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Permalink
https://escholarship.org/uc/item/8ht4k5js

Journal
Physical Review D, 97(9)

ISSN
2470-0010

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Publication Date
2018

DOI
10.1103/PhysRevD.97.092006

Peer reviewed
Search for photonic signatures of gauge-mediated supersymmetry in 13 TeV pp collisions with the ATLAS detector

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(Received 12 February 2018; published 22 May 2018)

A search is presented for photonic signatures, motivated by generalized models of gauge-mediated supersymmetry breaking. This search makes use of proton-proton collision data at \( \sqrt{s} = 13 \) TeV corresponding to an integrated luminosity of 36.1 fb\(^{-1}\) recorded by the ATLAS detector at the LHC, and it explores models dominated by both strong and electroweak production of supersymmetric partner states. Experimental signatures incorporating an isolated photon and significant missing transverse momentum are explored. These signatures include events with an additional photon or additional jet activity not associated with any specific underlying quark flavor. No significant excess of events is observed above the Standard Model prediction, and 95% confidence-level upper limits of between 0.083 and 0.32 fb are set on the visible cross section of contributions from physics beyond the Standard Model. These results are interpreted in terms of lower limits on the masses of gluinos, squarks, and gauginos in the context of generalized models of gauge-mediated supersymmetry, which reach as high as 2.3 TeV for strongly produced and 1.3 TeV for weakly produced supersymmetric partner pairs.

DOI: 10.1103/PhysRevD.97.092006

I. INTRODUCTION

This paper reports on a search for two complementary classes of events containing energetic isolated photons and large missing transverse momentum (with magnitude denoted \( E_{T}^{\text{miss}} \)). The search is performed with proton-proton (pp) collision data at a center-of-mass energy \( \sqrt{s} = 13 \) TeV corresponding to an integrated luminosity of 36.1 fb\(^{-1}\) recorded with the ATLAS detector at the Large Hadron Collider (LHC) in 2015 and 2016. For the first of the two classes, two isolated energetic photons are required (“diphoton” events), while for the second class only a single isolated photon is required, in combination with multiple hadronic jets (“photon + jets” events).

The results of searches for these two classes of events are interpreted in the context of several general models of gauge-mediated supersymmetry breaking (GGM) [1,2]. These models include both the production of supersymmetric partners of strongly coupled Standard Model (SM) particles and the production of partners of SM particles possessing only electroweak charge. In all models of GGM, the lightest supersymmetric particle (LSP) is the gravitino \( \tilde{G} \) (the partner of the hypothetical quantum of the gravitational field), with a mass significantly less than 1 GeV. In the GGM models considered here, the decay of the supersymmetric states produced in LHC collisions would proceed through the next-to-lightest supersymmetric particle (NLSP), which would then decay to the \( \tilde{G} \) LSP and one or more SM particles. Each of the two event classes corresponds to a specific choice of NLSP, each of which in turn has a high probability of decay into \( \gamma + \tilde{G} \). In all models considered, all supersymmetric states with the exception of the \( \tilde{G} \) are short lived, leading to prompt production of SM particles that are observed in the ATLAS detector. The result based on the diphoton signature extends and supplants an ATLAS search [3] performed with an integrated luminosity of 3.2 fb\(^{-1}\) of pp collision data taken at a center-of-mass energy of \( \sqrt{s} = 13 \) TeV, and complements searches [4,5] performed by the CMS Collaboration making use of 35.9 fb\(^{-1}\) of \( \sqrt{s} = 13 \) TeV pp collision data. The result based on the photon + jets signature extends and supplants an ATLAS search [6] performed with an integrated luminosity of 20.3 fb\(^{-1}\) of 8 TeV pp collision data.

The paper is organized as follows. More details of the theoretical background are provided in Sec. II. Section III presents the salient features of the ATLAS detector. Section IV provides details of the Monte Carlo simulations used in the analysis for background and signal processes. Section V discusses the reconstruction and identification of photons, leptons, jets, and whole-event observables relevant to the event selection, while Sec. VI describes the event selection itself. The estimation of background

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contributions and signal efficiency, and the study of systematic uncertainties are discussed in Secs. VII and VIII. The results are presented in Sec. IX and are interpreted in terms of limits on various GGM models. Finally, Sec. X is devoted to the conclusions.

II. GAUGE-MEDIATED SUPERSYMMETRY PHENOMENOLOGY

Supersymmetry (SUSY) [7–14] introduces a symmetry between fermions and bosons, resulting in a SUSY partner (sparticle) for each SM particle with identical quantum numbers except a difference by half a unit of spin. As none of these sparticles have been observed, SUSY must be a broken symmetry if realized in nature. Assuming R-parity conservation [15–19], sparticles are produced in pairs. These then decay through cascades involving other sparticles until the stable, weakly interacting LSP is produced, leading to a final state with significant $E_T^{miss}$.

This paper considers experimental signatures associated with models inspired by gauge-mediated SUSY breaking [20–25]. These signatures are largely determined by the nature of the NLSP; in GGM models, the NLSP is often formed from an admixture of any of the SUSY partners of the electroweak gauge and Higgs bosons. In this study, two cases are considered for the composition of the NLSP, both of which would produce photonic signatures in the ATLAS detector. In the first case, the NLSP is assumed to be purely binolike [the SUSY partner of the SM U(1) gauge boson], while in the second case, the NLSP is assumed to be an admixture of bino and neutral higgsino states. In this paper, the neutral NLSP is denoted $\tilde{\chi}_1^0$ irrespective of its composition.

Where not explicitly constrained by the assumptions of the specific GGM models under study, the masses and properties of SUSY partner states are controlled by several underlying parameters. These include the U(1), SU(2), and SU(3) gauge partner mass parameters ($M_1$, $M_2$, and $M_3$, respectively), the higgsino mass parameter $\mu$, the gravitino mass, and the ratio $\tan\beta$ of the two SUSY Higgs-doublet vacuum expectation values. A value of 1.5 is chosen for the latter; for all GGM models considered, the phenomenology relevant to this search is only weakly dependent on the value of $\tan\beta$.

If the NLSP is binolike, the final decay in each of the two cascades in a GGM SUSY event is predominantly $\tilde{\chi}_1^0 \rightarrow \gamma + G$, leading to final states with two photons and missing transverse momentum. If the NLSP is a mixture of the bino and higgsino, the higgsino mass parameter $\mu$ is chosen to be positive, leading to final decays split primarily between the modes $\tilde{\chi}_1^0 \rightarrow \gamma + \tilde{G}$ and $\tilde{\chi}_1^0 \rightarrow Z + \tilde{G}$, and thus a preponderance of final states with a single photon accompanied by multiple jets and $E_T^{miss}$. To provide a signature advantageous for the photon + jets analysis, the values of $\mu$ and $M_1$ are chosen so that, to within $\sim 1\%$, the $\tilde{\chi}_1^0$ branching fractions are $B(\tilde{\chi}_1^0 \rightarrow \gamma \tilde{G}) \sim 50\%$, $B(\tilde{\chi}_1^0 \rightarrow Z \tilde{G}) \sim 49\%$, and $B(\tilde{\chi}_1^0 \rightarrow h \tilde{G}) \sim 1\%$, irrespective of the mass of the $\tilde{\chi}_1^0$ neutralino ($h$ represents the scalar state observed at 125 GeV, assumed here to be the lightest CP-even state of the SUSY Higgs spectrum). Although not explored here, the choice $\mu < 0$ would lead to decays that prefer the production of the $h$ boson over the $Z$ boson, producing decays rich in $b$-quark jets but otherwise similar to the $\mu > 0$ case.

The results of the diphoton and photon + jets analyses are interpreted in the context of four distinct GGM models. Three of the GGM models are associated with the diphoton analysis, each featuring a purely binolike NLSP and distinguished by the state directly produced by the proton-proton collision. For the first of the three GGM models associated with the diphoton analysis, referred to as the “gluino-bino” model, production proceeds through a degenerate octet of gluinos, collectively denoted by $\tilde{g}$ (Fig. 1 left). For the second of these models (the “wino-bino” model; Fig. 1 right), production proceeds through a degenerate triplet of the SU(2) gauge partner (wino, or $W$) states $\tilde{\chi}^0_2$ and $\tilde{\chi}^0_1$, and is dominated by the production of $\tilde{\chi}^+_1$ and $\tilde{\chi}^+_0$ $\tilde{\chi}^-_0$. For the third of these models (the “squark-bino” model; Fig. 2 left), production proceeds through the squark states. All squark states are taken to be degenerate in mass, with the exception of the partners of the three right-handed up-type quarks, whose masses are decoupled (set to inaccessibly large values) in order to satisfy GGM sum rules [2]. For a binolike NLSP, the cross section for direct $\tilde{\chi}^0_1$ pair production is essentially zero for any value of the $\tilde{\chi}^0_1$ mass. For the ‘higgsino-bino’ GGM model associated with the photon + jets analysis (Fig. 2 right), for which the NLSP is chosen to be a mixture of the bino and higgsino, production again proceeds through a degenerate octet of gluino states. In this last case, however, there is a leading-order coupling between initial-state partons and the higgsino component of the $\tilde{\chi}_1^0$ neutralino, leading to a

$^1$For the case of left-handed top squark (stop) production when $m_{\tilde{t}_L} < m_{\tilde{g}} + m_{\tilde{q}}$, the stop decay proceeds through an effective neutral current interaction to a charm or up quark accompanied by the binolike $\tilde{\chi}_1^0$.
SUSY production process dominated by $\tilde{\chi}^0_1$ pair production for low values of the $\tilde{\chi}^0_1$ neutralino mass. However, the efficiency for detecting such events in the photon + jets analysis is very small, and so direct $\tilde{\chi}^0_1$ pair production is expected to play no role in the analysis.

