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MODELING THE COMFORT EFFECTS OF SHORT-WAVE SOLAR RADIATION INDOORS

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ABSTRACT
Exposure to sunlight indoors produces a substantial effect on an occupant’s comfort and on the air conditioning energy needed to correct for it, yet has in the past not been considered in design or in thermal comfort standards. A public online model of the effects of solar radiation on human heat gain and comfort has been developed to make this possible. SolarCal is a whole-body model for ease of use in early design. Its predictions compare closely (<0.1 PMV mean absolute error) to results of a human subject test. It can be used to determine the allowable transmittance of fenestration in a perimeter office.

HIGHLIGHTS:
• SolarCal, a simplified whole-body model for the thermal comfort effects of shortwave solar radiation.
• Publicly available web interface for carrying out calculations using SolarCal http://smap.cbe.berkeley.edu/comforttool.
• SolarCal’s ability to predict the impact of solar radiation on occupant thermal comfort verified against lab study.
• Several practical design scenarios where SolarCal can be effectively applied.
• Practitioner guidance for using the model and gathering the necessary data.

KEYWORDS: Solar load, Thermal comfort, Thermal sensation, Shading, MRT, ERF

INTRODUCTION
Windows unshaded from direct solar radiation are common in commercial buildings. They often introduce significant problems by admitting large amounts of solar (aka shortwave) radiation indoors. Some of the problems are visual, such as glare, but three thermal ones are also very important.
First, in most buildings the heat gain from solar radiation absorbed indoors must be removed by energy-intensive air-conditioning. Second, solar gain in the occupied zone is intensely variable and difficult to control: in attempting to keep the temperature of a sunlit section under control, adjacent spaces are likely to be overcooled. A third issue is the topic of this paper: solar radiation landing on occupants directly affects their thermal comfort. The solar heat absorbed and liberated in clothing and skin must be offset by cooler air and surface temperatures around the body for the occupant to remain comfortably in thermal balance (Figure 1). The temperature offset may be substantial and beyond the corrective capacity of conventional cooling systems.

This third issue has received surprisingly little notice in the design or evaluation of buildings. For example, the relevant indoor environmental standards ASHRAE Standard 55 Thermal environmental conditions for human occupancy [2], EN-ISO Standard 7730 [5], and CEN-15251 [6] do not even mention shortwave radiation. Although Fanger published projected area factors for the human body in 1970 [7], the subject of shortwave gain and comfort has been almost absent from the research literature until recently. A few studies [8, 9, 16, 19] have addressed the effect of solar heating on comfort.

There are no readily available design tools for predicting the effect of solar radiation falling directly on occupants in buildings. Potential developers of such tools may have been discouraged by the complexity of the task: identifying an occupant’s position, determining the position of solar beam radiation on interior room surfaces, determining the shading and reflection from interior furnishings, and determining the effect of solar altitude and azimuth on the occupant’s non-cylindrical body shape.

There are complex multi-segment thermal physiology and comfort models that predict detailed radiative heat exchanges between the human body and its environment via view factors [11, 12, 13]. These models also predict solar loads on local body parts. For example, the commercial software RadTherm [20] distributes solar loads to local body segments in the Fiala thermophysiological model, from which local skin temperatures are predicted [11]. The Berkeley Advanced Comfort Model [15] performs the same
functions. In both of these, the predicted local skin temperatures are then converted to local thermal sensation and comfort using the Zhang et al. [14] comfort model. Multi-segment physiology and comfort models are most commonly used in automotive design. The process is more time-intensive and constrained than typical building design, in which speed of use is more of an issue. Multi-segment models may be linked with CFD simulation, and with advanced fenestration models. WINDOW 6.2 [17] predicts bidirectional scattering for solar radiation impinging on complex window systems (glass, louvers, and shades). The scattered solar might be linked to a human manikin in order to distribute solar loads on different body parts [10]. Solar scattering models have not yet been linked to thermophysiological and comfort models.

For the foreseeable future, building designers will need a way to quickly calculate the consequences of different levels of indoor solar radiation indoors on comfort, peak cooling load, and energy use. The comfort consequences should be quantified on well-accepted thermal comfort scales. The peak cooling load and energy consequences should be quantified by how much the space’s temperature would have to be reduced to offset the solar heat liberated on the occupant. The solar variables under the designer’s control would be: the presence or absence of sunlight on the person, the extent of the person’s body area exposed to direct sun, and the intensity of solar radiation after filtering through glass and window furnishings. Evaluating these variables may not require great geometric precision since occupants’ positions in buildings cannot be very precisely predicted or fixed.

