Delta r\sim2.0 \) cm, where the surface of the safety factor q=3 is located. Then the power increases again and reaches a maximum at \( \Delta r\sim -3.0 \) cm. After that, the power deceases inwards. The profiles of the phase shift between the MSEFs and the magnetic fluctuations by Fast Fourier Transformation analysis is also provided in figure 5 (b). The sign of the phase shift changes at \( \Delta r \sim -2.0 \) cm, indicating that the sign of the MSEF inverts at the q=3 surface. The reduction of the MSEF and the change of the sign for the MSEF around q=3 surface may come from the m/n=6/2 islands. The radius of q=3 surface is estimated by magnetic measurements.

### 3.3 Time evolutions of MSEFs and magnetic fluctuations

In order to understand the interaction mechanism of the GAMs and the magnetic fluctuations, the temporal evolutions of the MSEFs and magnetic fluctuations of m/n=6/2 are investigated. Figure 6(a) shows the spectrogram of the floating potential fluctuations in the MSEF frequency range at the radial position of \( \Delta r=-3.0 \) cm. In the
period of 500 - 530 ms, the MSEF frequency rapidly decreases from 15.5 kHz to 12.5 kHz. At the beginning of the ECRH heating, the MSEF is located at the frequency of ~ 12.5 kHz, and its frequency decreases continuously. After ~590 ms, the MSEF frequency becomes stable and is about 10.5 kHz. Figure 6 (b) also gives the spectrogram of the m/n=6/2 magnetic fluctuations. The m/n=6/2 magnetic fluctuations follow the MSEF frequency and its intensity increases gradually. At 20 ms after the ECRH switching off, i.e., at ~650 ms, the MSEF frequency decrease again and no significant magnetic fluctuation is observed at the MSEF frequency. The result suggests that the frequency entrainment of the GAM and the m/n=6/2 magnetic fluctuations exists during the ECRH heating.

The temporal evolutions of the coherencies between the MSEFs at the radial position of Δr=−3.0 cm and magnetic fluctuations are provided in figure 6 (c). The coherency was calculated as \( \gamma_{XY} = |C_{XY}| \). The time window is 5ms and the band pass filter of two signals is 9-16 kHz. The higher coherency suggests the existences of the stronger coupling between the MSEFs and the m/n=6/2 magnetic fluctuations. With ECRH heating, the increase of the coherency suggests that the coupling strength is enhanced, particularly, during 610-620 ms.

3.4 Phase lock between MSEFs and magnetic fluctuations
The phase lock is another important evidence to prove the frequency entrainment linked to the nonlinear synchronization of GAMs and magnetic fluctuations. Figure 7 shows the probability density function (PDF) of the phase shifts between MSEFs and magnetic fluctuations at different time slices. The phase shifts are estimated with the Hilbert transform. Before ECRH heating, no significant peak is observed at different time regions. This indicates that their phases are unlocked. After ECRH switching on, the peaks become significant and the half widths of the peaks become narrow, especially, during the periods of 600-610 and 610-620 ms. After ECRH switching off, the half widths of the peaks become wider and the peak disappears gradually. This result suggests that the phase shifts between GAMs and magnetic fluctuations are locked through adjusting their phases via nonlinear interaction during ECRH heating.

![Fig. 7. (color online) The probability density functions of phase shifts between MSEFs and magnetic fluctuations at different time slices.](image)

3.5 Nonlinear coupling of MSEFs and LFZFs to turbulence

The coupling of the LFZFs and MSEFs to turbulence is an important physics mechanism associated with LFZF and MSEF formation mechanism. The bicoherence analysis, an indicator for the strength of nonlinear three wave coupling, can be used to
prove the existence of the coupling of the LFZFs and MSEFs to turbulence. The squared auto-bicoherence \( \hat{b}_f(f_3) = |B(f_3)|^2 \left\{ \left< \phi_f(f_1)\phi_f(f_2) \right> \right\} \) of the perturbations is calculated. Here the bispectrum \( B(f_i) = \phi_f(f_i)\phi_f(f_2)\phi_f^*(f_3 = f_1 + f_2) \). The frequency resolution is 1 kHz. The number of realization is \( M = 472 \), and the noise level is 0.002 for the analysis. Figure 8(a) plots the squared auto-bicohence of the floating potential fluctuations in the frequency region of \( f_1 < 100 \) kHz, and \( f_2 = 100 - 100 \) kHz. The bicoherence in the frequency region of \( f_1 = 60 \) kHz, \( f_2 = -10.5 \) kHz, and \( f = f_1 + f_2 \sim 10.5 \) kHz is significantly above the noise level. This analysis suggests that the turbulence may contribute to the MSEF formation through the nonlinear three wave coupling. In addition, the values of the bicoherences in the frequency region of \( f_1 <= 60 \) kHz, \( f_2 = -0 - 4 \) kHz, and \( f = f_1 + f_2 \sim 0 - 4 \) kHz are higher. This indicates that the turbulence may also contribute to the LFZF formation [28]. The summed bicoherence is shown in figure 8(b). The peaks in the LFZF and MSEF frequency regions are clearly demonstrated.

3.6 Nonlinear coupling of MSEFs to LFZFs

The new mechanism for the LFZF formation is the coupling of the MSEFs and LFZFs. This differs from the turbulence driving and deserves to be studied. Figure 9 gives the zoomed-in plot of figure 8(a). The squared auto-bicoherence of the floating potential fluctuations in the frequency region of \( f_1 < 30 \) kHz, and \( f_2 = -30 - 30 \) kHz is presented. The higher values in the frequency region of \( f_1 = 9 - 14 \) kHz, \( f_2 = ~0 - 4 \) kHz,
and \( f = f_1 + f_2 \sim 0-4 \text{ kHz} \) are apparently shown. The observation suggests that it is possible that the LFZFs are created through three wave coupling between MSEFs and LFZFs.