For all four GGM models, the masses of both the NLSP and the directly produced states are taken to be free parameters of the model, with all other SUSY partner masses other than those of the gravitino and $h$ state decoupled. The lifetime $\tau_{\tilde{\chi}^0_1}$ of the NLSP is set so that $c\tau_{\tilde{\chi}^0_1}$ is never greater than 0.1 mm. This ensures that all particles arising from the decay of the NLSP are prompt, and in particular that the relationship between the direction and the point of impact on the face of the calorimeter of photons from NLSP decay is consistent with that of a prompt photon (a separate analysis [26] searches for GGM models with a longer-lived binolike NLSP, leading to signatures with nonprompt photons).

III. ATLAS DETECTOR

The ATLAS detector [27] consists of an inner tracking system surrounded by a superconducting solenoid, electromagnetic (EM) and hadronic sampling calorimeters, and a muon spectrometer. The inner detector is immersed in a 2 T axial magnetic field and consists of pixel and silicon microstrip detectors inside a transition radiation tracker, providing charged-particle tracking in the region $|\eta| < 2.5$.\(^2\)

For the $\sqrt{s} = 13$ TeV run, a new innermost layer of the pixel detector, the “insertable B-layer” [28], was added at an average radius of 33 mm. The EM calorimeter uses lead as the absorber and liquid argon (LAr) as the active material. In the central rapidity region $|\eta| \lesssim 1.5$, the EM calorimeter is divided into three layers longitudinal in shower depth, one of them segmented into very narrow $\eta$ strips for optimal $\gamma/\pi^0$ separation. The EM calorimeter is augmented by a presampler layer for $|\eta| < 1.8$. Hadron calorimetry is based on different detector technologies, with scintillator tiles ($|\eta| < 1.7$) or LAr ($1.5 < |\eta| < 4.9$) as the active medium, and with steel, copper, or tungsten as the absorber material. The muon spectrometer consists of superconducting air-core toroids, a system of trigger chambers covering the range $|\eta| < 2.4$, and high-precision tracking chambers allowing muon momentum measurements for $|\eta| < 2.7$. ATLAS uses a two-level trigger system to select events [29]. A low-level hardware trigger is implemented in custom electronics and reduces the data rate to a design value of $\sim 100$ kHz using a subset of detector information. A high-level software trigger selects events with interesting final states using software algorithms that access the full detector information, reducing the average accepted event rate to $\sim 1$ kHz.

IV. SAMPLES OF SIMULATED PROCESSES

Samples of simulated events for various $pp$ collision processes are used to estimate the signal efficiency, develop and optimize the signal region (SR) selection, and in some cases estimate SM background contributions to the SRs. For the GGM model used to interpret the photon + jets results, the SUSY mass spectra and branching fractions are calculated using SUSPECT 2.43 [30] and SDECAY 1.5 [31], respectively, inside the package SUSY-HIT 1.5a [32], and with Higgs boson decay provided by HDECAY 3.4 [33]. For the GGM models used to interpret the diphoton results, the SUSY mass spectra and branching fractions are calculated using SUSPECT 2.41 [30] and SDECAY 1.3b [31], respectively. For all models, the Monte Carlo (MC) SUSY signal samples were generated to leading-order accuracy using MG5_aMC@NLO v2.3.3 [34], with up to two extra partons included beyond the underlying $2 \rightarrow 2$ SUSY production process. The simulation used the NNPDF2.3LO parton distribution functions (PDF) set [35], and was interfaced to PYTHIA 8.212 [36] with the ATLAS A14 set of tuned parameters [37] for the modeling of the parton showering, hadronization, and underlying event. Strong and electroweak SUSY production cross sections are calculated to next-to-leading order (NLO) in the strong coupling constant, adding the resummation of soft gluon emission at next-to-leading-logarithm accuracy (NLO + NLL) [38–44]. The nominal cross section and its uncertainty are taken from an envelope of cross-section predictions using different PDF sets and factorization and renormalization scales, as described in Ref. [45].

\(^2\)ATLAS uses a right-handed coordinate system with its origin at the nominal interaction point (IP) in the center of the detector and the $z$ axis along the beam pipe. The $x$ axis points from the IP to the center of the LHC ring, and the $y$ axis points upwards. Cylindrical coordinates $(r, \phi)$ are used in the transverse plane, $\phi$ being the azimuthal angle measured relative to the $x$ axis. The pseudorapidity is defined in terms of the polar angle $\theta$ as $\eta = -\ln[\tan(\theta/2)]$. Angular distance is measured in units of $\Delta R \equiv \sqrt{(\Delta \eta)^2 + (\Delta \phi)^2}$. A related quantity, $\Delta R_{\gamma}$, makes use of rapidity $\gamma$ rather than pseudorapidity $\eta$ to define phase-space separation: $\Delta R_{\gamma} \equiv \sqrt{(\Delta \gamma)^2 + (\Delta \phi)^2}$.\(^2\)
While most of the backgrounds to the GGM models under examination are estimated through the use of control samples selected from data, as described below, the extrapolation from control regions (CRs) to signal regions depends on samples of simulated events, as do the optimization studies. Simulated SM processes include single-photon and diphoton production both with and without an associated vector boson, $t\bar{t}$ production both with and without an accompanying photon, and multijet production. With the exception of the $t\bar{t}\gamma$ process, Standard Model processes were generated using the SHERPA 2.1.1 simulation package [46], making use of the CT10 [47] PDF set. Matrix elements were calculated for up to three-parton emission at leading order (LO) using the COMIX [48] generator and then combined with the SHERPA parton shower [49] according to an improved CKKW procedure [50]. The $t\bar{t}\gamma$ process was generated to next-to-leading-order accuracy using MG5_aMC@NLO v2.3.3 [34] in conjunction with PYTHIA 8.186 [51] with the NNPDF2.3LO PDF set and the A14 set of tuned parameters.

All MC samples were processed with the GEANT4-based simulation [52,53] of the ATLAS detector, or, where appropriate, a simulation of the ATLAS detector based on parametrized shower shapes in the calorimeter and GEANT4 elsewhere. Corrections are applied to the samples of simulated events to account for differences between data and simulation in the photon-based trigger, identification, and reconstruction efficiencies, as well as for the efficiency and misidentification rate of the algorithm used to identify jets containing $b$-hadrons ($b$-tagging). The effect of additional $pp$ interactions per bunch crossing (“pileup”) is taken into account by overlaying simulated minimum-bias events according to the observed distribution of the number of pileup interactions in data.

V. RECONSTRUCTION OF CANDIDATES AND OBSERVABLES

Primary vertices are formed from sets of two or more tracks, each with transverse momentum $p_T > 400$ MeV, that are consistent with having originated at the same three-dimensional space point within the luminous region of the colliding proton beams. When more than one such primary vertex is found, the vertex with the largest scalar sum of the squared transverse momenta of the associated tracks is chosen.

Electron candidates are reconstructed from EM calorimeter energy clusters consistent with having arisen from the impact of an electromagnetic particle (electron or photon) upon the face of the calorimeter. For the object to be considered an electron, it is required to match a track reconstructed by an algorithm optimized for recognizing charged particles with a high probability of bremsstrahlung. Electrons are required to pass a “tight” set of identification requirements as defined in Refs. [54–56], based on the characteristics of the EM shower development, the quality of the associated reconstructed track, and the quality of the association of the track with the calorimeter deposition. Electron candidates used by these searches are further required to have $p_T > 25$ GeV and $|\eta| < 2.47$, but excluding the transition region $1.37 < |\eta| < 1.52$ between the barrel and end cap calorimeters. A track-based isolation requirement is imposed, with the scalar sum of the transverse momenta of tracks within a cone of size $\Delta R = 0.2$ (excluding that of the electron candidate’s track) required to be less than a value that leads to a loss of efficiency of 5% for electrons with $p_T = 25$ GeV, and of less than 1% for electrons with $p_T > 60$ GeV. Finally, the electron track is required to be consistent with having originated from the primary vertex in the $r$-$z$ plane.

Electromagnetic clusters in the range $|\eta| < 2.37$ (excluding the transition region $1.37 < |\eta| < 1.52$) are classified as photon candidates provided that they either have no matched track (“unconverted” photons) or have one or more matched tracks consistent with having originated from a photon conversion vertex (“converted” photons). Photon candidates are required to have $E_T^{\gamma} > 25$ GeV, where $E_T^{\gamma}$ is the energy of the photon candidate, measured in the EM calorimeter, multiplied by the cosine of the angle of its trajectory relative to the plane perpendicular to the $z$ axis. The photon direction is estimated either using EM calorimeter shower-depth segmentation (if unconverted) or the position of the conversion vertex (if converted), together with constraints from the $pp$ collision point. Photon candidates are also required to fulfill “loose” or “tight” identification criteria [57,58] based on observables that reflect the shape of the electromagnetic showers in the calorimeter, in particular in the finely segmented first layer. While tight photons are required for all SRs, loose photons are used to construct control samples that aid in the estimation of backgrounds arising from misreconstructed jets. If an EM calorimeter deposition is identified as both a photon and an electron, the photon candidate is discarded and the electron candidate retained. Additionally, a calorimeter-based isolation requirement is imposed: after correcting for contributions from pileup and the deposition ascribed to the photon itself, the transverse energy $E_T^{\gamma} = 0.4$ deposited in a cone of size $\Delta R = 0.4$ surrounding the photon candidate’s energy deposition must satisfy the relation $E_T^{\gamma} < 2.75$ GeV + $0.22 \times E_T^{\gamma}$, with $E_T^{\gamma}$ in GeV.

Muon candidates are reconstructed via a combination of track information from the muon spectrometer and the inner tracking systems. Muons must pass the “medium” identification requirements defined in Ref. [59], based on requirements on the number of hits in the different inner detector and muon spectrometer subsystems, and on the significance of the charge-to-momentum ratio measurement. Muon candidates are required to have $p_T > 25$ GeV and $|\eta| < 2.7$. Muon candidates are also required to pass an isolation requirement identical to that for electron candidates. Finally, the muon track is required to be consistent
with having originated from the primary vertex in both the r-z and r-φ planes.