This paper describes a solar calculator (SolarCal) that is incorporated in the Center for the Built Environment (CBE) web-based Comfort Tool [18]. The Comfort Tool contains the provisions of ASHRAE Standard 55 [2] as its core, but it also has optional features beyond the current requirements of the Standard [21]. SolarCal is based on a method developed by Arens et al [1] to evaluate the effect of solar radiation on comfort outdoors. The SolarCal model is intentionally simplified so it can be used to quickly estimate the solar radiation in undetermined environments or in environments with simple geometries. In this paper, we compare SolarCal simulations against a recent human subject test of solar effects and comfort, to evaluate the effectiveness of SolarCal’s simplified radiation calculations, and its ability to predict comfort in terms of predicted mean thermal sensation votes (PMV) [7]. We also estimate the level of window shading needed to prevent unacceptable PMV increases for occupants near windows.

**METHOD OF CALCULATING SOLAR GAIN TO THE BODY INDOORS**

The SolarCal model is based on the effective radiant field (ERF), a measure of the net radiant energy flux to or from the human body. ERF is used to describe the additional (positive or negative) long-wave radiation energy at the body surface when surrounding surface temperatures are different from the air temperature. It is in W/m², where area...
refers to body surface area. The surrounding surface temperature of a space is commonly expressed as *mean radiant temperature* (MRT). The ERF on the human body from long-wave exchange with surfaces is related to MRT by:

\[
ERF = f_{eff} \cdot h_r \cdot (MRT - T_a) \tag{1}
\]

where \( f_{eff} \) is the fraction of the body surface exposed to radiation from the environment (=0.696 for a seated person and 0.725 for a standing person [7]); \( h_r \) is the radiation heat transfer coefficient (W/m² K); and \( T_a \) is the air temperature (°C).

The energy flux actually absorbed by the body is ERF times the long-wave emissivity/absorptivity \( \alpha_{LW} \), typically equal to 0.95. Solar radiation absorbed on the body’s surface can be equated to an additional amount of longwave flux, \( E_{RF_{solar}} \):

\[
\alpha_{LW} \cdot E_{RF_{solar}} = \alpha_{SW} \cdot E_{solar} \tag{2}
\]

where \( E_{solar} \) is the short wave solar radiant flux on the body surface (W/m²); \( \alpha_{SW} \) is short-wave absorptivity, ≈0.67 for (white) skin and average clothing.

\( E_{solar} \) is the sum of three fluxes that have been filtered by fenestration properties and geometry, and are distributed on the occupant body surface: direct beam solar energy coming directly from the sun \( (E_{dir}) \), diffuse solar energy coming from the sky vault \( (E_{diff}) \), and solar energy reflected upward from the floor \( (E_{refl}) \). These are defined below.

Diffuse radiation from the sky is assumed to be distributed on the upper half of the radiatively-exposed portion of the body.

\[
E_{diff} = 0.5 \cdot f_{svv} \cdot T_{sol} \cdot I_{diff} \tag{3}
\]

where \( f_{svv} \) is the fraction of sky vault in occupant’s view (Figure 2); \( I_{diff} \) is diffuse sky irradiance received on an upward-facing horizontal surface (W/m²); \( I_{diff} \) is a standard meteorological parameter measured in open terrain (Note: in less open terrain, natural and built surfaces protruding above the horizon block the diffuse sky radiation behind them. SolarCal assumes that that the reduction in \( I_{diff} \) is compensated for by the radiation reflected from the surfaces. In clear weather the angular fluxes from reflected and diffuse sky are roughly equal); \( T_{sol} \) is the total solar transmittance, the ratio of incident shortwave radiation to the total shortwave radiation passing through the glass and shades of a window system.