### 3.7 Turbulence envelope modulation

The modulations of MSEFs and LFZFs on turbulence are analyzed with the envelope analysis. The coherencies between the MSEFs and the turbulence envelope, and between the LFZF and turbulence envelope in various frequency bands presented in figure 10 (a) indicate that both LFZFs and MSEFs modulate the turbulence and that the MSEFs mainly regulate the turbulence of frequencies higher than 100 kHz and lower than 200 kHz. Whereas the LFZF mainly modulates the turbulence of frequencies lower than 100 kHz. The tendencies of the modulation from LFZF and MSEFs are similar in the frequency regime higher than 300 kHz. The corresponding phase shifts are close to \( \pi/2 \) and \( \pi \) between the MSEF and the turbulence envelope, and between the LFZF and the turbulence envelope in various frequency bands, respectively, as given in figure 10 (b). Here, \( f_c \) is the central frequency of the selected frequency band.
3.8 MSEF envelope modulation

The effects of LFZFs on MSEFs are exploited with the envelope analysis of the MSEFs. The waveforms of the LFZF and the envelope (shown in figure 11) show that the LFZF is well correlated with the MSEF envelope and the phase shifts between them is close to $\pi$. This analysis suggests that the LFZF modulates the MSEFs.

![Figure 11. (color online) The waveforms of the LFZF and the turbulence envelopes.](image)

4. Discussion and conclusion

The synchronization of GAMs and magnetic fluctuations is observed in the edge plasmas of the HL-2A tokamak. The new MSEFs, resulting from the synchronization and having components of dominant GAM and m/n=6/2 potential fluctuations, are found at the same frequency as that of the magnetic fluctuations of m/n=6/2. The MSEFs couple to turbulence and LFZFs. Both the MSEFs and the LFZFs modulate the turbulence while the MSEFs are regulated by the LFZFs.

This experiment is designed to measure the mode numbers of GAMs (n=0) and potential fluctuations (m/n=6/2) with the same frequency and the radial distribution of the MSEFs simultaneously and performed with multiple discharges and with similar plasma parameters. For this analysis, 20 shots have been used, among which 17 shots show such a phenomenon unambiguously. Another example of the phase PDFs is provided in the figure 12. The analysis of the phase PDFs shows that the significant peaks in PDFs during the ECRH appear always, while the apparent peaks in PDFs before ECRH appear or disappear shot to shot.

The m/n=3/1 basic harmonic mode is not observed in the present experiments. This indicates that the m/n=6/2 mode does not come from the m/n=3/1 basic harmonic
mode. The turbulence-driven GAMs has close frequency with m/n=6/2 magnetic fluctuations. The synchronization of GAMs and magnetic fluctuations suggests that GAMs and magnetic fluctuations can transfer energy between each other through nonlinear synchronization. Therefore, the observation suggests that synchronization might contributes to the excitation of m/n=6/2 magnetic fluctuations. This can not be understood by the present theory. In this experiment, we also observed that the MSEFs interact with LFZFs and turbulence, suggesting that the synchronization contributes to the LFZF formation, and thus reduces turbulence level. The LFZF is a favorable for the L-H transitions [29]. Thus, we speculate that the synchronization can contribute to confinement regime transitions, especially L-H transitions. Note that the m/n=4/2 mode of f~12 kHz is not correlated with GAMs. The possible conjecture is that the q=2 rational surface is far away from the GAM location although the m/n=4/2 mode frequency is close to that of GAMs. The m/n=4/2 modes occur at the q=2 rational surface in the core plasmas while both the GAMs and the m/n=6/2 modes are localized in the edge plasmas. This difference between 4/2 and 6/2 modes gives a clue to understand the mechanism that causes observed synchronization.

Fig. 12. (color online) The probability density functions of phase shifts between MSEFs and magnetic fluctuations at different time slices.
The observation provides a problem definition to study nonlinear interactions among magnetic islands and the low frequency zonal flows and GAMs. It has been theoretically pointed that the mean and zonal flows and magnetic island interact directly [30-32], e.g., the influence by the flow on island growth [33] and that by magnetic island on flow [34] have been reported. The indirect interactions between flows and islands have also been extensively studied. Here, indirect means the interaction between them via change of turbulence. That is, the energy of microscopic turbulence is transferred to tearing modes [35-38], so that the fluctuation intensity and the drive of zonal flows by turbulence can be reduced. The magnetic islands enhance the damping rate of zonal flows, so that they affect the intensities of flows and turbulence simultaneously [39]. These theoretical studies have focused on the impacts, which are given as averaged values on the magnetic surface, so that the sensitivity to the phase of magnetic perturbation has not attracted attentions much. It has also been pointed out that the fluctuation intensity is modulated with the same period as magnetic islands [35, 36], and an initial observation was reported [40]. Therefore, there can be a coupling effect between them, which is sensitive to the phase of the magnetic island. The fact that the zonal flow is synchronous with the island actually suggests that the zonal flows see the islands, and respond to the island with sensitivity to the phase.

This study of the interactions of LFZFs and GAMs and magnetic fluctuations suggest that the phase dynamics of magnetic fluctuations and zonal flows can contribute to the coherent structure formation, and thus control the transport and plasma confinement.

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