Making use of utilities within the FastJet package [60], jets are reconstructed from three-dimensional energy clusters in the calorimeter [61] with the anti-κ0, jet clustering algorithm [62] with a radius parameter R = 0.4. In the diphoton analysis, only jet candidates with p_T > 30 GeV and |η| < 2.8 are considered. For jets used in the photon + jets analysis, the acceptance is further reduced to |η| < 2.5. Jets are calibrated as described in Refs. [63,64], with the expected average energy contribution from pileup clusters subtracted in accordance with the angular area of the jet. Jets resulting from the hadronization of b-quarks are identified using the multivariate MV2c10 b-tagging algorithm, which is based on quantities such as impact parameters of associated tracks, and reconstructed secondary vertices [65,66]. This algorithm is used at a working point that provides 77% b-tagging efficiency in simulated t̄t̄ events, and a rejection factor of 134 for light-quark and gluon jets and 6 for charm jets.

To avoid ambiguity that arises when an electron or photon is also reconstructed as a jet, the following procedure is used: if a jet and an electron or photon are reconstructed with a separation of ΔR < 0.2, the electron or photon is retained and the jet is discarded; if 0.2 < ΔR < 0.4, then the jet is retained and the electron or photon is discarded. Finally, in order to suppress the reconstruction of muons arising from showers induced by jets, if a jet and a muon are found with ΔR < 0.4, the jet is retained and the muon is discarded.

The vector momentum imbalance E_Tmiss in the transverse plane is obtained from the negative vector sum of the reconstructed and calibrated physics objects, and an additional soft term. The soft term is constructed from all tracks that are not associated with any reconstructed electron, muon, or jet, but which are associated with the primary vertex.

Several additional observables are defined to help in the discrimination of SM backgrounds from potential GGM signals. The “effective mass” m_eff is defined as the scalar sum of the transverse energy of identified photons, any additional leptons and jets in the event, plus the value of E_Tmiss. The “photon-enhanced” total visible transverse energy observable H_T is defined as the transverse energy of the selected photons and any additional leptons and jets in the event, without the addition of E_Tmiss. In this case the contribution from photonic signatures is emphasized by discarding the photon-jet ambiguity resolution procedure when identifying photons and jets. Requiring a minimum value for either of these observables exploits the high energy scale associated with the production of massive SUSY partners. The photon-E_Tmiss separation Δφ(γ, E_Tmiss) is defined as the azimuthal angle between the E_Tmiss vector and the selected photon. In the diphoton analysis, Δφ_min(γ, E_Tmiss) is defined to be the minimum value of Δφ(γ, E_Tmiss) of the two selected photons. The minimum jet-E_Tmiss separation Δφ_min(jet, E_Tmiss) is defined as the minimum azimuthal angle between the E_Tmiss vector and the two leading (highest-p_T) jets in the event. For the diphoton analysis, leading jets are required to have p_T > 75 GeV for the purpose of constructing this observable, and if no such jet is found no requirement is placed on the observable. Small values of these angular-separation observables are often associated with SM backgrounds arising from poorly reconstructed photons or jets. Finally, the quantity R_T is defined as the scalar sum of the transverse momenta of the four highest-p_T jets in the event divided by the scalar sum of the transverse momenta of all jets in the event; smaller values of R_T are typical for the jet-rich events of the higgsino-bino GGM model that is the focus of the photon + jets analysis.

VI. EVENT SELECTION

The data sample is selected by a trigger requiring the presence of one loose photon with E_T > 140 GeV for the photon + jets analysis or two loose photons with E_T > 35 GeV and E_T > 25 GeV, respectively, for the diphoton analysis. After applying data-quality requirements related to the beam and detector conditions, the total available integrated luminosity is 36.1 fb^{-1}.

For the diphoton analysis, targeting the exploration of the gluino-bino, squark-bino, and wino-bino GGM models incorporating a purely binolike ˜χ^0_1, two separate SR selection strategies are used: a “SR_H” selection targeting the production of higher-mass strongly coupled SUSY states (gluinos and squarks) and a “SR_W” selection targeting the production of lower-mass weakly coupled SUSY states (winos). For each of these approaches, two SRs are defined: the first (SR_L, L) optimized for the case of a lower-mass ˜χ^0_1 and the second (SR_H, H) for a higher-mass ˜χ^0_1. For fixed production-scale (gluino, squark, wino) mass, increasing the mass of the bino NLSP increases the energy carried off by the unobserved gravitinos, at the expense of the overall visible energy deposition.

For the photon + jets analysis, targeting the higgsino-bino GGM model, a further two SRs are defined. The first of these (SR_H) is optimized for a high-mass gluino and a low-to-intermediate mass neutralino, for which there is a large mass difference between the gluino and the neutralino. Such events are characterized by large jet multiplicity and exceptional hadronic activity, but moderate missing transverse momentum. The second of these SRs targets the compressed scenario for which the difference between the gluino and neutralino masses is small, resulting in lower jet multiplicity and suppressed hadronic activity while producing harder photons and greater missing transverse momentum.
All four diphoton SRs require two tight, isolated photons with $E_T > 75$ GeV, while SR$_{Zj}$ and SR$_{Rj}$ require a single tight, isolated photon with $E_T > 145$ GeV and $E_T > 400$ GeV, respectively. To exploit the transverse momentum imbalance created by the unobservable gravitinos, an event must exhibit significant $E_T^{miss}$ to be included in any of the SRs. To ensure that the $E_T^{miss}$ observable is accurately measured, minimum requirements on $\Delta \phi_{\text{min}}(\gamma, E_T^{miss})$ and $\Delta \phi_{\text{min}}(\text{jet}, E_T^{miss})$ are considered for each SR.

Requirements are made on a number of additional observables, defined in Sec. V, with values chosen to optimize the sensitivity to the GGM signal of interest in each SR. To exploit the high energy scale associated with SUSY production at masses close to the expected limit of sensitivity of the various SRs, all SRs include minimum requirements on one of the two total-transverse-energy observables $H_T$ or $m_{\text{jet}}$. As an illustration, Fig. 3 (left) shows the $H_T$ distribution of diphoton events as well as that expected from SM sources (estimated as described in Sec. VII) and from four characteristic scenarios of the binolike NLSP GGM gluino-production model. Due to the large backgrounds arising from SM single-photon production, requirements must be placed on additional observables in order to optimize the signal sensitivity in the photon + jets analysis. A minimum of five (three) jets is required for events in SR$_{Zj}$ (SR$_{Rj}$). For SR$_{Zj}$ of the photon + jets analysis, an additional requirement that events have $R_T^4 < 0.90$ helps reduce the background from SM events, which tend to have fewer and softer jets than do signal events. Examples of the discriminating power of the $R_T^4$ observable are shown in Fig. 3 (right). Finally, for both SR$_{Zj}$ and SR$_{Rj}$, events with one or more leptons (electron or muon) are rejected in order to suppress the contribution from SM events containing leptonically decaying $W$ or $Z$ bosons produced in association with a hard radiated photon (“$W\gamma$” production). In addition, a predecessor to SR$_{Zj}$, originally designed for a search using a smaller data set (13.2 fb$^{-1}$), has been retained, as the number of events observed in that search exceeded the background prediction. This third photon + jets SR is referred to as SR$_{Zj}^{200}$ and differs from SR$_{Zj}$ only by the relaxed requirement $E_T^{miss} > 200$ GeV relative to the $E_T^{miss} > 300$ GeV requirement of SR$_{Zj}$. A summary of the selection requirements for the various SRs is presented in Table I.

VII. BACKGROUND ESTIMATION

Backgrounds to the various SRs arise from a number of sources that generate real photons in combination with
energetic neutrinos, as well as events in which one or more energetic jets or electrons are misidentified as photons. In the following, the methodology of the background estimation for the two experimental signatures is discussed, and the resulting background estimates, broken down by source, are tabulated. Backgrounds arising from misidentified jets and electrons are estimated through the use of control samples including jets or electrons, scaled by efficiencies and rates determined from data. Other backgrounds are estimated via MC simulation, often constrained by observed event counts in dedicated CRs. For the estimation of background contributions that rely upon MC simulation, either directly or through the estimation of "transfer factors" relating the background content of CRs to that of corresponding SRs, the effect of MC modeling uncertainties is considered.

In the photon + jets analysis, expected SM backgrounds constrained by CRs are determined separately for each SR with a maximum-likelihood fit, referred to as the "background-only fit." The background-only fit constrains the normalization of the dominant backgrounds to the observed event yields in the associated CRs, assuming that no signal is present in the CRs. The inputs to the fit for each SR include the numbers of events observed in its associated CRs and the number of events predicted by simulation in each region for all background processes. The latter are described by Poisson statistics. The systematic uncertainties in the expected values are included in the fit as nuisance parameters, modeled by Gaussian distributions with widths corresponding to the sizes of the associated uncertainties. Correlations between the various CRs are taken into account. The product of the various probability density functions forms the likelihood, which the fit maximizes by adjusting the background normalization and the nuisance parameters. Background models are confirmed in validation regions (VRs) with selection criteria closely related to those of the corresponding SR, but with one or more selection criteria modified to suppress the potential contribution of a GGM signal to the VR.

### A. Backgrounds to the diphoton analysis

Backgrounds from SM contributions to the four diphoton SRs are grouped into three primary components. The first of these, referred to as "QCD background," arises from a mixture of processes that include $\gamma\gamma$ production as well as $\gamma$ + jet and multijet events with at least one jet misreconstructed as a photon. The second background component, referred to as "EW background," is due primarily to $W + X$ (here "X" can be any number of jets, accompanied by no more than one photon; the two-photon case is treated separately) and $t\bar{t}$ events. These events tend to include final-state neutrinos that produce significant $E_T^{miss}$. In both cases, EW background events entering the signal regions generally have at least one electron misreconstructed as a photon. The QCD and EW backgrounds are estimated through the use of dedicated control samples of data events.