The total outdoor solar radiation on the horizontal \( (I_{TH}) \) is filtered by both \( T_{sol} \) and \( f_{svvs} \) and multiplied by the reflectance (albedo) of the floor and lower furnishings \( (R_{floor}) \). In addition, the short-wave reflected to the lower half of the body will be accompanied by
increased long-wave radiation from floor surfaces warmed by the non-reflected portion of the solar. This long-wave flux may be approximated by increasing the value of \( R_{\text{floor}} \).

\[
E_{\text{refl}} = 0.5 f_{\text{eff}} f_{\text{svv}} T_{\text{sol}} I_{TH} R_{\text{floor}}
\]

where \( I_{TH} \) is the total horizontal direct and diffuse irradiance outdoors (W/m\(^2\)); and \( R_{\text{floor}} \) is the floor reflectance (a value might be (0.2 to 0.3) for short-wave plus long-wave combined).

Direct radiation affects only the projected area \( A_p \) of the body, and is reduced by any shading of the body provided by the indoor surroundings:

\[
E_{\text{dir}} = \left( \frac{A_p}{A_D} \right) f_{\text{bes}} T_{\text{sol}} I_{\text{dir}}
\]

where \( A_p \) is the projected area of a standard person exposed to direct beam sunlight; \( A_D \) is the DuBois surface area of the assumed person (around 1.8 m\(^2\)); \( f_{\text{bes}} \) is the fraction of body exposed to sunlight (Figure 3. Note that this measure does not include the body’s self-shading, only the shading from surroundings); and \( I_{\text{dir}} \) is direct beam (normal) solar radiation (W/m\(^2\)). The meteorological radiation parameters are related as: \( I_{TH} = I_{\text{dir}} \sin \beta + I_{\text{diff}} \), where \( \beta \) is the solar altitude.

\[\text{Figure 2. Fraction of sky vault in occupant’s view (f}_{\text{svv}})\]

\[\text{Figure 3. Fraction of body exposed to sun (f}_{\text{bes}})\]

\( E_{\text{REF solar}} \) can therefore be calculated from the following equation:

\[
E_{\text{REF solar}} = (0.5 f_{\text{eff}} f_{\text{svv}} (I_{\text{diff}} + I_{TH} R_{\text{floor}}) + A_p f_{\text{bes}} I_{\text{dir}} / A_D) T_{\text{sol}} (\alpha_{SW}/\alpha_{LW})
\]

In direct beam sunlight, the projected area of a human body varies with solar altitude and azimuth. Fanger [7] quantified this using the empirically determined projected area factor \( (f_p) \):

\[
A_p = f_{\text{eff}} f_p A_D
\]
In the CBE Comfort tool, $f_p$ for seated and standing postures were taken from the graphs in ASHRAE Standard 55-2013 [2] and fit using a 2-D interpolating spline (Figure 4).

![Figure 4. Projected area of body exposed to sun ($A_p$) as a function of altitude and azimuth, in standing posture (left) and seated posture (right). Azimuth zero represents the sun in front of the occupant.](image)

To obtain $ERF_{solar}$ with equation (6), the inputs are $f_{svs}, f_p, T_{sol}, f_{bes}, I_{diff}, I_{TH}, R_{floor}, I_{dir}, \alpha_{SW}$, and $\alpha_{LW}$ along with solar altitude ($\beta$) and azimuth. To reduce the climate data input in SolarCal, $I_{diff}$ may be estimated as $I_{diff} = 0.17 I_{dir} \sin \beta$. Finally, $ERF_{solar}$ is added to the longwave ERF input to determine a new solar-adjusted MRT ($\Delta MRT$) using equation (1). This allows a new PMV to be calculated for an occupant exposed to shortwave radiation.

**INPUT DATA**

The following paragraphs suggest methods for obtaining good estimates for the SolarCal input parameters.

Direct beam solar radiation ($I_{dir}$) values can be found in Typical Meteorological Year (TMY) weather files [22]. The column labeled DNI (Direct Normal Intensity) contains a year’s worth of representative hourly solar intensity data, which can be used to derive a design condition. For example, the 95th percentile of the daily maximum DNI may be a reasonable design condition. Should hourly weather data not be available, Table 1 contains direct solar beam radiation data for a standard cloudless atmosphere [4] that can be used in this situation. The best value can be chosen by considering the latitude of the site and the season of the design condition. For example, the maximum solar altitude occurring on the summer solstice in Berkeley, CA is about 75°, corresponding to a design condition of 915 W/m².
Table 1. Typical direct beam solar radiation values for a standard cloudless atmosphere depending on the solar altitude angle.