The third background component, referred to as "irreducible," consists of $W$ and $Z$ bosons produced in association with two real photons, with a subsequent decay into one or more neutrinos. For this background, the $W(\rightarrow\ell\nu) + \gamma\gamma$ component dominates and requires corrections to its LO contribution that are both large and rapidly varying across the phase space of the $W(\rightarrow\ell\nu) + \gamma\gamma$ (plus possible additional jets) process [67]. Thus a data-driven approach is developed to constrain the $W(\rightarrow\ell\nu) + \gamma\gamma$ contribution to the four SRs. The $Z(\rightarrow\ell\ell) + \gamma\gamma$ contribution is estimated directly from the MC simulation.

The QCD background to SR$_{S-L}^{W\gamma}$, SR$_{S-H}^{W\gamma}$, SR$_{W-L}^{W\gamma}$, and SR$_{W-H}^{W\gamma}$ is expected to arise from events with a single real, isolated photon and a jet whose fragmentation fluctuates in such a manner as to cause it to be misidentified as a second isolated photon ("jet → $\gamma$" events), and, to a lesser extent, from events with two real, isolated photons unaccompanied by any additional electroweak bosons ("QCD diphoton" events). The contribution from dijet events is found to be small and largely incorporated into the jet → $\gamma$ background estimate.

To estimate the jet → $\gamma$ contribution, a "QCD control sample" is identified within the diphoton-trigger data
The estimated level of agreement between data and simulation is obtained by counting the number of scaled QCD events containing jets to reproduce the observed numbers of jets in each bin in the number of observed jets, values of $E_T$, and for each bin in the number of observed jets, values of $E_T$ and $\eta$. The statistical uncertainty in each estimate is determined from the unscaled number of events in the QCD control and diphoton MC samples that satisfy these requirements. If no events remain in the given sample, a one-sided statistical uncertainty is adopted, corresponding to the 68% confidence level (C.L.) Poisson upper limit on the possible background contribution. An additional uncertainty of $\pm 50\%$ is included to account for possible modeling uncertainties. The resulting QCD background estimates and their overall uncertainties are shown in Table II, separately for the jet $\to \gamma$ and QCD diphoton contributions.

The EW background is estimated via an “electron-photon control sample” composed of events with at least one isolated tight photon and one isolated electron, each with $E_T > 75$ GeV; when there is more than one identified electron, the one with the highest $p_T$ is used. The electron-photon control sample is scaled by the probability for such an electron to be misreconstructed as a tight photon, as estimated from a comparison of the rate of $Z$ boson reconstruction in the $e\gamma$ and $ee$ final states. The electron-to-photon scale factor varies between 1% and 5%, with larger factors associated with larger values of $|\eta|$, since the misidentification rate depends on the amount of material in front of the calorimeter. Events with additional photons or leptons are vetoed from the control sample to preserve its orthogonality to the various diphoton and photon + jets SRs. After applying all additional selection requirements to the scaled electron-photon control sample, and including a systematic uncertainty of $\pm 20\%$ associated with the determination of the scale factor, the resulting estimates of the EW background to the four diphoton SRs are shown in Table II.

The $W(\to\ell\nu) + \gamma\gamma$ background to the four diphoton SRs is estimated using a lepton-diphoton ($\ell\gamma\gamma$) CR. To enhance the contribution of $W(\to\ell\nu) + \gamma\gamma$ and to ensure that the $\ell\gamma\gamma$ CR is exclusive of the four SRs, the photon $E_T$ requirement is lowered to 50 GeV and a requirement of $50 < E_T^{\text{miss}} < 150$ GeV is imposed. To ensure that the CR sample arises from the same region of the $W(\to\ell\nu) + \gamma\gamma$ process phase space as the expected background, a further requirement that the transverse momentum of the $\gamma\gamma$ system be greater than 100 GeV is imposed. A total of 13 events is observed in the CR, for which MC simulation suggests that 3.9 events are expected to arise from SM sources other than $W(\to\ell\nu) + \gamma\gamma$. In the limit that no GGM signal contributes to the $\ell\gamma\gamma$ control region, an enhancement factor of $1.6 \pm 0.6 \pm 0.4$ must be applied to the $W(\to\ell\nu) + \gamma\gamma$

<table>
<thead>
<tr>
<th>Signal region</th>
<th>$\text{SR}<em>{\gamma\gamma}^{T</em>{S-L}}$</th>
<th>$\text{SR}<em>{\gamma\gamma}^{T</em>{H}}$</th>
<th>$\text{SR}<em>{W</em>{-L}}^{T_{S-L}}$</th>
<th>$\text{SR}<em>{W</em>{-H}}^{T}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Jet $\to \gamma$</td>
<td>$0.19^{+0.21}_{-0.10}$</td>
<td>$0.19^{+0.21}_{-0.10}$</td>
<td>$0.93 \pm 0.67$</td>
<td>$0.19^{+0.21}_{-0.10}$</td>
</tr>
<tr>
<td>QCD diphoton</td>
<td>$0.00^{+0.17}_{-0.00}$</td>
<td>$0.00^{+0.17}_{-0.00}$</td>
<td>$0.15^{+0.17}_{-0.15}$</td>
<td>$0.00^{+0.17}_{-0.00}$</td>
</tr>
<tr>
<td>EW background</td>
<td>$0.08 \pm 0.04$</td>
<td>$0.06 \pm 0.04$</td>
<td>$0.88 \pm 0.23$</td>
<td>$0.51 \pm 0.15$</td>
</tr>
<tr>
<td>$(W \to \ell\nu)\gamma\gamma$</td>
<td>$0.22 \pm 0.14$</td>
<td>$0.21 \pm 0.13$</td>
<td>$1.55 \pm 0.78$</td>
<td>$1.08 \pm 0.56$</td>
</tr>
<tr>
<td>$(Z \to \nu\nu)\gamma\gamma$</td>
<td>$0.01 \pm 0.01$</td>
<td>$0.03 \pm 0.02$</td>
<td>$0.15 \pm 0.08$</td>
<td>$0.27 \pm 0.13$</td>
</tr>
<tr>
<td>Expected background events</td>
<td>$0.50^{+0.30}_{-0.26}$</td>
<td>$0.48^{+0.30}_{-0.25}$</td>
<td>$3.7 \pm 1.1$</td>
<td>$2.05^{+0.65}_{-0.63}$</td>
</tr>
<tr>
<td>Observed events</td>
<td>$0$</td>
<td>$0$</td>
<td>$6$</td>
<td>$1$</td>
</tr>
</tbody>
</table>
TABLE III. Definition, expected content, and observed content of the seven validation regions used to confirm the diphoton analysis background model. Here, $N_{\text{exp}}$ is the number of required leptons of the stated type, and $N_{\text{exp}}$ and $N_{\text{obs}}$ are the expected and observed numbers of events, respectively. The remainder of the quantities are defined in the text. Events satisfying the selection requirements of any of the four diphoton signal regions are excluded from these validation regions. The uncertainties in the numbers of expected events are the combined statistical and systematic uncertainties. An ellipsis is entered when no such requirement is made of the given validation region.

<table>
<thead>
<tr>
<th>Region</th>
<th>$E_T^\gamma$ [GeV]</th>
<th>$\Delta \phi_{\text{min}}$ (jet, $E_T^\gamma$)</th>
<th>$N_{\text{lep}}$</th>
<th>$H_T$ [GeV]</th>
<th>$E_T^{\text{miss}}$ [GeV]</th>
<th>$N_{\text{exp}}$</th>
<th>$N_{\text{obs}}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>VR1/7</td>
<td>$&gt; 75$</td>
<td>$&gt; 0.5$</td>
<td>$\cdots$</td>
<td>$\cdots$</td>
<td>$&lt; 150$</td>
<td>$43500 \pm 4400$</td>
<td>$43918$</td>
</tr>
<tr>
<td>VR2/7</td>
<td>$&gt; 75$</td>
<td>$&gt; 0.5$</td>
<td>$\cdots$</td>
<td>$1000 - 2500$</td>
<td>$&lt; 150$</td>
<td>$2850 \pm 520$</td>
<td>$3139$</td>
</tr>
<tr>
<td>VR3/7</td>
<td>$&gt; 75$</td>
<td>$&gt; 0.5$</td>
<td>$\cdots$</td>
<td>$100 - 150$</td>
<td>$\cdots$</td>
<td>$112 \pm 36$</td>
<td>$109$</td>
</tr>
<tr>
<td>VR4/7</td>
<td>$&gt; 50$</td>
<td>$\cdots$</td>
<td>$1\mu$</td>
<td>$&lt; 2000$</td>
<td>$\cdots$</td>
<td>$34.5 \pm 7.2$</td>
<td>$38$</td>
</tr>
<tr>
<td>VR5/7</td>
<td>$&gt; 50$</td>
<td>$\cdots$</td>
<td>$1\mu$</td>
<td>$&lt; 2000$</td>
<td>$\cdots$</td>
<td>$19.8 \pm 7.1$</td>
<td>$25$</td>
</tr>
<tr>
<td>VR6/7</td>
<td>$&gt; 75$</td>
<td>$&gt; 0.5$</td>
<td>$\cdots$</td>
<td>$&gt; 1750$</td>
<td>$\cdots$</td>
<td>$290 \pm 130$</td>
<td>$336$</td>
</tr>
<tr>
<td>VR7/7</td>
<td>$&gt; 75$</td>
<td>$&gt; 0.5$</td>
<td>$\cdots$</td>
<td>$\cdots$</td>
<td>$&gt; 100$</td>
<td>$139 \pm 40$</td>
<td>$146$</td>
</tr>
</tbody>
</table>

MC sample to achieve agreement between the MC simulation and data in the $\ell\ell\gamma$ control region. The statistical uncertainty of $\pm 0.6$ arises from the Poisson error in the difference between the observed number of events in the $\ell\ell\gamma$ control region and the number of events expected from SM processes other than $W(\rightarrow \ell\nu)+\gamma\gamma$ production. The systematic uncertainty of $\pm 0.4$ arises from assuming that the non-$W(\rightarrow \ell\nu)+\gamma\gamma$ contributions to the $\ell\ell\gamma$ CR have an uncertainty of 100%; this uncertainty dominates smaller contributions arising from potential mismodeling of the detector response. For each diphoton SR, the $W(\rightarrow \ell\nu)+\gamma\gamma$ background estimate is then provided by applying all associated SR requirements to the scaled $W(\rightarrow \ell\nu)+\gamma\gamma$ MC sample. The resulting $W(\rightarrow \ell\nu)+\gamma\gamma$ background estimate in each of the four SRs, assuming that there is no signal contribution to the $\ell\ell\gamma$ CR, is shown in Table II. Also shown is the combined background estimate, including uncertainty, from all SM sources; for the $Z(\rightarrow \nu\bar{\nu})+\gamma\gamma$ background, an uncertainty of $\pm 45\%$ is assigned to account for the effect of QCD scale dependence associated with the limited-order simulation of the $Z(\rightarrow \nu\bar{\nu})+\gamma\gamma$ process discussed in Sec. IV.

The accuracy of the resulting overall background model is confirmed by the use of seven VRs that, while excluding events in the four diphoton SRs, have kinematic properties similar to those of the signal region. The definitions of these VRs are shown in Table III, together with the expected and observed numbers of events in each region. Figure 4 also shows this comparison, with the expected number of events broken down into its contributing SM sources.

Figure 5 shows the distribution of the missing transverse momentum $E_T^{\text{miss}}$ for the sample satisfying all requirements of the SR$_{W-H}^\gamma$ (left) and SR$_{W-L}^\gamma$ (right) selections except the $E_T^{\text{miss}}$ requirement itself. Overlaid are the expected SM backgrounds, separated into the various contributing sources.

B. Backgrounds to the photon + jets analysis

Backgrounds from SM contributions to the three photon + jets SRs are expected to arise from both events

FIG. 4. Comparisons between expected and observed content of the validation and signal regions for the diphoton analysis. The uncertainties in the numbers of expected events are the combined statistical and systematic uncertainties. The lower panel shows the pull (difference between observed and expected event counts normalized by the uncertainty) for each region.
with real photons and events for which an electron or a jet is misidentified as a photon. The former source is expected to receive contributions from events in which a W/Z boson or a t\bar{t} pair is produced in association with a real photon (Wγ, Zγ, and t\bar{t}γ backgrounds), with neutrinos in the subsequent weak decays of these produced states providing significant $E_T^{\text{miss}}$. The contribution from single-top production in association with a high-energy photon is expected to be negligible. Events with real photons can also contribute to the background in the photon + jets analysis when significant $E_T^{\text{miss}}$ arises from instrumental sources (QCD background). The Wγ, t\bar{t}γ, and QCD backgrounds are estimated by constraining a corresponding MC sample to match the observed event count in a dedicated CR enriched in the given background process but otherwise kinematically similar to the given SR, making use of the maximum-likelihood approach described at the beginning of this section. The MC simulation is then used to provide an estimate of the expected background in the photon + jets SRs. Smaller contributions from Zγ and WW (with or without an accompanying W or Z boson) production are estimated directly from the MC simulation. The methods used to estimate contributions from events for which electrons (“e → γ” backgrounds) or jets (“jet → γ” backgrounds) are misidentified as photons are identical to those used in the diphoton analysis, with the exception that the single-photon trigger sample is used instead of the diphoton trigger sample, the requirement that the electron or loose photon be accompanied by a tight isolated photon is removed, and the requirement for photons to be considered poorly isolated is changed to $8 < E_T^{\text{miss}} - 0.22 \times E_T^{\text{eff}} - 2.45 < 27$ GeV.

All CRs require at least one isolated photon with $E_T > 145$ GeV. The QCD-background control region CRγ+jets is similar to SRγL, but with the $E_T^{\text{miss}}$ requirement lowered to $E_T^{\text{miss}} > 100$ GeV, the $R_T^0$ requirement removed, the number of required jets lowered to three, and the $\Delta\phi_{\text{min}}(\text{jet}, E_T^{\text{miss}})$ requirement inverted. This provides a region dominated by real photons arising from radiative QCD processes that is otherwise fairly similar to the photon + jets SRs. The Wγ-background control region CRWγ is defined by requiring that there be one or more isolated leptons (electron or muon), at least one jet, and no b-tagged jet in the event. In addition, the $E_T^{\text{miss}}$ requirement is changed to $100 < E_T^{\text{miss}} < 200$ GeV and the $m_{\text{eff}}$ requirement reduced to $m_{\text{eff}} > 500$ GeV in order to enhance and isolate the Wγ contribution. The t\bar{t}γ-background control region CRt\bar{t}γ is defined similarly, but requires at least two jets and that two of the jets are b-tagged jets. In order to increase the number of events in the CR the $E_T^{\text{miss}}$ requirement is lowered to $50 < E_T^{\text{miss}} < 200$ GeV. Both the Wγ-background and t\bar{t}γ-background CRs maintain the requirement $\Delta\phi_{\text{min}}(\text{jet}, E_T^{\text{miss}}) > 0.4$. Table IV summarizes the selection criteria for the three photon + jets analysis CRs.

The event counts in the resulting QCD, Wγ, and t\bar{t}γ CRs are used to scale the $\gamma + \text{jet}$, Wγ, and t\bar{t}γ MC samples, respectively, after applying a selection identical to that of
the corresponding CR. The scale factors are determined in a simultaneous fit to all CRs, taking into account mutual cross contamination between the different backgrounds. The scale factors (ratio of the derived background contribution in the corresponding control region to the MC expectation) are found to be $1.67 \pm 0.49, 1.24 \pm 0.11,$ and $1.20 \pm 0.17$ for the QCD, $W\gamma,$ and $t\bar{t}\gamma$ backgrounds, respectively. The resulting SR contributions from the QCD, $W\gamma,$ and $t\bar{t}\gamma$ processes depend upon transfer factors, given by MC simulation, that relate the contribution of a given background process in the CR to that in the SR. Uncertainties in the transfer factors include those arising from experimental uncertainties in the efficiency for identifying objects and in measuring their energy, as well as theoretical uncertainties that are estimated by varying the underlying PDF set and renormalization and factorization scales used in the generation of the MC background samples. These uncertainties are incorporated into the overall background estimate uncertainties that arise from the simultaneous fit. Estimates for the contributions of the three real-photon backgrounds are shown in Table V, with the overall uncertainty taking into account correlations between the various background sources. For the three photon + jets SRs, the systematic uncertainty in each background estimate is dominated by the theoretical uncertainties in the relevant MC samples and the experimental uncertainties in the jet energy scale and resolution.

The accuracy of the resulting photon + jets analysis background model is confirmed by the use of 11 VRs. Similar to the diphoton analysis VRs, these VRs exclude events in the various photon + jets SRs while having kinematic properties similar to those of the signal region. Validation regions $VR1^{j}$ through $VR6^{j}$, defined in Table VI, target the confirmation of the modeling of backgrounds arising from $\gamma$ + jets production. Validation regions $VR7^{j}$ through $VR11^{j}$, defined in Table VII, target

### Table IV

Selection criteria for the three photon + jets analysis control regions. Here, $N_{\gamma}$ is the number of required photons, $E_{\gamma}^{T}$ the transverse energy of the leading photon, $N_{\text{lep}}$ the number of required leptons, $N_{\text{jets}}$ the number of required jets, and $N_{b\text{-jets}}$ the number of required $b$-quark jets. The remainder of the quantities are defined in the text. An ellipsis is entered when no such requirement is made in the given control region.

<table>
<thead>
<tr>
<th>CR$_{\gamma+jets}$</th>
<th>CR$_{W\gamma}$</th>
<th>CR$_{t\bar{t}\gamma}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$N_{\gamma}$</td>
<td>$\geq 1$</td>
<td>$\geq 1$</td>
</tr>
<tr>
<td>$E_{\gamma}^{T}$</td>
<td>$&gt;145$ GeV</td>
<td>$&gt;145$ GeV</td>
</tr>
<tr>
<td>$N_{\text{lep}}$</td>
<td>$0$</td>
<td>$\geq 1$</td>
</tr>
<tr>
<td>$E_{\text{miss}}^{\gamma}$</td>
<td>$&gt;100$ GeV</td>
<td>$100$–200 GeV</td>
</tr>
<tr>
<td>$N_{\text{jets}}$</td>
<td>$\geq 3$</td>
<td>$\geq 1$</td>
</tr>
<tr>
<td>$N_{b\text{-jets}}$</td>
<td>$\cdots$</td>
<td>$0$</td>
</tr>
<tr>
<td>$\Delta \phi(\text{jet}, E_{\text{miss}}^{\gamma})$</td>
<td>$&lt;0.4$</td>
<td>$&gt;0.4$</td>
</tr>
<tr>
<td>$\Delta \phi(\gamma, E_{\text{miss}}^{\gamma})$</td>
<td>$&gt;0.4$</td>
<td>$\cdots$</td>
</tr>
<tr>
<td>$m_{\text{eff}}$</td>
<td>$&gt;2000$ GeV</td>
<td>$&gt;500$ GeV</td>
</tr>
</tbody>
</table>

### Table V

The expected and observed numbers of events in the photon + jets signal regions. The quoted errors are the combined statistical and systematic uncertainties.