<table>
<thead>
<tr>
<th>Solar altitude angle [°]</th>
<th>5</th>
<th>10</th>
<th>20</th>
<th>30</th>
<th>40</th>
<th>50</th>
<th>60</th>
<th>70</th>
<th>80</th>
<th>90</th>
</tr>
</thead>
<tbody>
<tr>
<td>Direct beam solar radiation [W/m²]</td>
<td>210</td>
<td>390</td>
<td>620</td>
<td>740</td>
<td>810</td>
<td>860</td>
<td>890</td>
<td>910</td>
<td>920</td>
<td>925</td>
</tr>
</tbody>
</table>

The sky vault view fraction, $f_{svv}$, may be estimated directly or with a simple equation. It is equal to the ratio of the sky vault covered by the window aperture after it is projected onto the sky vault from the position of the occupant. This value depends mostly on the dimensions of the window (width $w$, height $h$) and the distance between the occupant and the window ($d$). With these values we can derive the approximation

$$f_{svv} \approx \frac{\tan^{-1}\left(\frac{h}{2d}\right) \tan^{-1}\left(\frac{w}{2d}\right)}{90^\circ}$$

(8)

where the inverse tangent function returns values in degrees. When calculating $f_{svv}$ for multiple windows, the $f_{svv}$ for each may be calculated and summed to get an approximate total $f_{svv}$. Note that exterior objects obstructing the sky vault should not be considered, since they have a similar diffuse reflectivity as the sky vault.

Figure 5. From the moving walkway, the altitude angle to the top of the window is approximately 60°. Since the width of the window is very large, we have a $f_{svv}$ value of about 1/3. Image courtesy of YuFeng Zhang
The solar transmittance $T_{sol}$ is most easily obtained from the International Glazing Database, containing data from many glazing manufacturers [23]. The database is included in the WINDOW software developed by LBNL [24].

Transmittance is sometimes specified in terms of shading coefficient (SC). SC is by definition referenced to the radiation passing through clear glass with a $T_{sol}$ of 0.87. Similarly, center-of-glass Solar Heat Gain Coefficient (SHGC) provides an approximation of $T_{sol}$. These metrics differ from $T_{sol}$ in that they include the inward longwave flux resulting from shortwave radiation absorbed in the glass. This additional flux does not arrive at the occupant in the collimated beam of direct shortwave radiation. Using SC and SHGC, the model will tend to overpredict solar gain on the occupant when glass absorptance is high, or the occupant is further from the window.

In SolarCal, the solar altitude/azimuth parameters only determine the radiation incident on the occupant. Transmission through the building’s fenestration also depends on the angle of the sun relative to the glazing, but the SolarCal model does not extend to including the glazing orientation. It is the designer’s responsibility to adjust $T_{sol}$ for transmission reductions caused by non-normal solar incidence angles on the window.

The shortwave absorptivity $\alpha_{SW}$ of the occupant may range widely depending on the color of the occupant’s skin, as well as the color and amount of clothing covering the body. In the SolarCal web tool, we choose 0.67 as a reasonable estimate for this value. If the user has specific assumptions about the clothing or skin color of the occupants, a more accurate estimate can be calculated using Table 2 [3].

Table 2. Shortwave absorptivity ($\alpha_{SW}$) values for common clothing and skin types.

<table>
<thead>
<tr>
<th></th>
<th>White clothing</th>
<th>Khaki clothing</th>
<th>Black clothing</th>
<th>White skin</th>
<th>Brown skin</th>
<th>Black skin</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\alpha_{SW}$</td>
<td>0.2</td>
<td>0.57</td>
<td>0.88</td>
<td>0.57</td>
<td>0.65</td>
<td>0.84</td>
</tr>
</tbody>
</table>

Note: because SolarCal is a whole-body model, it cannot differentiate between local body parts (such as check, back, hand etc.), or between body parts with or without clothing. Comfort effects stemming from such differences must be modeled with multiple-segment comfort models as described in the Introduction above [15, 20].