<table>
<thead>
<tr>
<th>Signal region</th>
<th>SR$<em>{L</em>{175}}^{j}$</th>
<th>SR$<em>{L</em>{200}}^{j}$</th>
<th>SR$_{W}^{j}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\gamma$ + jets (QCD)</td>
<td>$0.06^{+0.21}_{-0.00}$</td>
<td>$0.42^{+0.43}_{-0.42}$</td>
<td>$0.14 \pm 0.14$</td>
</tr>
<tr>
<td>$W\gamma$</td>
<td>$0.54 \pm 0.24$</td>
<td>$0.81 \pm 0.22$</td>
<td>$0.40 \pm 0.26$</td>
</tr>
<tr>
<td>$Z\gamma$</td>
<td>$0.31 \pm 0.16$</td>
<td>$0.36 \pm 0.13$</td>
<td>$0.42 \pm 0.19$</td>
</tr>
<tr>
<td>$t\bar{t}\gamma$</td>
<td>$0.30 \pm 0.11$</td>
<td>$0.54 \pm 0.17$</td>
<td>$0.07 \pm 0.03$</td>
</tr>
<tr>
<td>$e \rightarrow \gamma$</td>
<td>$0.07 \pm 0.03$</td>
<td>$0.16 \pm 0.06$</td>
<td>$0.04 \pm 0.04$</td>
</tr>
<tr>
<td>$\gamma$/$W\gamma$/$Z\gamma$</td>
<td>$0.03 \pm 0.01$</td>
<td>$0.03 \pm 0.01$</td>
<td>$0.06 \pm 0.02$</td>
</tr>
<tr>
<td>Expected background events</td>
<td>$1.33^{+0.58}_{-0.32}$</td>
<td>$2.68^{+0.64}_{-0.63}$</td>
<td>$1.14^{+0.61}_{-0.36}$</td>
</tr>
<tr>
<td>Observed events</td>
<td>4</td>
<td>8</td>
<td>3</td>
</tr>
</tbody>
</table>

### Table VI

Definition, expected content, and observed content of the six validation regions used to confirm the accuracy of the modeling of the $\gamma$ + jets background to the photon + jets analysis. Here, $E_{\gamma}^{T}$ is the transverse energy of the leading photon, $N_{\text{lep}}$ is the number of required leptons, $N_{\text{jets}}$ is the number of required jets, and $N_{\text{exp}}$ and $N_{\text{obs}}$ are the expected and observed numbers of events, respectively. The remainder of the quantities are defined in the text. The uncertainties in the expected numbers of events are the combined statistical and systematic uncertainties. An ellipsis is entered when no such requirement is made in the given validation region.

<table>
<thead>
<tr>
<th>VR$^{j}$</th>
<th>VR$^{j}$</th>
<th>VR$^{j}$</th>
<th>VR$^{j}$</th>
<th>VR$^{j}$</th>
<th>VR$^{j}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$E_{\gamma}^{T}$ [GeV]</td>
<td>$&gt;145$</td>
<td>$&gt;145$</td>
<td>$&gt;145$</td>
<td>$&gt;400$</td>
<td>$&gt;400$</td>
</tr>
<tr>
<td>$N_{\text{lep}}$</td>
<td>$0$</td>
<td>$0$</td>
<td>$0$</td>
<td>$0$</td>
<td>$0$</td>
</tr>
<tr>
<td>$N_{\text{jets}}$</td>
<td>$\geq 5$</td>
<td>$\geq 5$</td>
<td>$\geq 5$</td>
<td>$\geq 3$</td>
<td>$\geq 3$</td>
</tr>
<tr>
<td>$\Delta \phi(\text{jet}, E_{\text{miss}}^{\gamma})$</td>
<td>$&gt;0.4$</td>
<td>$&gt;0.4$</td>
<td>$&gt;0.4$</td>
<td>$&gt;0.4$</td>
<td>$&gt;0.4$</td>
</tr>
<tr>
<td>$\Delta \phi(\gamma, E_{\text{miss}}^{\gamma})$</td>
<td>$&gt;0.4$</td>
<td>$&gt;0.4$</td>
<td>$&gt;0.4$</td>
<td>$&gt;0.4$</td>
<td>$&gt;0.4$</td>
</tr>
<tr>
<td>$E_{\text{miss}}^{\gamma}$ [GeV]</td>
<td>$50$–175</td>
<td>$75$–175</td>
<td>$100$–175</td>
<td>$100$–175</td>
<td>$125$–175</td>
</tr>
<tr>
<td>$R_{T}^{j}$ [GeV]</td>
<td>$&lt;0.90$</td>
<td>$&lt;0.90$</td>
<td>$&lt;0.90$</td>
<td>$\cdots$</td>
<td>$\cdots$</td>
</tr>
<tr>
<td>$N_{\text{exp}}$</td>
<td>$112 \pm 20$</td>
<td>$42 \pm 11$</td>
<td>$10.9 \pm 4.1$</td>
<td>$120 \pm 36$</td>
<td>$36.6 \pm 9.9$</td>
</tr>
<tr>
<td>$N_{\text{obs}}$</td>
<td>108</td>
<td>41</td>
<td>15</td>
<td>126</td>
<td>40</td>
</tr>
</tbody>
</table>

92006-11
TABLE VII. Definition, expected content, and observed content of the five validation regions used to confirm the accuracy of the modeling of the $W\gamma$, $t\bar{t}\gamma$, and electron-to-photon misidentification backgrounds to the photon + jets analysis. Here, $E_T^\gamma$ is the transverse energy of the leading photon, $N_{\text{lep}}$ is the number of required leptons, $N_{\text{jets}}$ is the number of required jets, $N_{b\text{-jets}}$ is the number of required $b$-quark jets, and $N_{\text{exp}}$ and $N_{\text{obs}}$ are the expected and observed numbers of events, respectively. The remainder of the quantities are defined in the text. The uncertainties in the expected numbers of events are the combined statistical and systematic uncertainties. An ellipsis is entered when no such requirement is made in the given validation region.

<table>
<thead>
<tr>
<th>Region</th>
<th>$E_T^\gamma$ [GeV]</th>
<th>$N_{\text{lep}}$</th>
<th>$N_{\text{jets}}$</th>
<th>$N_{b\text{-jets}}$</th>
<th>$\Delta \phi(\gamma, E_T^{\text{miss}})$</th>
<th>$E_T^{\text{miss}}$ [GeV]</th>
<th>$m_{\text{eff}}$ [GeV]</th>
<th>$N_{\text{exp}}$</th>
<th>$N_{\text{obs}}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>VR7\text{L}</td>
<td>$&gt;145$</td>
<td>$\geq 1$</td>
<td>$\geq 2$</td>
<td>$\ldots$</td>
<td>$&gt;0.4$</td>
<td>$&lt;200$</td>
<td>$&gt;1000$</td>
<td>$408 \pm 79$</td>
<td>$410$</td>
</tr>
<tr>
<td>VR8\text{L}</td>
<td>$&gt;145$</td>
<td>$\geq 1$</td>
<td>$\geq 2$</td>
<td>$\ldots$</td>
<td>$&gt;0.4$</td>
<td>$&lt;200$</td>
<td>$&gt;1500$</td>
<td>$66 \pm 12$</td>
<td>$59$</td>
</tr>
<tr>
<td>VR9\text{L}</td>
<td>$&gt;145$</td>
<td>$\geq 1$</td>
<td>$\geq 2$</td>
<td>$\ldots$</td>
<td>$&lt;0.4$</td>
<td>$&gt;200$</td>
<td>$[1000, 2000]$</td>
<td>$127 \pm 23$</td>
<td>$127$</td>
</tr>
<tr>
<td>VR10\text{L}</td>
<td>$&gt;145$</td>
<td>$\geq 1$</td>
<td>$\geq 2$</td>
<td>$\ldots$</td>
<td>$&lt;0.4$</td>
<td>$&gt;200$</td>
<td>$[500, 2000]$</td>
<td>$12.1 \pm 2.1$</td>
<td>$11$</td>
</tr>
<tr>
<td>VR11\text{L}</td>
<td>$&gt;145$</td>
<td>$\ldots$</td>
<td>$\ldots$</td>
<td>$\ldots$</td>
<td>$\ldots$</td>
<td>$\ldots$</td>
<td>$\ldots$</td>
<td>$87 \pm 12$</td>
<td>$94$</td>
</tr>
</tbody>
</table>

the confirmation of the modeling of backgrounds arising from $W\gamma$ and $t\bar{t}\gamma$ production and from the misidentification of electrons as photons. Figure 6 shows the comparison between the expected and observed content in the VRs, with the expected content broken down into its contributing SM sources.

Figure 7 shows the distribution of the missing transverse momentum $E_T^{\text{miss}}$ for the sample satisfying all requirements of the SR\text{L} (left) and SR\text{H} or SR\text{L,200} (right) selection except the $E_T^{\text{miss}}$ requirement itself. Overlaid are the expected SM backgrounds, separated into the various contributing sources.

VIII. SIGNAL YIELD AND ASSOCIATED UNCERTAINTIES

GGM signal acceptances and efficiencies are estimated using MC simulation for each simulated point in the gluino-bino, wino-bino, squark-bino, and higgsino-bino parameter spaces, and vary widely across the regions of these spaces relevant to establishing the model constraints presented below. The product of acceptance and efficiency tends to be greatest (30%–35%) when the masses of both the produced and the NLSP states are largest, leading to large amounts of both visible energy and missing transverse momentum that would clearly distinguish signal from background events. However, for the more restrictive selection of the photon + jets analysis, particularly when the NLSP mass is small, the product of acceptance and efficiency can be significantly smaller. For example, for the region relevant to establishing limits at low values of $m_{\tilde{\chi}^0_1}$, the acceptance times efficiency of the SR\text{L} selection is of the order of 0.1%, leading to a relatively modest constraint on the mass of produced SUSY states.

The MC-based estimate of the signal yield is affected by various experimental systematic uncertainties, described...
below. The resulting experimental systematic uncertainty in the signal yield is incorporated in the determination of limits on the mass parameters of the various GGM signal models considered in this search.

The uncertainty in the integrated luminosity is 2.1%. It is derived, following a methodology similar to that detailed in Ref. [68], from a calibration of the luminosity scale using \(x-y\) beam-separation scans performed in August 2015 and May 2016. Making use of a bootstrap method, the efficiency of the single-photon trigger is determined to be greater than 99%, with an uncertainty of less than \(\pm 1\%\), for photons satisfying the photon + jets selection criteria [29]. The diphoton trigger efficiency is found to be close to 100% for events satisfying the diphoton analysis selection criteria, with an uncertainty of less than \(\pm 0.4\%\).

The \(\eta\)-dependent uncertainty in the efficiency of photon identification, determined as described in Ref. [58], is between \(\pm 0.2\%\) and \(\pm 0.4\%\) for \(E_T^\gamma < 200\) GeV, and between \(\pm 1\%\) and \(\pm 4\%\) for larger values of \(E_T^\gamma\). The uncertainty in the energy scale for electrons and photons with high \(E_T\), determined as described in Ref. [55], varies with \(\eta\) over the range \(\pm (0.5-1.5)\%\). For high \(E_T\), the uncertainty in the photon energy resolution is dominated by the uncertainty in the constant term of the calorimetric energy resolution; at \(E_T = 300\) GeV, the relative uncertainty is \(\pm (30-40)\%\) depending on \(\eta\). For jets with \(100 < p_T < 500\) GeV, the uncertainty in the jet energy scale is found to be less than \(\pm 1\%\) [64]. Due to uncertainties in corrections for pileup, this uncertainty rises with falling \(p_T\), reaching a value of about \(\pm 4.5\%\) at \(p_T = 20\) GeV. Uncertainties in the values of whole-event observables, such as \(E_T^{\text{miss}}\) and \(H_T\), arise from uncertainties in the energy of the objects from which they are constructed. In addition, the \(E_T^{\text{miss}}\) observable receives a contribution from tracks associated with the primary vertex but not associated with any of the reconstructed objects in the event [69]. Uncertainties arising from the inclusion of these unassigned contributions are found to contribute negligibly to the overall uncertainty in the value of the \(E_T^{\text{miss}}\) observable.

In the regions of GGM parameter space relevant for establishing the exclusion limits discussed in Sec. IX, and excepting MC statistical uncertainty, the quadrature sum of the individual sources of systematic uncertainty in the signal reconstruction efficiency in the diphoton analysis is of order \(\pm 5\%\), and is dominated by the uncertainties in photon identification and the calorimetric energy scales. In the photon + jets analysis the systematic uncertainty is larger (approximately \(\pm 20\%\)), due partially to an increased sensitivity to the jet energy scale and resolution associated with the multiple-jet requirement.

**IX. RESULTS**

The number of events observed in each SR is shown in Table VIII, along with the size of the expected SM
TABLE VIII. Summary of the observed number of events ($N_{\text{obs}}$), and the number of events expected from SM sources ($N_{\text{exp}}$), for each of the seven SRs. Also shown are the derived ($\sigma_{\text{obs}}^{95}$) and expected ($\sigma_{\text{exp}}^{95}$) model-independent 95% C.L. limits on the number of events from non-SM processes, and the observed ($\langle\Delta\sigma\rangle_{95}^{\text{exp}}$) and expected ($\langle\Delta\sigma\rangle_{95}^{\text{exp}}$) 95% C.L. limits on the visible cross section from non-SM processes. The last column of the table shows the significance $Z$ of the observed excess (if any), and the probability $p$, capped at 0.5, that an experiment with only background fluctuates to at least the observed number of events.

<table>
<thead>
<tr>
<th>Signal region</th>
<th>$N_{\text{obs}}$</th>
<th>$N_{\text{exp}}$</th>
<th>$\sigma_{\text{obs}}^{95}$</th>
<th>$\sigma_{\text{exp}}^{95}$</th>
<th>$\langle\Delta\sigma\rangle_{95}^{\text{exp}}$ [fb]</th>
<th>$\langle\Delta\sigma\rangle_{95}^{\text{exp}}$ [fb]</th>
<th>$Z$ ($p$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$SR_{7-L}$</td>
<td>0</td>
<td>0.50$^{+0.30}_{-0.26}$</td>
<td>3.0</td>
<td>3.1$^{+1.4}_{-1.2}$</td>
<td>0.083</td>
<td>0.086$^{+0.039}_{-0.003}$</td>
<td>0.00 (0.50)</td>
</tr>
<tr>
<td>$SR_{7-H}$</td>
<td>0</td>
<td>0.48$^{+0.30}_{-0.25}$</td>
<td>3.0</td>
<td>3.1$^{+1.3}_{-0.1}$</td>
<td>0.083</td>
<td>0.086$^{+0.036}_{-0.003}$</td>
<td>0.00 (0.50)</td>
</tr>
<tr>
<td>$SR_{W-L}$</td>
<td>6</td>
<td>3.7$^{+1.1}_{-0.6}$</td>
<td>8.6</td>
<td>5.8$^{+2.8}_{-1.6}$</td>
<td>0.238</td>
<td>0.161$^{+0.078}_{-0.044}$</td>
<td>1.06 (0.14)</td>
</tr>
<tr>
<td>$SR_{W-H}$</td>
<td>1</td>
<td>2.05$^{+0.65}_{-0.63}$</td>
<td>3.7</td>
<td>4.4$^{+1.9}_{-1.0}$</td>
<td>0.103</td>
<td>0.122$^{+0.053}_{-0.028}$</td>
<td>0.00 (0.50)</td>
</tr>
<tr>
<td>$SR_{L}$</td>
<td>4</td>
<td>1.33$^{+0.54}_{-0.32}$</td>
<td>7.6</td>
<td>4.7$^{+1.6}_{-0.8}$</td>
<td>0.210</td>
<td>0.130$^{+0.044}_{-0.022}$</td>
<td>1.81 (0.035)</td>
</tr>
<tr>
<td>$SR_{L200}$</td>
<td>8</td>
<td>2.68$^{+0.64}_{-0.63}$</td>
<td>11.5</td>
<td>5.4$^{+2.2}_{-1.2}$</td>
<td>0.318</td>
<td>0.151$^{+0.033}_{-0.033}$</td>
<td>2.36 (0.009)</td>
</tr>
<tr>
<td>$SR_{L1}$</td>
<td>3</td>
<td>1.14$^{+0.51}_{-0.36}$</td>
<td>6.6</td>
<td>5.9$^{+1.8}_{-1.1}$</td>
<td>0.183</td>
<td>0.162$^{+0.030}_{-0.030}$</td>
<td>1.20 (0.116)</td>
</tr>
</tbody>
</table>

These results are also illustrated in Figs. 4 and 6, with the expected background broken down into its contributing SM sources. No significant evidence of physics beyond the SM is observed in any of the SRs.

The most significant excess relative to the expected background is observed in $SR_{L200}$ of the photon + jets analysis. Considering both statistical and systematic uncertainty, and assuming that all observed events are from SM sources, an observation of eight or more events over an expected background of $2.68_{-0.63}^{+0.64}$ events represents an upward fluctuation with a probability of occurrence of approximately 0.9%.

Based on the observed and expected numbers of events in the seven SRs shown in Table VIII, 95% C.L. upper limits are set for each SR on the number of events from any scenario of physics beyond the SM. These limits are based on the profile likelihood ratio [70] and CL$_{s}$ [71] prescriptions, making use of the likelihood function described in Sec. VII. Assuming that no events due to physical processes beyond those of the SM populate the various CRs used to estimate SR backgrounds, observed 95% C.L. upper limits on the number of such events vary between 3.0 (for $SR_{7-H}$ and $SR_{7-L}$) and 11.5 (for $SR_{L200}$). Dividing by the integrated luminosity of 36.1 fb$^{-1}$, these number-of-event limits translate into 95% C.L. upper limits on the visible cross section for new physics, defined as the product of cross section, branching fraction, acceptance, and efficiency, for the different SR definitions. Here, the acceptance ($A$) is defined to be the fraction of events whose underlying objects pass all kinematic and whole-event selection requirements, and the efficiency ($\epsilon$) to be the fraction of those events that would be observed after reconstruction in the detector. The resulting observed visible cross-section limits vary between 0.083 fb and 0.32 fb.

By considering, in addition to the event counts in the SRs, the values and uncertainties of the acceptance times efficiency of the SR selection requirements, as well as the NLO (+NLL) GGM cross sections [38-44], 95% C.L. lower limits are set on the masses of the accessible SUSY states of the GGM scenarios explored in this study. The SR with the best expected sensitivity at each simulated point in the parameter space of the corresponding GGM model(s) is used to determine the degree of exclusion of that model point.

For the diphoton analysis, in the region of gluino (squark) mass near the expected 95% C.L. exclusion limit, $SR_{7-H}$ is expected to provide the greatest sensitivity to the gluino-bino (squark-bino) model for bino masses above 1600 GeV (900 GeV), with a transition to $SR_{W-L}$ for bino masses below this value. For the wino-bino model, the similar transition point between the use of $SR_{W-L}$ and $SR_{W-H}$ is found to be at 400 GeV. The resulting observed limits on the gluino and wino masses are exhibited, as a function of bino mass, for the diphoton analysis gluino, squark, and wino production models in Figs. 8, 9, and 10 respectively. For the wino production model, the discontinuity at $m_{\tilde{g}} = 400$ GeV is due to the small excess of events observed in the $SR_{W-L}$ signal region.