COMPARING MODEL PREDICTIONS TO A HUMAN SUBJECT TEST

Hodder and Parsons (‘H/P’) used an automobile mockup (Figure 6) with moveable heat lamps to emulate four levels of solar radiation impinging on human subjects [8]. Air temperature was between 22.8 and 24.0°C, metabolic rate 1.2 met, and clothing resistance 0.7 clo. Figure 7 shows the input variables for modeling the test, as represented in the SolarCal interface.
Table 3 first shows solar loads on the subject (W/m²) predicted by SolarCal’s $A_p$ method and by BCM’s detailed 5000 polygon manikin; SolarCal is 7% low. The $\Delta MRT$ from SolarCal is then compared to $\Delta MRT$ calculated from H/P’s globe thermometer readings. The two $\Delta MRT$ values were then used to calculate PMV. The experiment found that 200 W/m² solar gain produced an increase of roughly one PMV scale unit. The SolarCal PMV prediction agrees well with the experiment’s actual thermal sensation votes (<0.1 PMV mean absolute error), which use the identical scale as PMV. The discrepancies are less than 0.15 scale unit except with zero radiation.

<table>
<thead>
<tr>
<th>Solar radiation level (W/m²)</th>
<th>600</th>
<th>400</th>
<th>200</th>
<th>0</th>
</tr>
</thead>
<tbody>
<tr>
<td>Air temperature (°C)</td>
<td>24.0</td>
<td>23.4</td>
<td>23.4</td>
<td>22.8</td>
</tr>
<tr>
<td>Solar load (W/m²)</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>BCM with 5000 polygon manikin</td>
<td>103.4</td>
<td>68.9</td>
<td>34.5</td>
<td>0</td>
</tr>
<tr>
<td>SolarCal model</td>
<td>96.7</td>
<td>64.4</td>
<td>32.2</td>
<td>0</td>
</tr>
<tr>
<td>$\Delta \text{MRT}$</td>
<td>H/P test using Globe T</td>
<td>20.0</td>
<td>18.4</td>
<td>14.3</td>
</tr>
<tr>
<td>-----------------</td>
<td>------------------------</td>
<td>------</td>
<td>------</td>
<td>------</td>
</tr>
<tr>
<td>SolarCal model</td>
<td></td>
<td>23.1</td>
<td>15.4</td>
<td>7.7</td>
</tr>
<tr>
<td>PMV</td>
<td>H/P results using computed $\text{MRT}$</td>
<td>2.8</td>
<td>2.3</td>
<td>1.9</td>
</tr>
<tr>
<td>SolarCal model</td>
<td></td>
<td>3.1</td>
<td>1.9</td>
<td>0.9</td>
</tr>
<tr>
<td>Actual mean thermal sensation vote in H/P experiment</td>
<td>3.1</td>
<td>1.9</td>
<td>1.1</td>
<td>0.2</td>
</tr>
</tbody>
</table>

**CALCULATION EXAMPLES**

In this section we will develop two example SolarCal calculations.

1) Should skylights admit solar radiation onto the occupant from overhead, SolarCal can be used to assess the resulting comfort impact. The designer must determine a time in the year when direct solar radiation strikes the occupant, and obtain $T_{\text{sol}}$ for that time, accounting for the incidence angle of the solar beam on the skylight glazing.

Assume the occupant is seated and a horizontal skylight with dimensions 2m x 2m is 4m is directly above the occupant. The site is Miami, FL, where the solar altitude angle in summer is high enough to admit direct solar through this skylight onto the occupant. For a maximum solar altitude angle of 87°, use Table 1 to determine a direct solar beam intensity of 925 W/m². The skylight glass has a rated $T_{\text{sol}}$ of 0.2, which will remain about the same for this near-normal solar incidence angle.

Only the occupant’s lower legs will be shaded by the desk under this overhead sun angle, so the $f_{\text{hse}}$ is 0.9. We will assume shortwave absorptivity of 0.7. The floor is covered with a dark carpet with reflectivity of 0.2. We will assume the longwave from the absorbed solar gain in the carpet adds another 0.3 to the floor reflectance, for a total of 0.5. The $f_{\text{svv}}$ is approximated from equation (8):

$$f_{\text{svv}} \approx \frac{\tan^{-1}\left(\frac{2}{n}\right) \tan^{-1}\left(\frac{2}{n}\right)}{90 \times 180} = 0.01$$  \hspace{1cm} (9)

These conditions result in a MRT delta of 3.9°C, and an ERF of 16.5 W/m². We will discuss the significance of this later.

Notice that if this modest skylight is enlarged to a size often seen in glazed atria ($f_{\text{svv}} \sim 0.5$) the MRT delta increases to a MRT delta of 8.2°C and an ERF of 34.2 W/m².

2) Here we analyze a shading design for an occupant placed near a window, as in Figure 1. The solar altitude is 75° with a direct solar intensity of 910 W/m². The vertical glass has a rated $T_{\text{sol}}$ of 0.5, which the designer determines to be 0.3 for the sun angle under consideration. The occupant is seated facing the 3m x 3m window at a distance of 1m, yielding a $f_{\text{svv}}$ of 0.32. In this case we will assume that half of the body is shaded by the furniture of the occupant, and that the absorptivity is 0.7. A light beige-colored floor

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has a total SW+LW reflectivity of 0.6. Under these conditions, the $\Delta MRT$ is 8.0°C. The results of this are plotted in Figure 8. In both cases, the air temperature (25°C) and relative humidity (50%) are represented by the red dot, airspeed is 0.1 m/s, clothing is a typical summer ensemble (0.5 CLO), and the metabolic rate is 1.2 MET. On the left hand side, the MRT is 25°C. On the right, the MRT is 33°C, after the 8.0°C adjustment. The blue area represents the comfort zone on the chart for the respective conditions, where the PMV is between -0.5 and 0.5.

Figure 8. The psychrometric chart with comfort zone representing the range of -0.5 to 0.5 PMV before (L) and after (R) an 8.0°C $\Delta MRT$ has been applied to a typical comfort model input condition. The tool is available online:
http://smap.cbe.berkeley.edu/comforttool.

The solar increase to MRT clearly produces an unmanageable shift in the occupant’s comfort zone, moving the occupant well outside its boundaries with a high PMV. The designer can use the model to evaluate solar control options that reduce this heat gain.

APPLICATION TO SHADING
The PMV increase caused by short-wave solar radiation can be used to determine a practical maximum for allowable $T_{sol}$ in architectural interiors.

It seems reasonable to assume that solar gain in a typical conditioned office should not increase the occupant’s PMV more than one-half a scale unit (e.g., from 0 to +0.5, starting at the neutral temperature and increasing to the upper boundary of the comfort zone).

The total $T_{sol}$ required to limit occupant overheating is shown in Table 2 for the geometry of a simulated perimeter zone cubicle shown in Figure 9. $I_{de} = 900$ W/m², solar altitude = 65°, $f_{svv} = 0.3$, $f_{bes} = 0.5$, and $R_{floor} = 0.5$. The indoor environment is: air speed = 0.1 m/s, relative humidity = 50%; and occupant clothing = 0.57 clo. The sun is from the side at 90° azimuth, and activity is 1.1 met.
Table 2. Solar transmission ($T_{sol}$) that limits an occupant’s PMV increase to one-half scale unit

<table>
<thead>
<tr>
<th>Metabolic rate (met)</th>
<th>Azimuth 30°</th>
<th>Azimuth 90°</th>
<th>Azimuth 120°</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>12.2%</td>
<td>13.5%</td>
<td>14.1%</td>
</tr>
<tr>
<td>1.1</td>
<td>13.5%</td>
<td>14.9%</td>
<td>15.5%</td>
</tr>
<tr>
<td>1.2</td>
<td>15.2%</td>
<td>16.7%</td>
<td>17.5%</td>
</tr>
<tr>
<td>1.3</td>
<td>16.4%</td>
<td>18.1%</td>
<td>18.9%</td>
</tr>
</tbody>
</table>

Figure 9. Office cubicle geometry

However, if a building were being maintained at the cool boundary of the comfort zone, solar gain might usefully increase the occupant’s PMV by as much as one scale unit. (For energy reasons, this strategy should only be allowed in the heating season!). Figure 10 uses the above cubicle example to show the boundary of allowable $T_{sol}$ for a range of indoor ambient temperature conditions. It is the red line representing the PMV = 0.5 contour. The blue and black lines in the figure are the PMV=0 and PMV= - 0.5 contours, respectively. An ambient temperature deviation of 1.5ºC from neutral corresponds to a 0.5 PMV scale change, as does a 0.15 change in $T_{sol}$.