For the purpose of establishing these model-dependent limits, both the normalization of the $W(\rightarrow l\nu) + \gamma\gamma$ background estimate and the limit on the possible number of events from new physics are extracted from a simultaneous fit to the SR and $W(\rightarrow l\nu) + \gamma\gamma$ control region. However, for masses near the various diphoton-analysis exclusion limits, the signal contamination in the $W(\rightarrow l\nu) + \gamma\gamma$ control sample is appreciable only for the wino-bino parameter space, reaching approximately 0.4 events (4% of the 9.1 events in the $l\gamma\gamma$ CR attributed to the $W(\rightarrow l\nu) + \gamma\gamma$ process) as the bino mass approaches zero. Also shown in these three figures, as well as in Fig. 11, are the expected limits, including their statistical and background uncertainty ranges, as well as observed limits for SUSY model cross sections ±1 standard deviation of theoretical uncertainty from their central value.
FIG. 8. Exclusion limits in the gluino-bino mass plane, using the SR$_{S\rightarrow H}$ analysis for $m_{\tilde{g}} > 1600$ GeV and the SR$_{S\rightarrow L}$ analysis for $m_{\tilde{g}} < 1600$ GeV. Combinations of gluino and bino mass are excluded at greater than 95% C.L. in the area to the left of the unbroken curve. The observed limits are exhibited for the nominal SUSY model cross-section expectation, as well as for a SUSY cross section increased and decreased by 1 standard deviation of the cross-section systematic uncertainty. Also shown is the expected limit, as well as the ±1 standard-deviation range of the expected limit, which is asymmetric due to the small expected number of events. The gray region is that previously excluded with the 2015 data sample; see Ref. [3].

FIG. 9. Exclusion limits in the squark-bino mass plane, using the SR$_{S\rightarrow H}$ analysis for $m_{\tilde{g}} > 900$ GeV and the SR$_{S\rightarrow L}$ analysis for $m_{\tilde{g}} < 900$ GeV. Combinations of squark and bino mass are excluded at greater than 95% C.L. in the area to the left of the unbroken curve. The observed limits are exhibited for the nominal SUSY model cross-section expectation, as well as for a SUSY cross section increased and decreased by 1 standard deviation of the cross-section systematic uncertainty. Also shown is the expected limit, as well as the ±1 standard-deviation range of the expected limit, which is asymmetric due to the small number of expected events.

FIG. 10. Exclusion limits in the wino-bino mass plane, using the SR$_{W\rightarrow H}$ analysis for $m_{\tilde{g}} > 400$ GeV and the SR$_{W\rightarrow L}$ analysis for $m_{\tilde{g}} < 400$ GeV. The vertical axis represents bino mass while the horizontal axis represents wino mass. Combinations of wino and bino masses are excluded at greater than 95% C.L. in the area to the left of the unbroken curve. The observed limits are exhibited for the nominal SUSY model cross-section expectation, as well as for a SUSY cross section increased and decreased by 1 standard deviation of the cross-section systematic uncertainty. Also shown is the expected limit, along with its ±1 standard-deviation range. The discontinuity at $m_{\tilde{g}} = 400$ GeV is due to the switch between the use of the SR$_{W\rightarrow L}$ and SR$_{W\rightarrow H}$ analyses, the former of which exhibits a small excess of observed events relative to the expected SM background. The gray region is that previously excluded with the data sample taken at $\sqrt{s} = 8$ TeV; see Ref. [6].

Considering all possible values of the $\chi^0_1$ mass, 95% C.L. lower limits of 2150 GeV, 1820 GeV, and 1060 GeV are set by the diphoton analysis on the value of the gluino, squark, or wino mass, respectively, for any value of the NLSP bino mass less than that of the gluino, squark, or wino mass. Based on a sample of 35.9 fb$^{-1}$ of $p p$ data accumulated at $\sqrt{s} = 13$ TeV, and assuming a branching fraction of 100% for the photonic decay of the $\chi^0_1$, the CMS Collaboration has set 95% C.L. lower limits of 1790 GeV and 1580 GeV for similar models of gluino and squark production and decay, respectively [4]. For a GGM model similar to the wino-bino model of the diphoton analysis, a separate CMS Collaboration analysis [4] has set a 95% C.L. lower limit as high as 1000 GeV on the wino mass, depending on the value of the bino-like $\chi^0_1$ mass.

Using the photon + jets analysis, limits are set in the two-dimensional plane of the masses of the gluino and the mixed higgsino-bino NLSP. For values of $m_{\tilde{g}}$ and $m_{\chi_1^0}$ close to the expected 95% C.L. exclusion limit, SR$_{S\rightarrow L}$ is expected to provide a greater sensitivity for NLSP masses below approximately 1500 GeV, and so is made use of in this region; for higher NLSP masses, SR$_{S\rightarrow H}$ is used to establish the degree of exclusion of points in the GGM-model.
parameter space. The resulting observed exclusion contour is shown in Fig. 11. In the context of this GGM model, lower limits as high as 2050 GeV are established for the gluino mass, depending on the value of $m_{\tilde{\chi}^0_1}$. The sensitivity of the analysis has not been explored for values of the NLSP mass within 50 GeV of that of the gluino, where the selection efficiency diminishes due to the restriction of phase space for producing multiple high-$p_T$ jets, and the tendency of the gluino to become metastable as the splitting between the gluino and $\tilde{\chi}^0_1$ masses becomes small.

X. CONCLUSION

Making use of proton-proton collision data at $\sqrt{s} = 13$ TeV corresponding to an integrated luminosity of 36.1 fb$^{-1}$ recorded by the ATLAS detector at the LHC in 2015 and 2016, a search is performed for photonic signatures of new physics associated with significant missing transverse momentum. Single-photon and diphoton selection strategies were developed and used to search for evidence for several general gauge-mediated SUSY-breaking scenarios. No significant excess of events over the Standard Model expectation is observed in any of the searches, and limits are set on possible contributions of new physics. Model-independent limits between 0.083 fb and 0.32 fb are set on the associated visible cross section of contributions from physics beyond the Standard Model.

Based on these limits on contributions from new physics, model-dependent limits are set on the masses of SUSY particles within the context of GGM. A diphoton signature is used to search for strongly and weakly produced SUSY states with a decay chain proceeding through a binolike next-to-lightest supersymmetric particle (NLSP). In the context of these models, lower limits of 2150, 1820, and 1060 GeV are set on the masses of gluinos, squarks, and a degenerate set of winos, respectively, for any value of the bino mass less than the mass of these produced states. In addition, a photon + jets signature is used to search for an alternative scenario in which the GGM NLSP is a higgsino-bino admixture with a roughly equal branching fraction to photons and $Z$ bosons. In the context of this model, lower limits as high as 2050 GeV are established for the gluino mass, depending on the value of the NLSP mass.

ACKNOWLEDGMENTS

We thank CERN for the very successful operation of the LHC, as well as the support staff from our institutions without whom ATLAS could not be operated efficiently. We acknowledge the support of ANPCyT, Argentina; YerPhI, Armenia; ARC, Australia; BMWFW and FWF, Austria; ANAS, Azerbaijan; SSTC, Belarus; CNPq and FAPESP, Brazil; NSERC, NRC, and CFI, Canada; CERN; CONICYT, Chile; CAS, MOST, and NSFC, China; COLCIENCIAS, Colombia; MSMT CR, MPO CR, and VSC CR, Czech Republic; DNRF and DNSRC, Denmark; IN2P3-CNRS, CEA-DRF/IRFU, France; SRNSFG, Georgia; BMBF, HGF, and MPG, Germany; GSRT, Greece; RGC, Hong Kong SAR, China; ISF, I-CORE, and Benoziyo Center, Israel; INFN, Italy; MEXT and JSPS, Japan; CNRST, Morocco; NWO, Netherlands; RCN, Norway; MNiSW and NCN, Poland; FCT, Portugal; MNE/IFA, Romania; MES of Russia and NRC KI, Russian Federation; JINR; MESTD, Serbia; MSSR, Slovakia; ARRS and MIZŠ, Slovenia; DST/NRF, South Africa; MINECO, Spain; SRC and Wallenberg Foundation, Sweden; SERI, SNSF, and Cantons of Bern and Geneva, Switzerland; MOST, Taiwan; TAEK, Turkey; STFC, United Kingdom; DOE and NSF, United States of America. In addition, individual groups and members have received support from BCKDF, the Canada Council, CANARIE, CRC, Compute Canada, FQRNT, and the Ontario Innovation Trust, Canada; EPLANET, ERC, ERDF, FP7, Horizon 2020, and Marie Sklodowska-Curie Actions, European Union; Investissements d’Avenir Labex and Idex, ANR, Région Auvergne, and Fondation Partager le Savoir, France; DFG and AvH Foundation, Germany; Herakleitos, Thales, and Aristeia programs cofinanced by EU-ESF and the Greek NSRF; BSF, GIF, and Minerva, Israel; BRF, Norway; CERCA Programme Generalitat de Catalunya, Generalitat Valenciana, Spain; the Royal
Society and Leverhulme Trust, United Kingdom. The crucial computing support from all WLCG partners is acknowledged gratefully, in particular from CERN, the ATLAS Tier-1 facilities at TRIUMF (Canada), NDGF (Denmark, Norway, Sweden), CC-IN2P3 (France), KIT/GridKA (Germany), INFN-CNAF (Italy), NL-T1 (Netherlands), PIC (Spain), ASGC (Taiwan), RAL (UK), and BNL (USA), the Tier-2 facilities worldwide, and large non-WLCG resource providers. Major contributors of computing resources are listed in Ref. [72].

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PHYS. REV. D 97, 092006 (2018)

SEARCH FOR PHOTONIC SIGNATURES OF GAUGE- ...

PHYS. REV. D 97, 092006 (2018)


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092006-29
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