Figure 10. $T_{sol}$ boundary predicted by the SolarCal model
In the absence of solar gain, lowering 1.5°C from neutral causes thermal sensation to drop from PMV=0 to -0.5. Adding solar radiation 15% $T_{sol}$ brings thermal sensation up 0.5 PMV units, back to neutral. To reach the upper threshold (PMV=0.5) from this lower temperature, $T_{sol}$ can be as high as 30% before PMV exceeds 0.5. However, above neutral ambient temperatures (the right side of the figure), the allowable $T_{sol}$ must be below 0.15, reaching zero at 1.5°C above neutral.

**LIST OF SYMBOLS**

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
<th>Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>MRT</td>
<td>Mean radiant temperature</td>
<td>°C</td>
</tr>
<tr>
<td>ERF</td>
<td>Effective radiant field</td>
<td>W/m²</td>
</tr>
<tr>
<td>$I_{eff}$</td>
<td>Fraction of body exposed to sun</td>
<td>-</td>
</tr>
<tr>
<td>$h_r$</td>
<td>Radiation heat transfer coefficient</td>
<td>W/m²-K</td>
</tr>
<tr>
<td>$T_a$</td>
<td>Air temperature</td>
<td>°C</td>
</tr>
<tr>
<td>$\alpha_{LW}$</td>
<td>Longwave radiation absorptivity</td>
<td>-</td>
</tr>
<tr>
<td>$\alpha_{SW}$</td>
<td>Shortwave radiation absorptivity</td>
<td>-</td>
</tr>
<tr>
<td>$ERF_{solar}$</td>
<td>Effective radiant field solar component</td>
<td>W/m²</td>
</tr>
<tr>
<td>$E_{solar}$</td>
<td>Total shortwave solar radiant flux</td>
<td>W/m²</td>
</tr>
<tr>
<td>$E_{dir}$</td>
<td>Direct beam component of shortwave solar radiant flux</td>
<td>W/m²</td>
</tr>
<tr>
<td>$E_{diff}$</td>
<td>Diffuse component of shortwave solar radiant flux</td>
<td>W/m²</td>
</tr>
<tr>
<td>$E_{refl}$</td>
<td>Reflected component of shortwave solar radiant flux</td>
<td>W/m²</td>
</tr>
<tr>
<td>$f_{svv}$</td>
<td>Fraction of sky vault exposed to body</td>
<td>-</td>
</tr>
<tr>
<td>$T_{sol}$</td>
<td>Glazing solar transmittance</td>
<td>-</td>
</tr>
<tr>
<td>$I_{dir}$</td>
<td>Direct solar beam intensity</td>
<td>W/m²</td>
</tr>
<tr>
<td>$I_{diff}$</td>
<td>Diffuse solar intensity</td>
<td>W/m²</td>
</tr>
<tr>
<td>$I_{TH}$</td>
<td>Total horizontal solar intensity</td>
<td>W/m²</td>
</tr>
<tr>
<td>$R_{floor}$</td>
<td>Floor reflectivity</td>
<td>-</td>
</tr>
<tr>
<td>$A_p$</td>
<td>Projected area</td>
<td>m²</td>
</tr>
<tr>
<td>$f_{bes}$</td>
<td>Fraction of body exposed to sun</td>
<td>-</td>
</tr>
<tr>
<td>$\beta$</td>
<td>Solar altitude angle</td>
<td>deg</td>
</tr>
</tbody>
</table>

**CONCLUSIONS**

- The direct warming effect of solar radiation on occupants may cause discomfort, and require a large amount of correction by the cooling system. It should be accounted for in architectural and engineering design, preferably early in the process. This paper describes SolarCal, a new public online web-based tool for
predicting solar effects on comfort.

- The SolarCal model computes an increase in MRT equivalent to shortwave gains from direct, diffuse, and indoor-reflected radiation on a person. This is then used to compute PMV using the method prescribed in ASHRAE Standard 55-2013.

- Comparison of results from SolarCal, the advanced multi-segment Berkeley Comfort Model, and a physical experiment shows SolarCal giving reasonable predictions of solar effects on MRT, and on comfort expressed as PMV.

- Low solar transmittance is needed to prevent excessive increase in occupants’ thermal sensation indoors. The transmission of glass plus shades together probably should not exceed 15% if the sun will be shining on an occupant indoors.

REFERENCES


WEB REFERENCES


